Tutorial: Synthesis of control circuits from STG specifications

- Lecturers:
  - Jordi Cortadella (University Politècnica de Catalunya, Spain)
  - Michael Kishinevsky (The University of Aizu, Japan)
- in collaboration with:
  - Alex Kondratyev (The University of Aizu, Japan)
  - Luciano Lavagno
    (Cadence Berkeley Labs, USA and Politecnico di Torino, Italy)
  - Alex Yakovlev (University of Newcastle upon Tyne, UK)

Thanks to Peter Vanbekbergen for previous contributions to this tutorial and to Enric Pastor and Oriol Roig for the development of tools (petrify and versify)

Outline = Design Flow

- Specification
- Synthesis conditions
- State encoding
- Logic decomposition
- Technology mapping
- Verification
- Testing

Appendix 1: Hazards and races

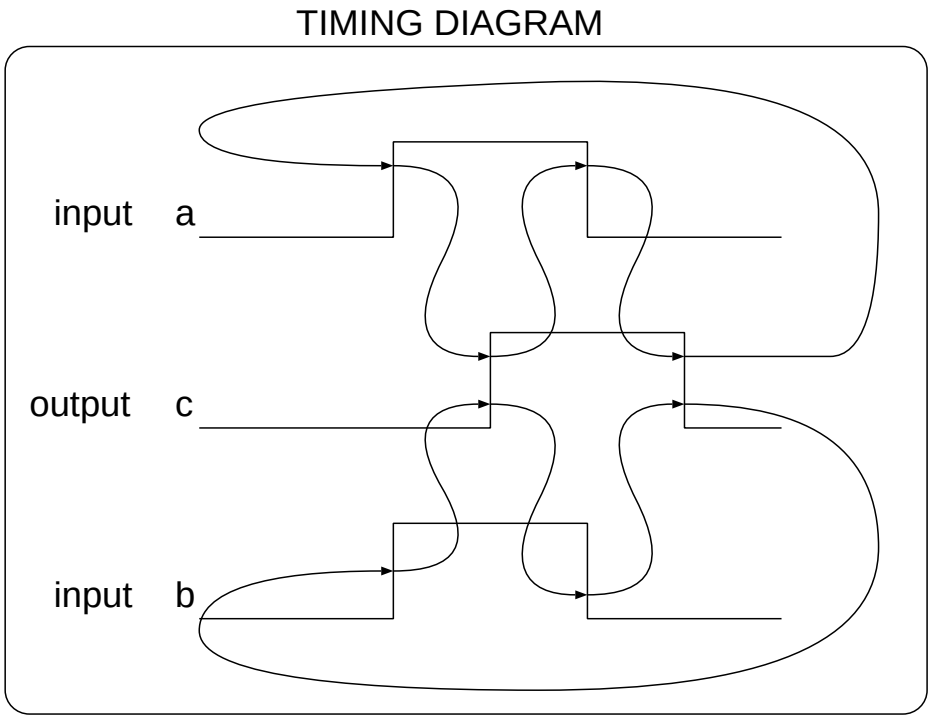
Appendix 2: Other design styles

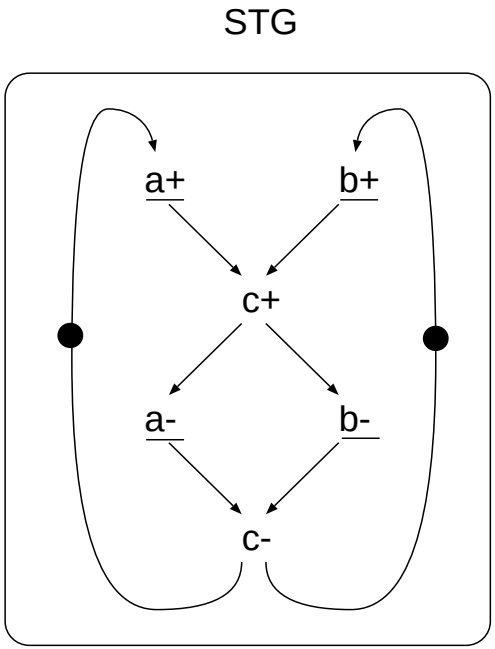
To be presented on Thursday 11:00-12:30

Part 1: Specification of control and synthesis overview

- Formalizing Timing Diagrams
- Signal Transition Graph (STG) model
- Signal Transition Graphs and Petri Nets
- Synthesis overview
- Example with concurrency (handshake communication)
- Example with choice (SR latch with completion)

From Timing Diagram to Formal model

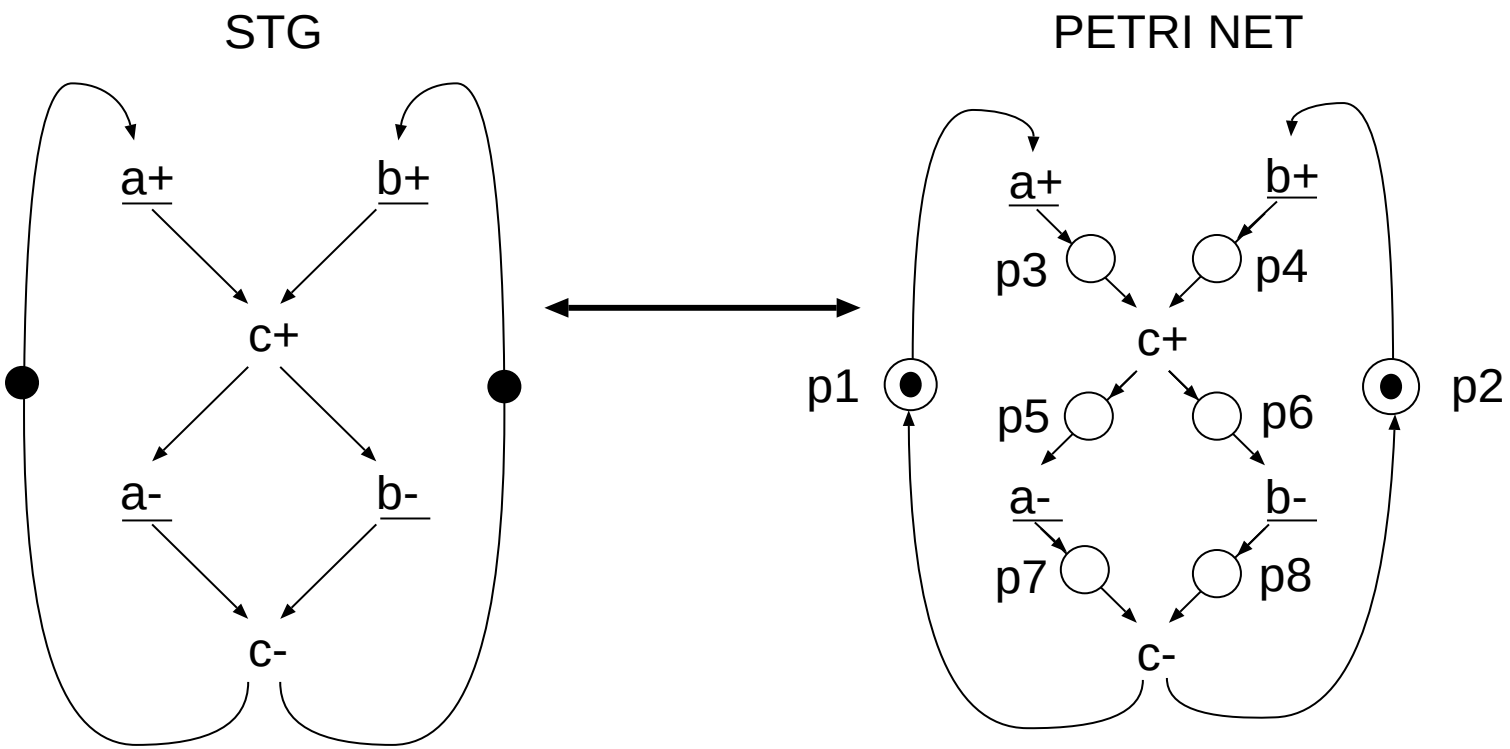




SIGNAL TRANSITION GRAPH(2)

- Vertices represent signal transitions.
- Arcs represent causal relations between transitions.
- Introduced by [Molnar 85] [Chu 87] [Rosenblum 85]

SIGNAL TRANSITION GRAPH



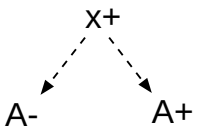
STG is an interpreted Petri net.

CONSISTENCY

INCONSISTENT

A+ ⇢ A+ Two subsequent up-transitions without a down-transition in between

A- ⇢ A- Two subsequent down-transitions without an up-transition in between



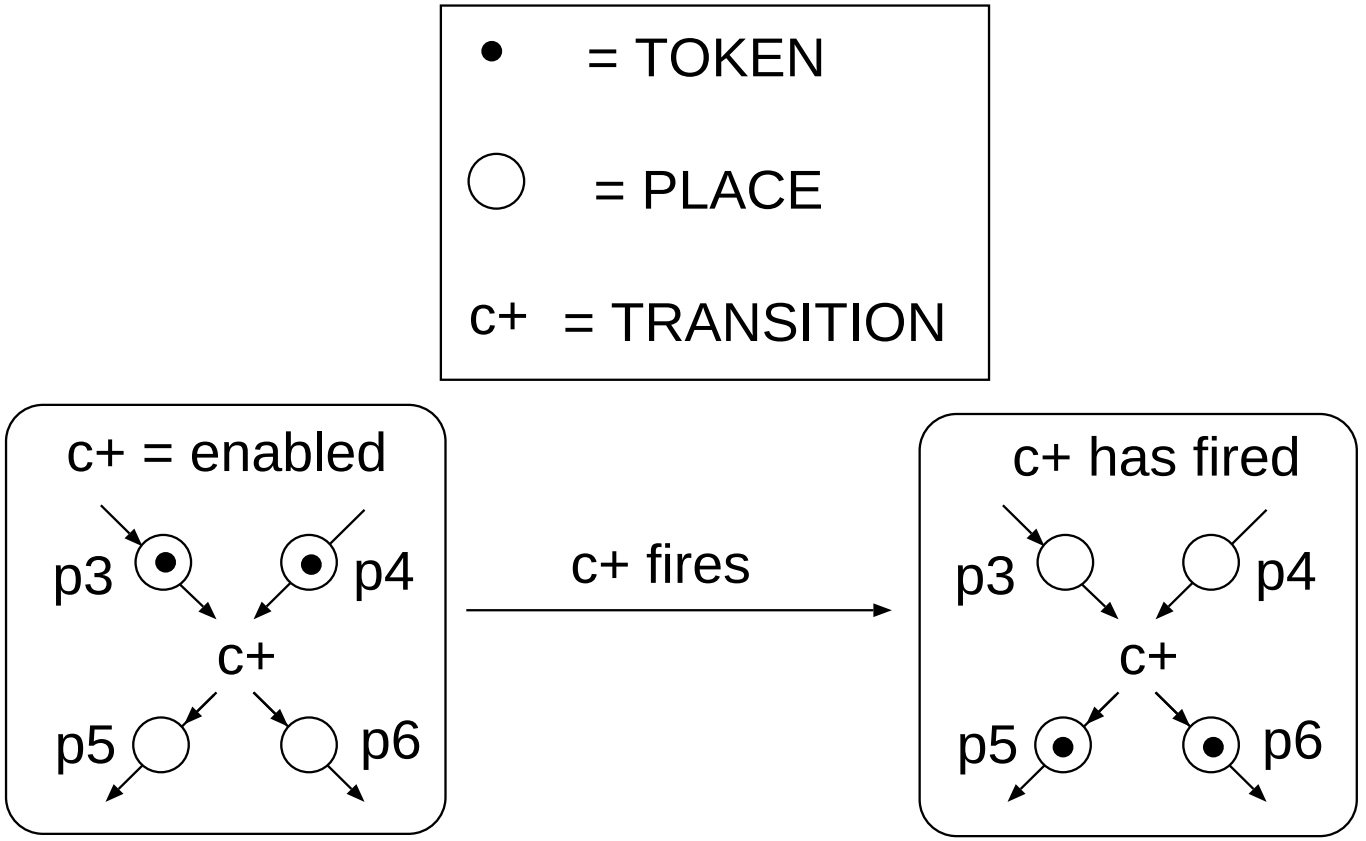
Parallel transitions of the same signal

CONSISTENT

A+ ⇢ A- ⇢ A+

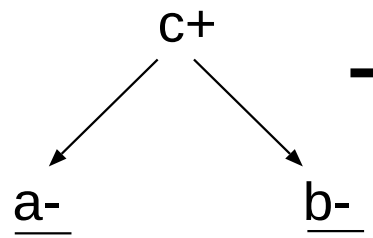
Two up-transitions with a down-transition in between (and vice versa)

FIRING SEMANTICS



MODELING POWER

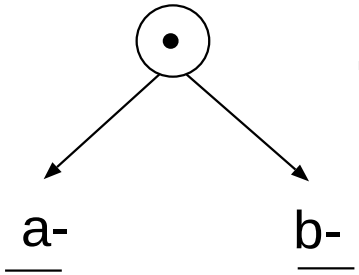
CONCURRENCY



a- concurrent with b-

EITHER a- fires before b-
OR b- fires before a-
OR a- and b- fire simultaneously

CHOICE



EITHER a- fires
OR b- fires
but not both

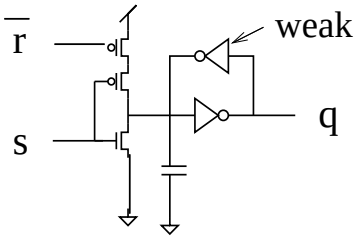
choice made by environment

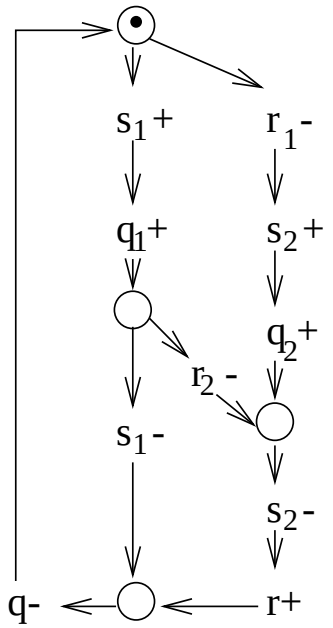
Specification with choice

Set-dominant SR-latch

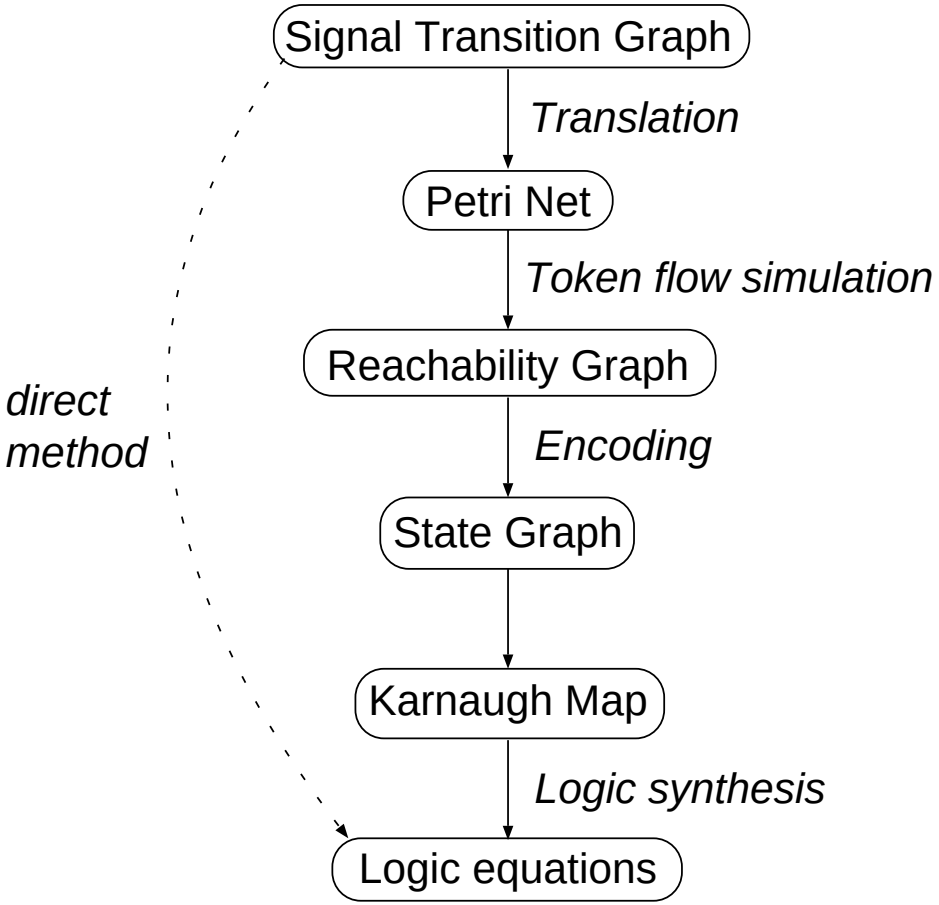
1. Q goes high when S goes high
2. Q goes low when R goes high
   while $S = 0$

Environment determines when
to apply s_1+ and r_1-





Synthesis overview

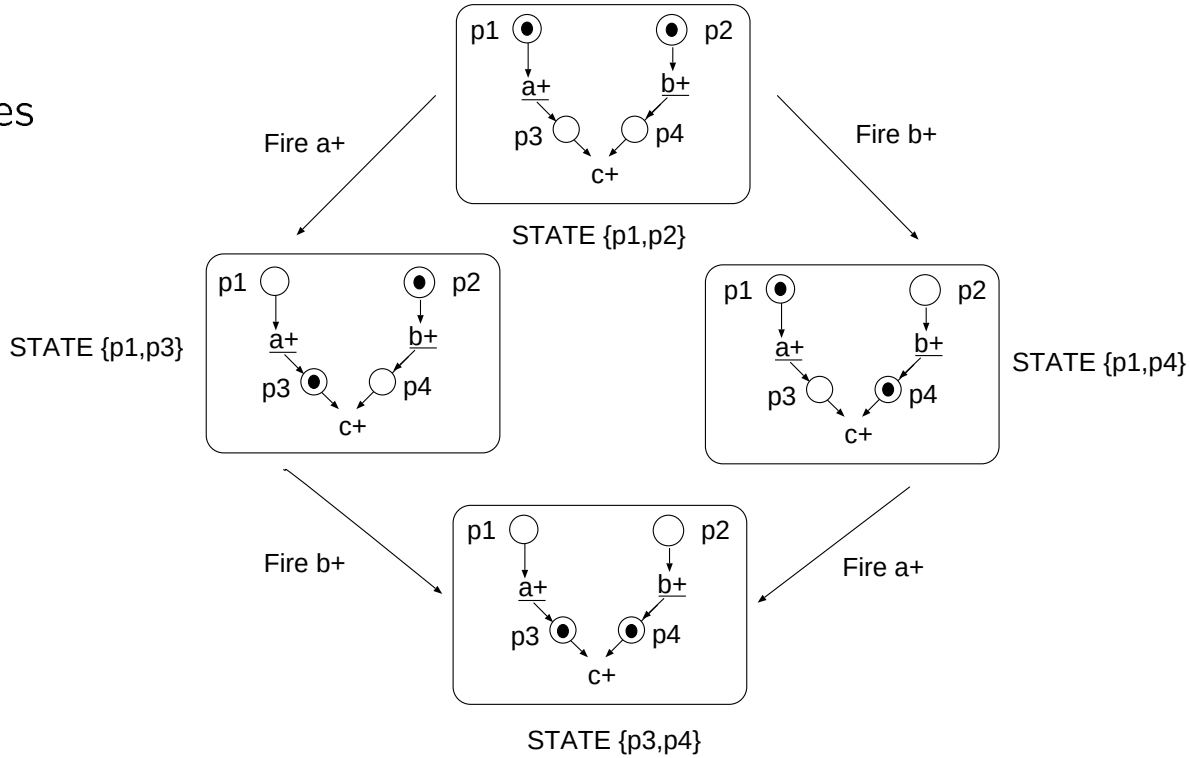


REACHABILITY GRAPH

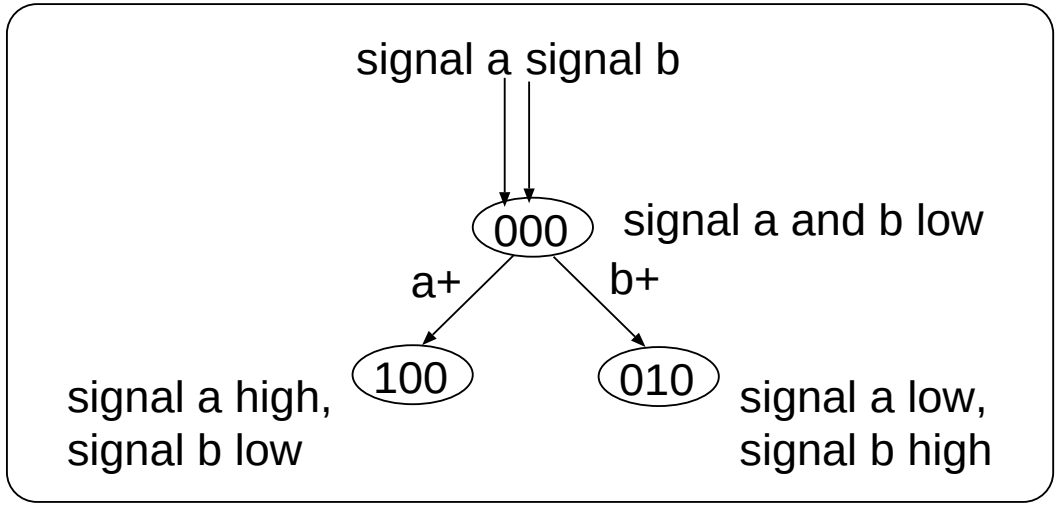
- Vertices represent states the circuit can be in.
- Arcs represent transition from one state to another.
- Can be derived from the Petri net by simulating the token flow.
- Easiest representation to do analysis on.
- Size may be exponential in the number of transitions.
- Similar to trace structures [Dill], transition diagrams [Muller].

Reachability Graph

- Vertices – circuit states
- Arcs – transitions
- Token flow simulation
- Easy for analysis
- Can be exponential

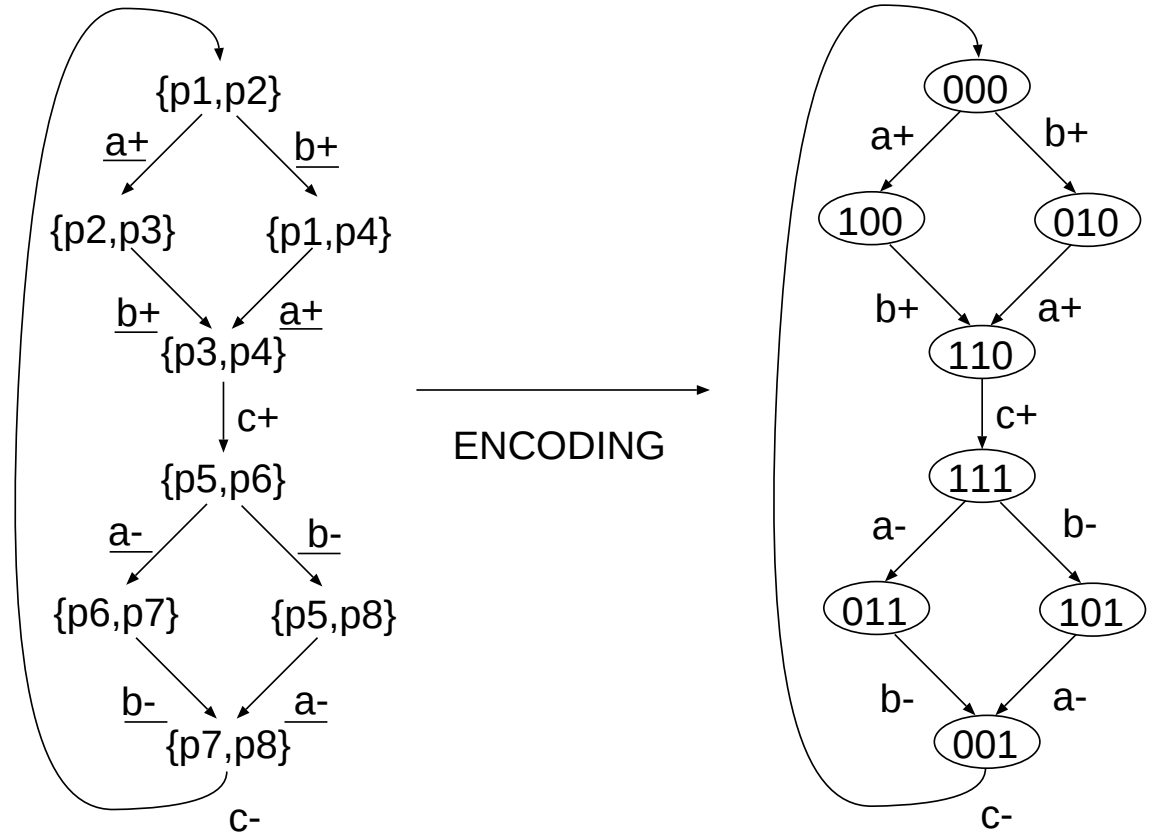


ENCODING



- Every state is assigned a code.
- This code is determined by signals in the *Petri net*.
- Based on this code, logical equations can be derived.

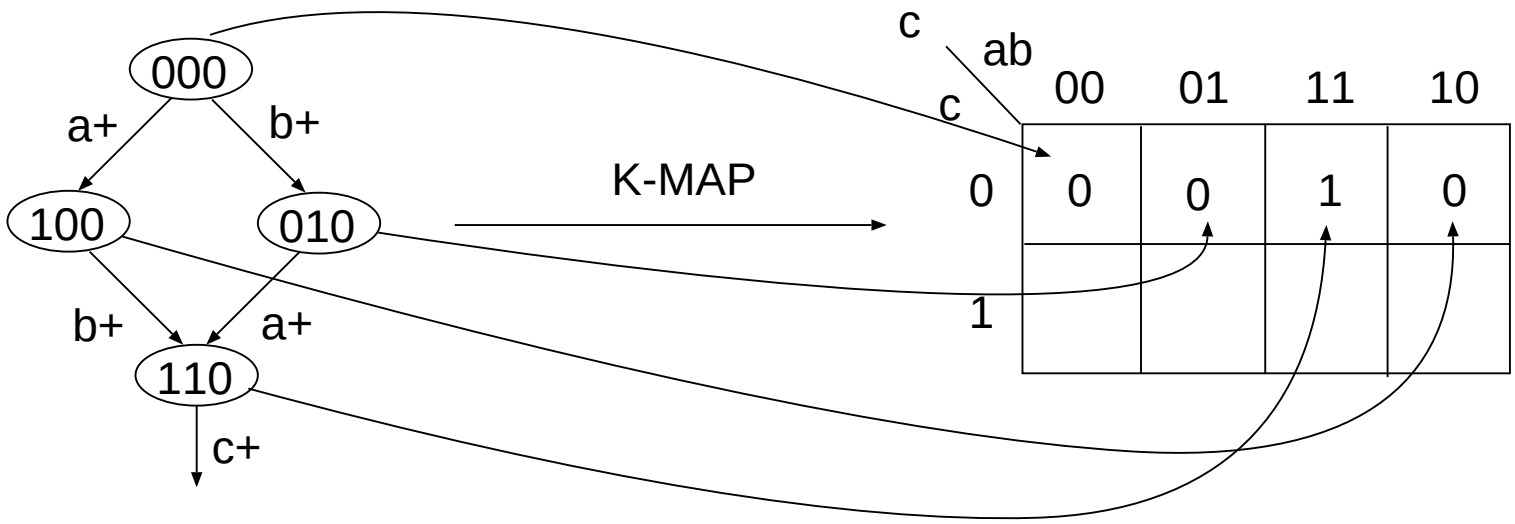
STATE GRAPH



REACHABILITY GRAPH

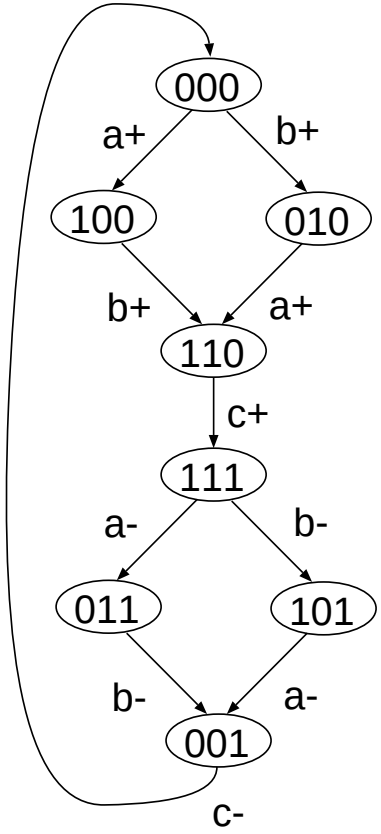
STATE GRAPH

Next State Functions for Signals



- State 000: c is assigned 0 because c stays low in this state.
- State 011: c is assigned 1 because c goes high in this state (c^+ is enabled).

EQUATIONS



STATE GRAPH

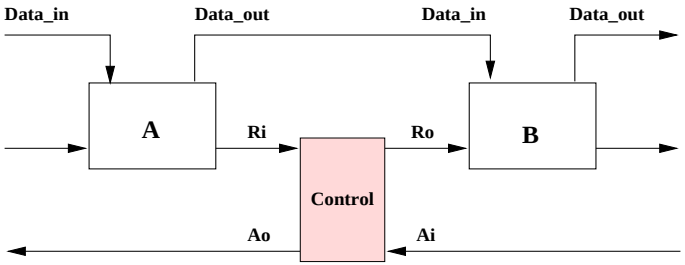
K-MAP

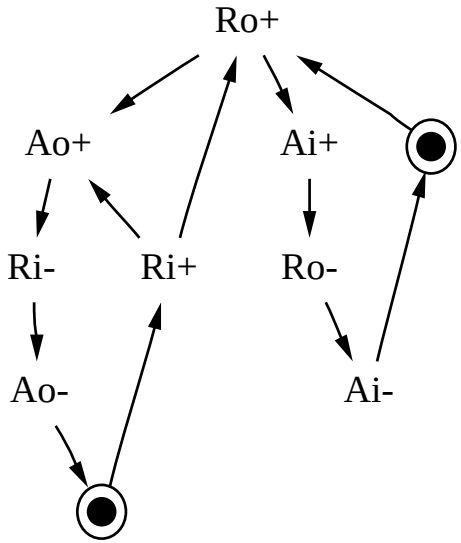
c \ ab	00	01	11	10
0	0	0	1	0
1	0	1	1	1

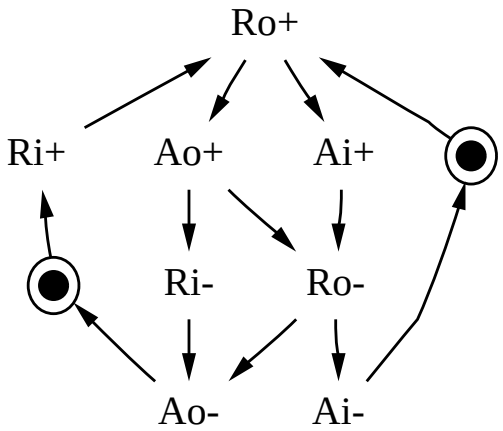
LOGIC EQUATIONS

c = ab + ac + bc

Example: half-handshake circuit

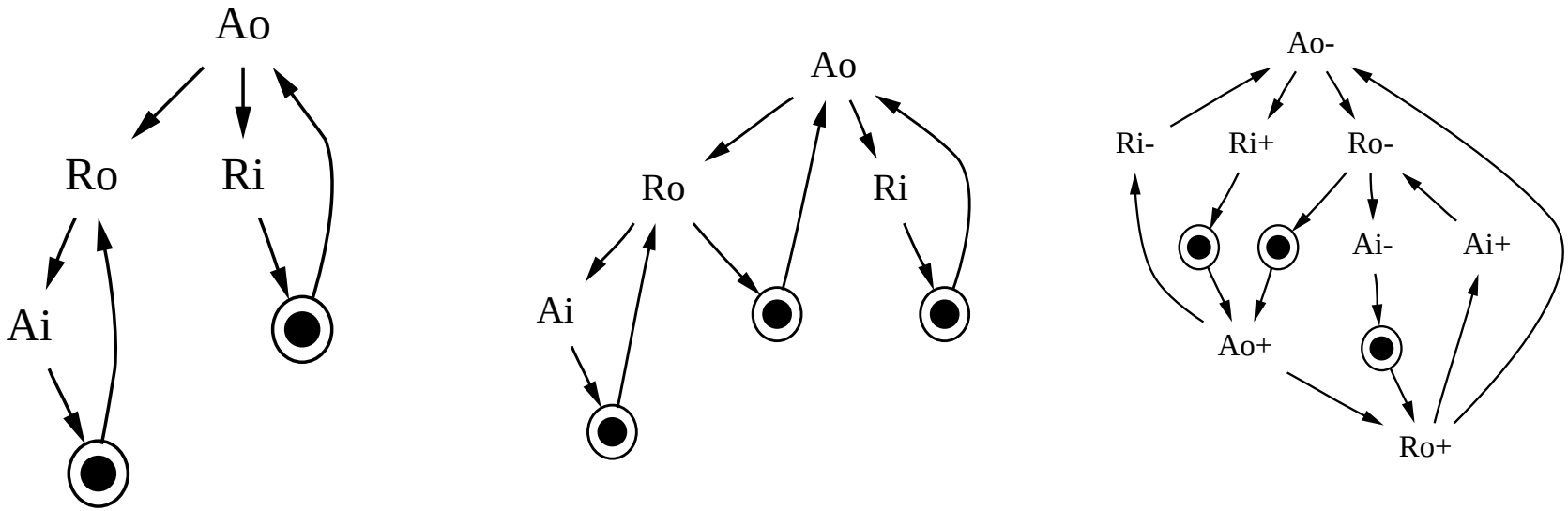






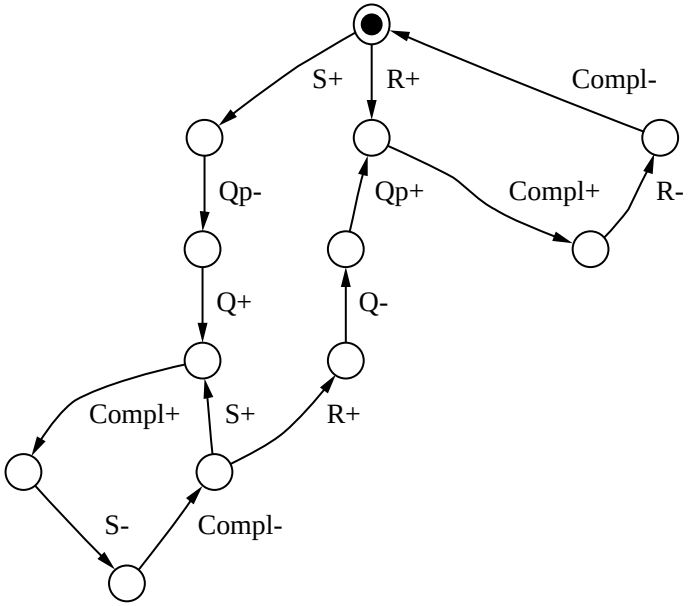
A data processing structure [T.Meng 91] and partial and complete STG specifications of the "half-handshake" control.

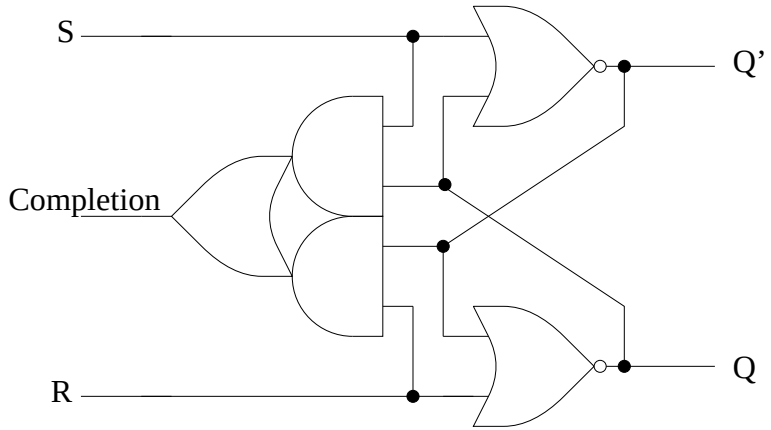
Example: full-handshake circuit



Partial and complete two-phase STG specifications of the "full-handshake" control. A four-phase equivalent of the two-phase specification.

Example: SR-latch with completion detection



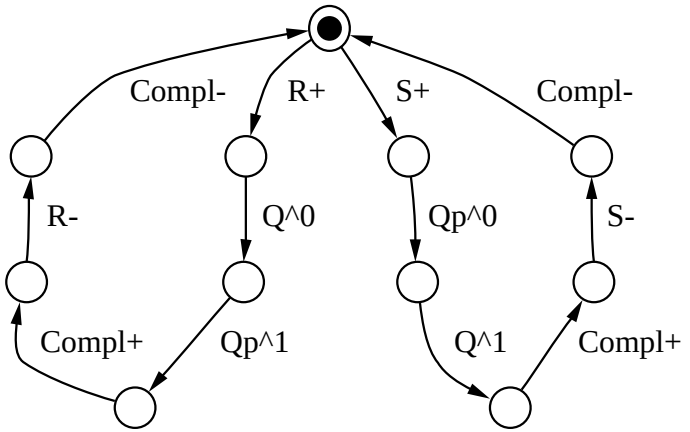


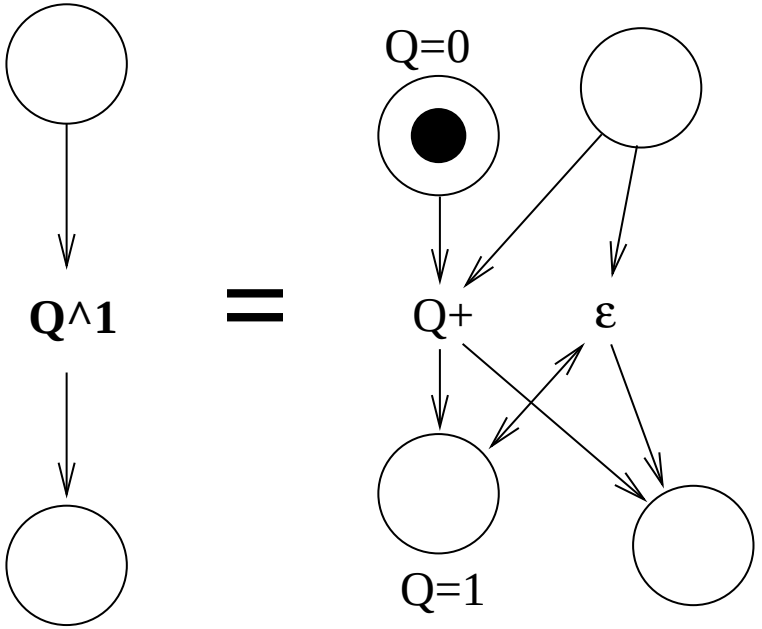
Specification and implementation

Limitations

- The advantages of STG:
  - Concurrency of signal transitions
  - Conditional behavior based on signal transitions
- The disadvantages of STG:
  - Conditional behavior based on signal levels
  - No timing information, just relative ordering of events
  - OR-type behavior is hard to model
- Different extensions have been proposed

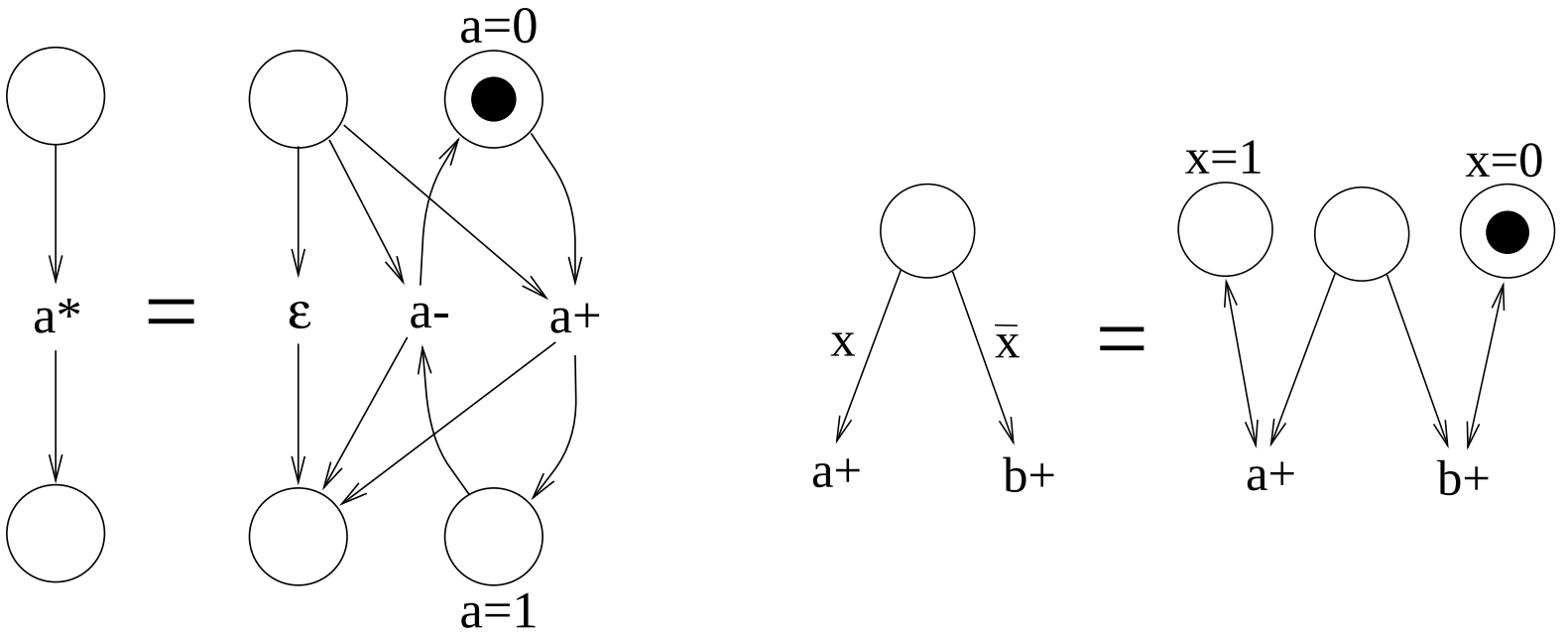
Extensions: level transitions





Assigment of value to signal (with or without transition)

Extensions: DC transitions and boolean guards



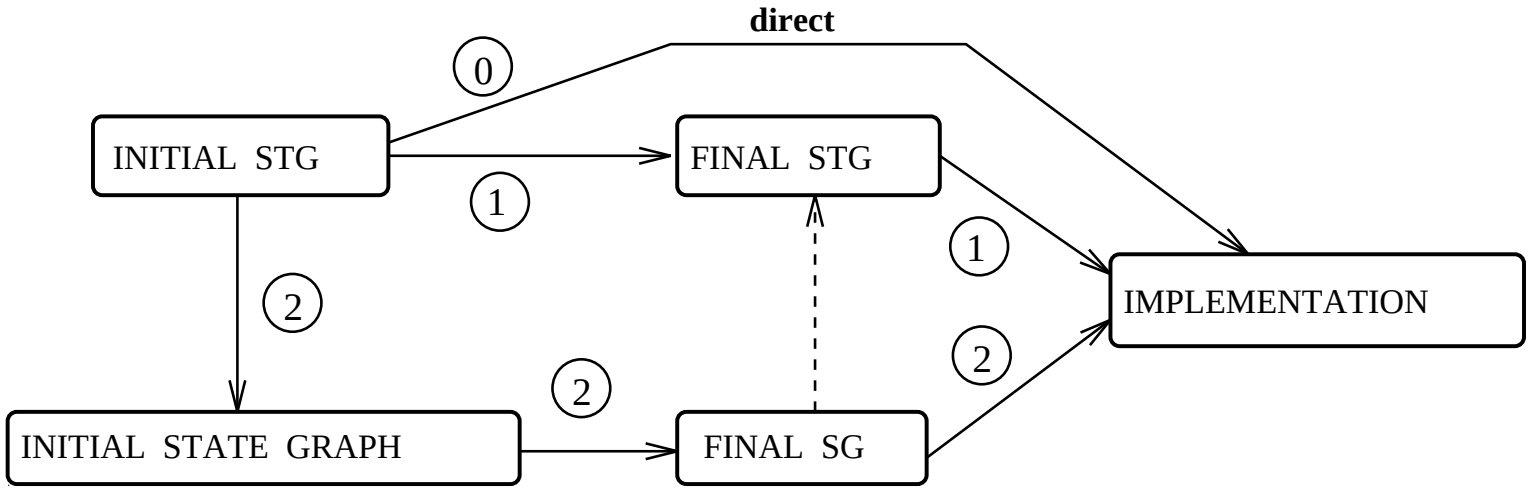
The behavior of the signals supporting boolean guards must be specified in the STG.

Part 2: Synthesis conditions

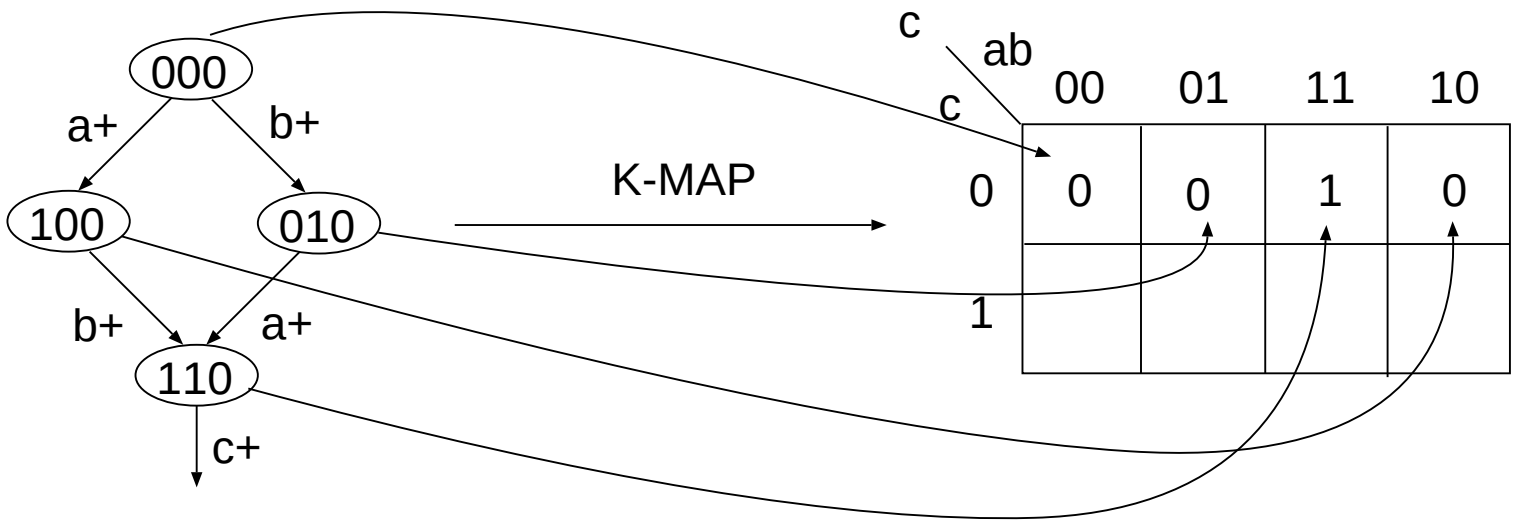
- Derivation of logic equations
- Synthesis conditions for implementability: boundedness, consistency, CSC
- Problems with delays (example: C-element)
- What is speed-independence ? SI = QDI
- Synthesis conditions for SI (persistency, commutativity)

Synthesis by STG

- Route 0 – direct translation method
- Route 1 and 2 – synthesis based on transformations (adding signals, arcs, etc.)
- Which route to take? This tutorial is about route 2.



Next State Functions for Signals



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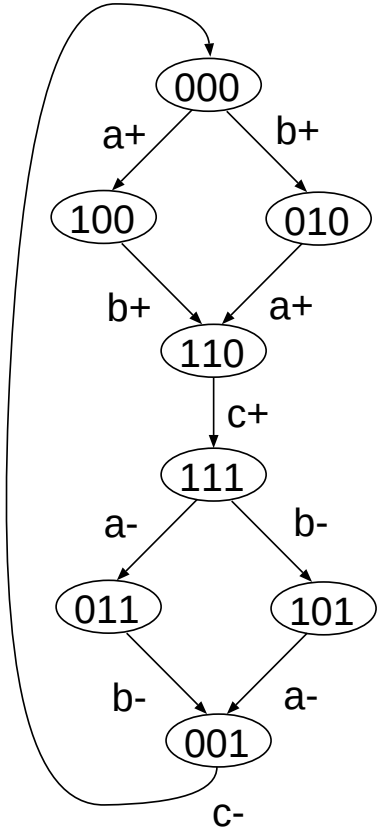
EQUATIONS



STATE GRAPH

K-MAP

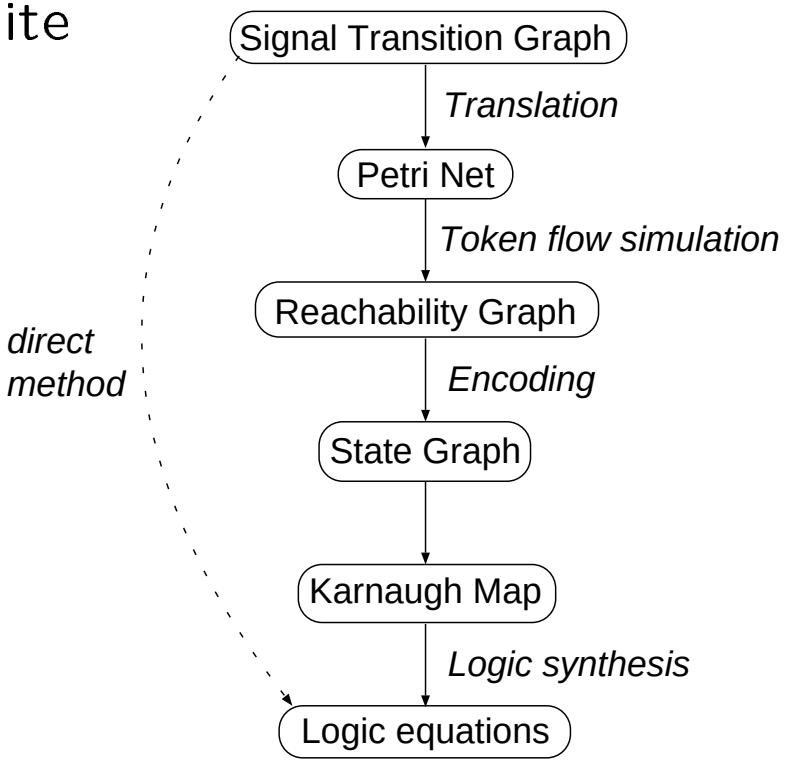
c \ ab	00	01	11	10
0	0	0	1	0
1	0	1	1	1

LOGIC EQUATIONS

c = ab + ac + bc

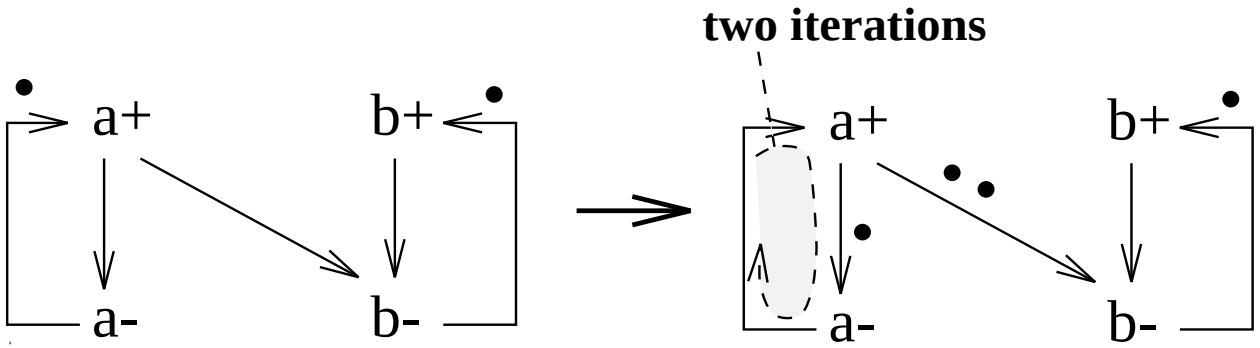
Synthesis conditions

- A reachability graph can be infinite
- Binary encoding of a reachability graph not always possible
- A State graph can have conflicts for logic functions
- Logic can be hazardous (not speed-independent)



Checking synthesis conditions is necessary.

Boundedness



Boundedness $\Longleftrightarrow$ finite reachability graph

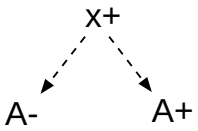
Boundedness of Petri Nets is decidable.

Consistent state assignment

INCONSISTENT

A+ ⇢ A+ Two subsequent up-transitions without a down-transition in between

A- ⇢ A- Two subsequent down-transitions without an up-transition in between



Parallel transitions of the same signal

CONSISTENT

A+ ⇢ A- ⇢ A+

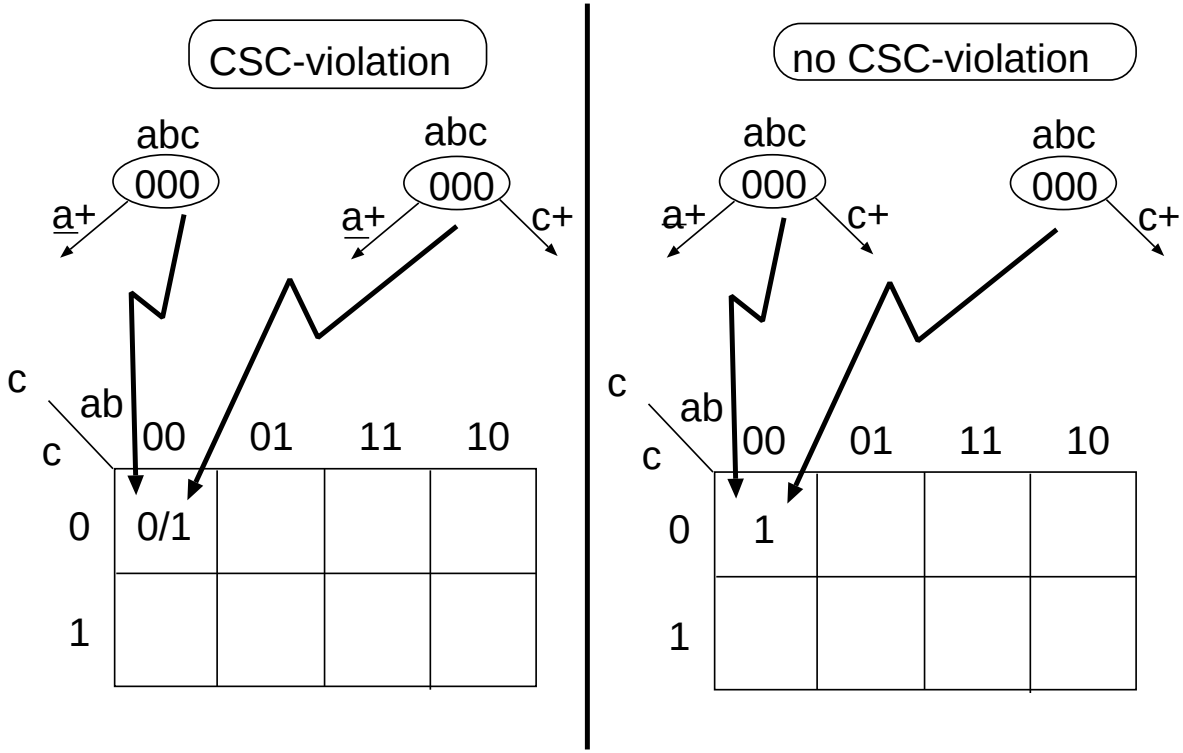
Two up-transitions with a down-transition in between (and vice versa)

$$\cdots \rightarrow a+ \rightarrow b+ \rightarrow a+ \rightarrow \cdots$$

Example: ab: $0*0 \xrightarrow{a+} 10* \xrightarrow{b+} 11 \xrightarrow{a+} ?1$

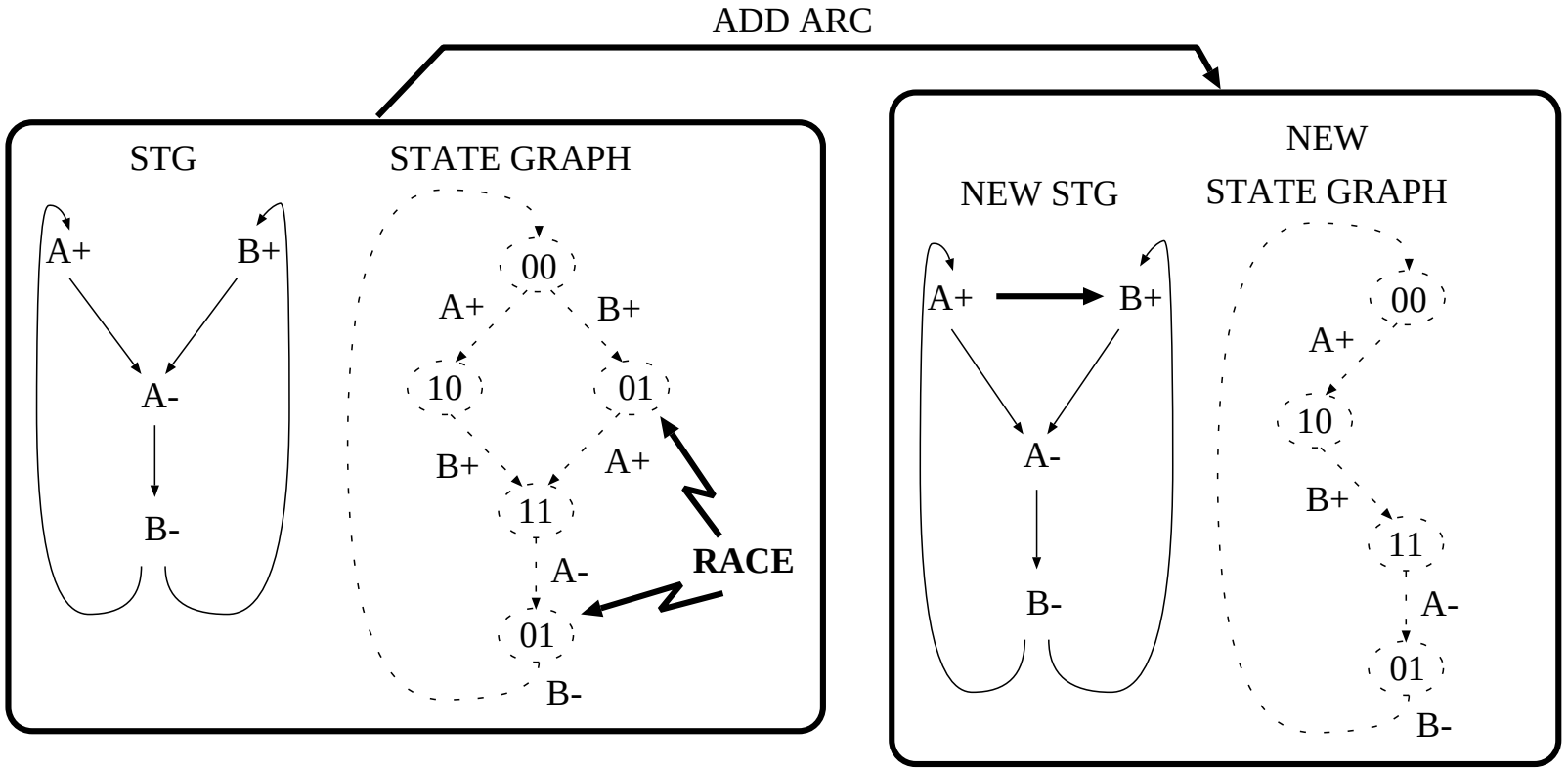
Boundedness + CSA $\Longleftrightarrow$ finite binary state graph

Complete State Coding (CSC)



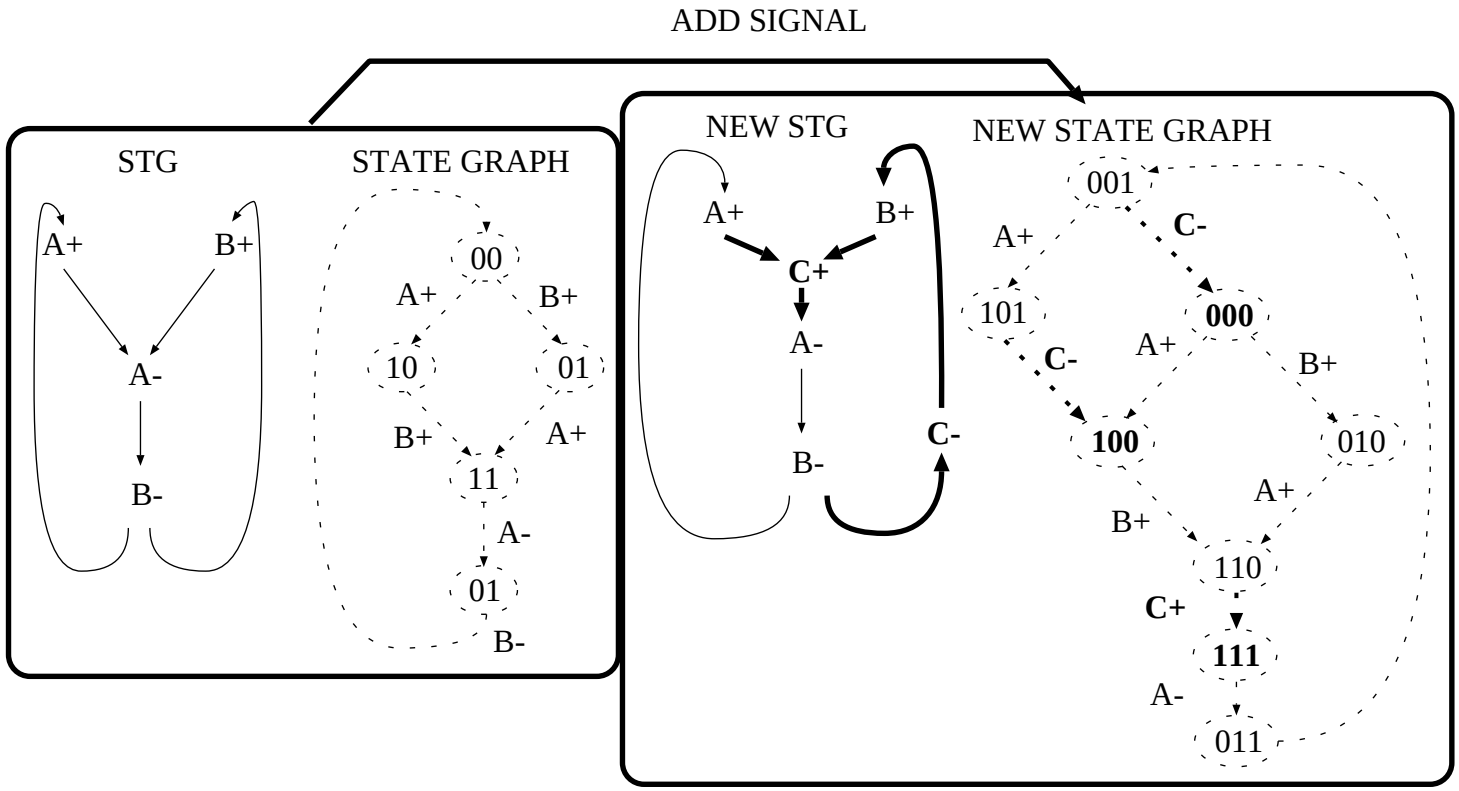
CSC-conflict: two states have the same binary code and different sets of enabled *non-input* signals

Solving CSC by concurrency reduction



Non-equivalent transformation – concurrency is reduced!

Solving CSC by signal insertion

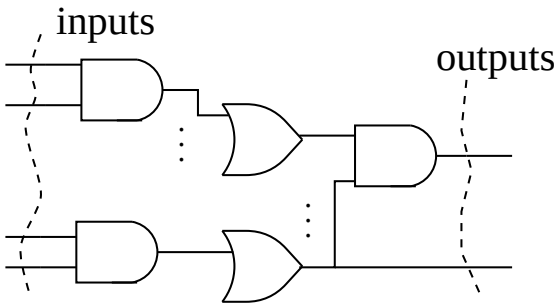


Equivalent transformation – all original traces are preserved

Preserving interface

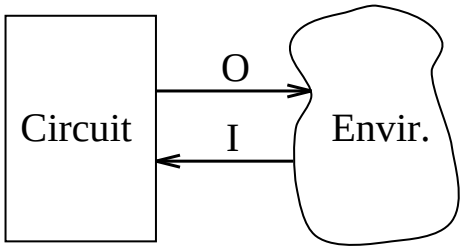
On $I \cup O$ circuit shows

the same language as STG



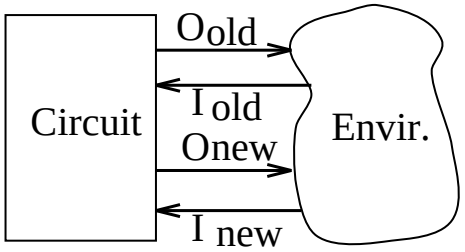
- **I/O-implementability**

  Circuit and STG have exactly the same $I \cup O$ set.
  Interface is preserved



- **Implementability**

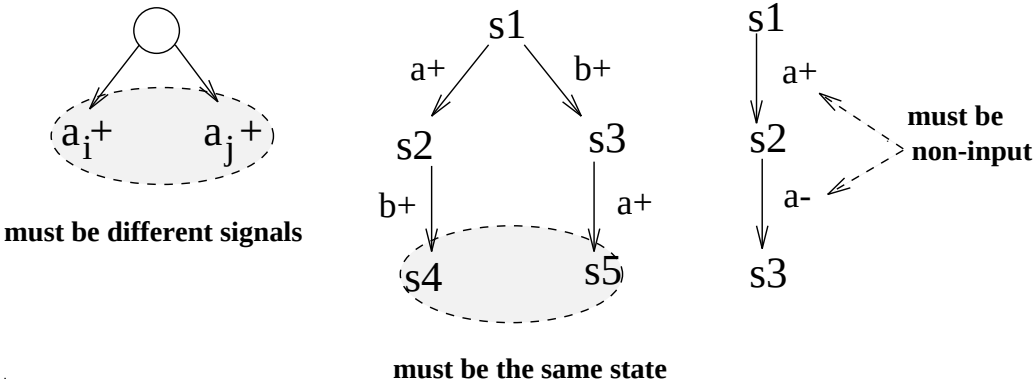
  New inputs and outputs can be added to a circuit.
  Interface is not preserved



I/O implementability

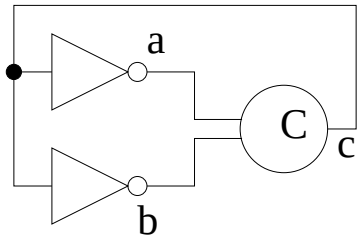
- **Irreducible CSC conflicts:**
  cannot be solved without changing interface.
  In `Petrify` use `-timed` option

- All CSC-conflicts are reducible if STG is:
  - Deterministic
  - Commutative
  - No complementary input sequences



Boundedness + CSA + CSC $\Longleftrightarrow$ Logic circuit

Speed-independence (D. Muller'56)



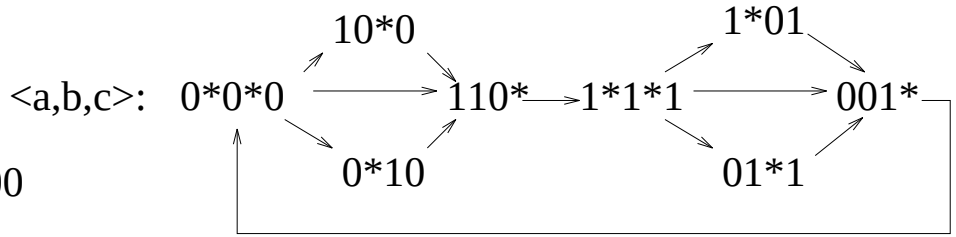
$a = \overline{c}$

$b = \overline{c}$

$c = a\,b + c\,(a+b)$

Initial state: <a,b,c> = 000

State Graph

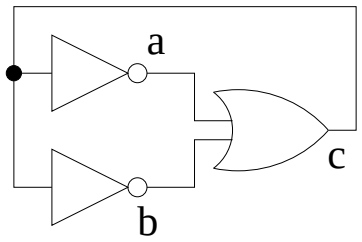


There are no disabled transitions $1^* \rightarrow 1$ and $0^* \rightarrow 0$ in the state graph

Circuit is *speed-independent*

Muller's model assumes the unbounded gate delay model

Checking speed-independence

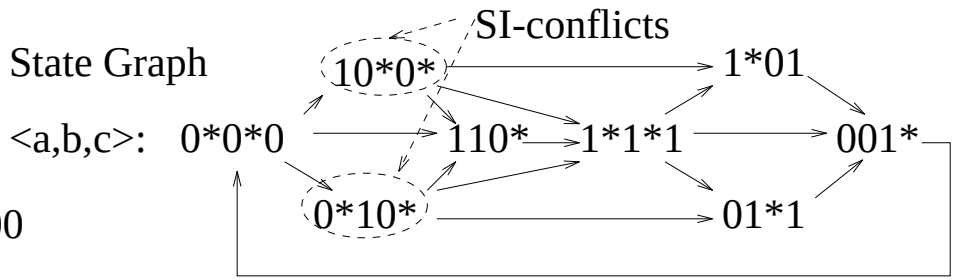


$a = \overline{c}$

$b = \overline{c}$

$c = a + b$

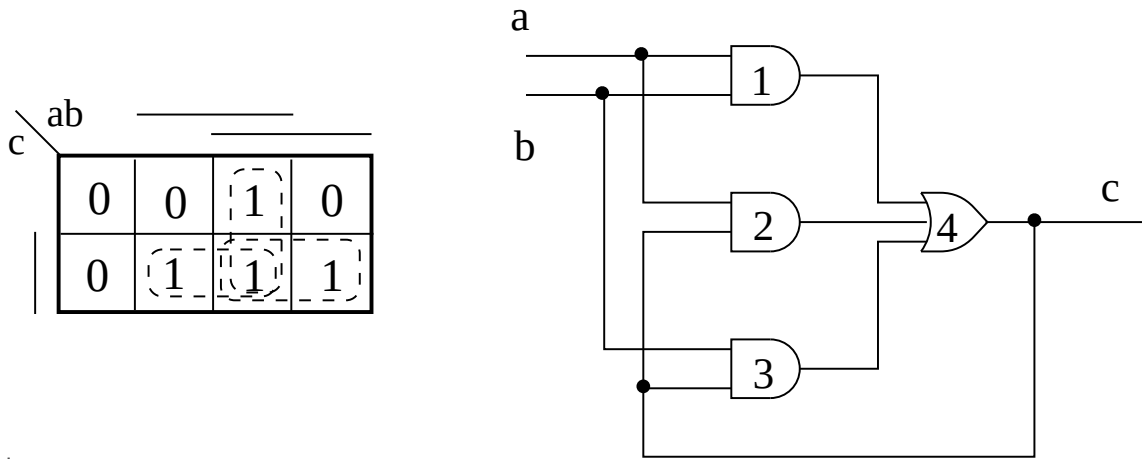
Initial state: <a,b,c> = 000



Circuit is not speed-independent
(or, more precisely, not semi-modular)

Analysis for speed-independence: (D.Muller'56)
(1) traverse states and
(2) check that no SI-conflicts are reachable

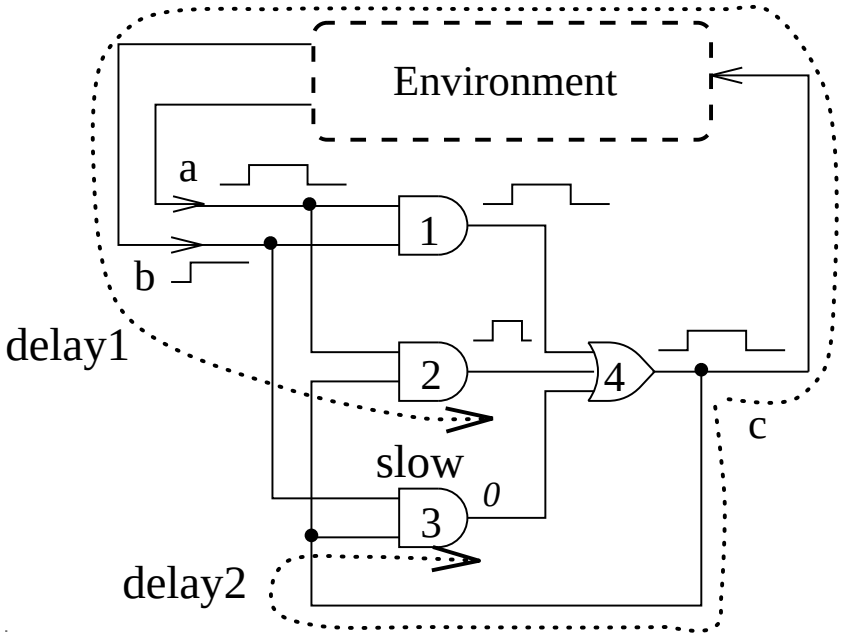
C-element on basic gates



Is this implementation correct?

Answer: It depends on the delay model and the model of the environment

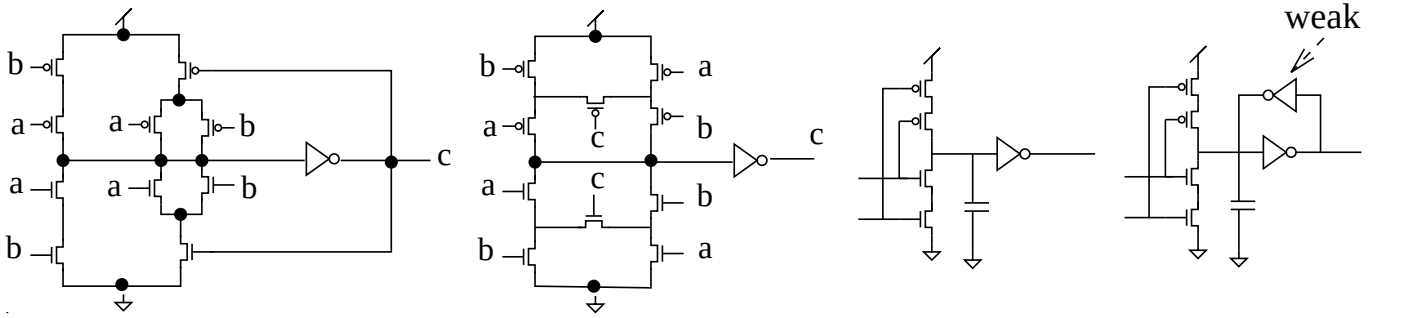
Delay assumptions



- *Delay 1* is a propagation delay from node 1 via environment to node 3
- *Delay 2* is a propagation delay from node 1 via internal feedback to node 3
- *Delay 1* must be greater than *Delay 2*

Delay assumptions influence correctness of asynchronous design

CMOS implementation of a C-element



Static Dynamic Quasi-static

Are these implementations correct?

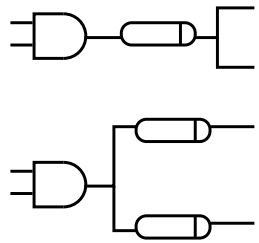
Careful design is required (layout, transistor sizing, charge sharing)

What influences the design methodology

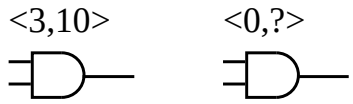
- Environment model
- Delay model
- Signalling model
- Specification language

Delay models

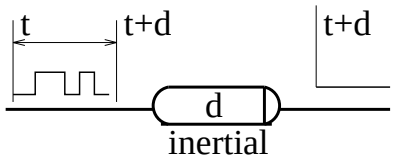
- Place: gates, wires, gates + wires

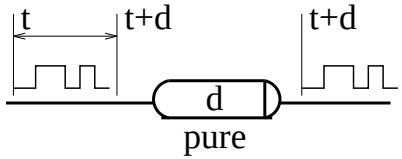


- Timing properties: bounded and unbounded
  Bounded = lower and upper delay bounds are known
  Unbounded = delays are unknown but finite

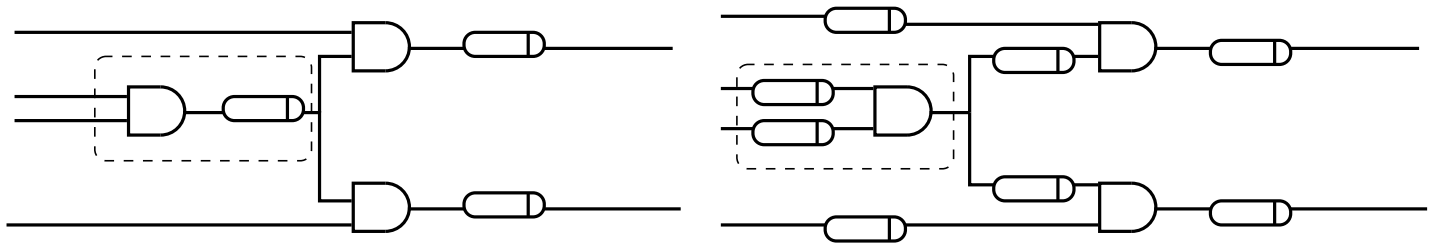


- Memory properties: inertial and pure
  Intermediate models are possible





Gate vs wire delay models



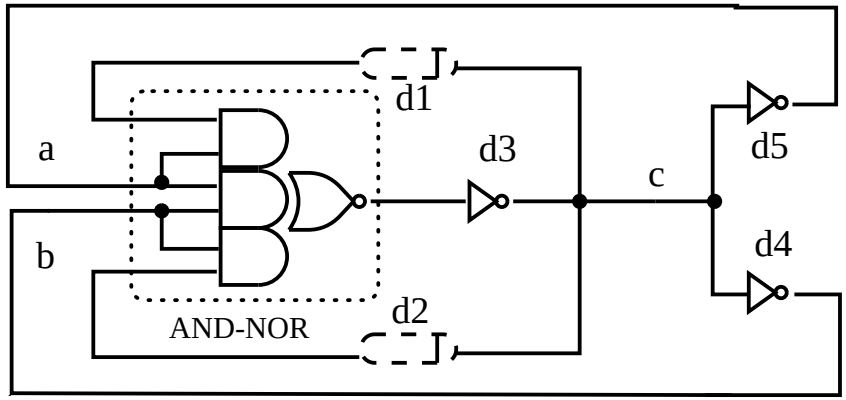
- Gate delay model = delays are in gates, no delays in wires

  More realistic:
  1. gates have arbitrary delays
  2. the skew of wire delays **after fork** is less than gate delay

- Wire delay model = gate+wire delay model:

  Wires (and gates) may have arbitrary delays

Delay models and correctness



- This design is correct for unbounded **gate** delay model
- This design is incorrect for unbounded **wire** delay model
  If $d1 > d3 + d5$ or $d2 > d3 + d4 \Rightarrow$ premature change on c
- For the bounded delay model correctness depends on delay constraints.

Design styles for asynchronous control logic

• **Bounded delays (BD):** realistic for gates and wires.

Technology mapping is easy.
Verification is difficult since time must be considered.

• **Speed-independent (SI):**pessimistic delay model for gates (unbounded) and often acceptable for wires (the skew of delays after fork is less than gate delay).

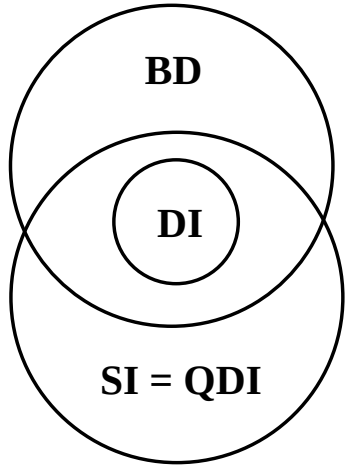
Technology mapping is more difficult.
Verification is easy since time is excluded.

• **Delay-insensitive (DI):** pessimistic delay model for gates and wires (both are unbounded).

DI class (built out of basic gates) is almost empty.

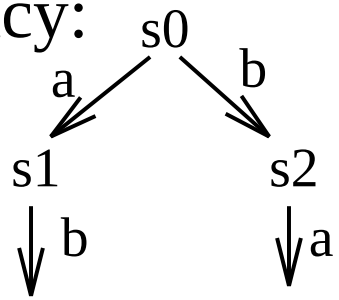
• **Quasi-delay insensitive (QDI)** = delay-insensitive except critical wire forks, called *isochronic forks*.

In practice this is the same as speed-independent.

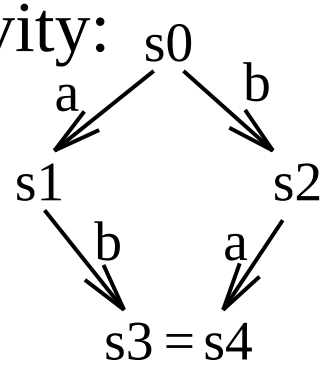


Persistency and commutativity

Persistency:



Commutativity:



In speed-independent design *hazard-free = no disabling*

Signal Persistency: (1) Non-input signals cannot be disabled and
(2) Inputs cannot be disabled by non-inputs

Bound. + CSA + CSC + Persist. + Comm. $\Longleftrightarrow$ SI-circuit

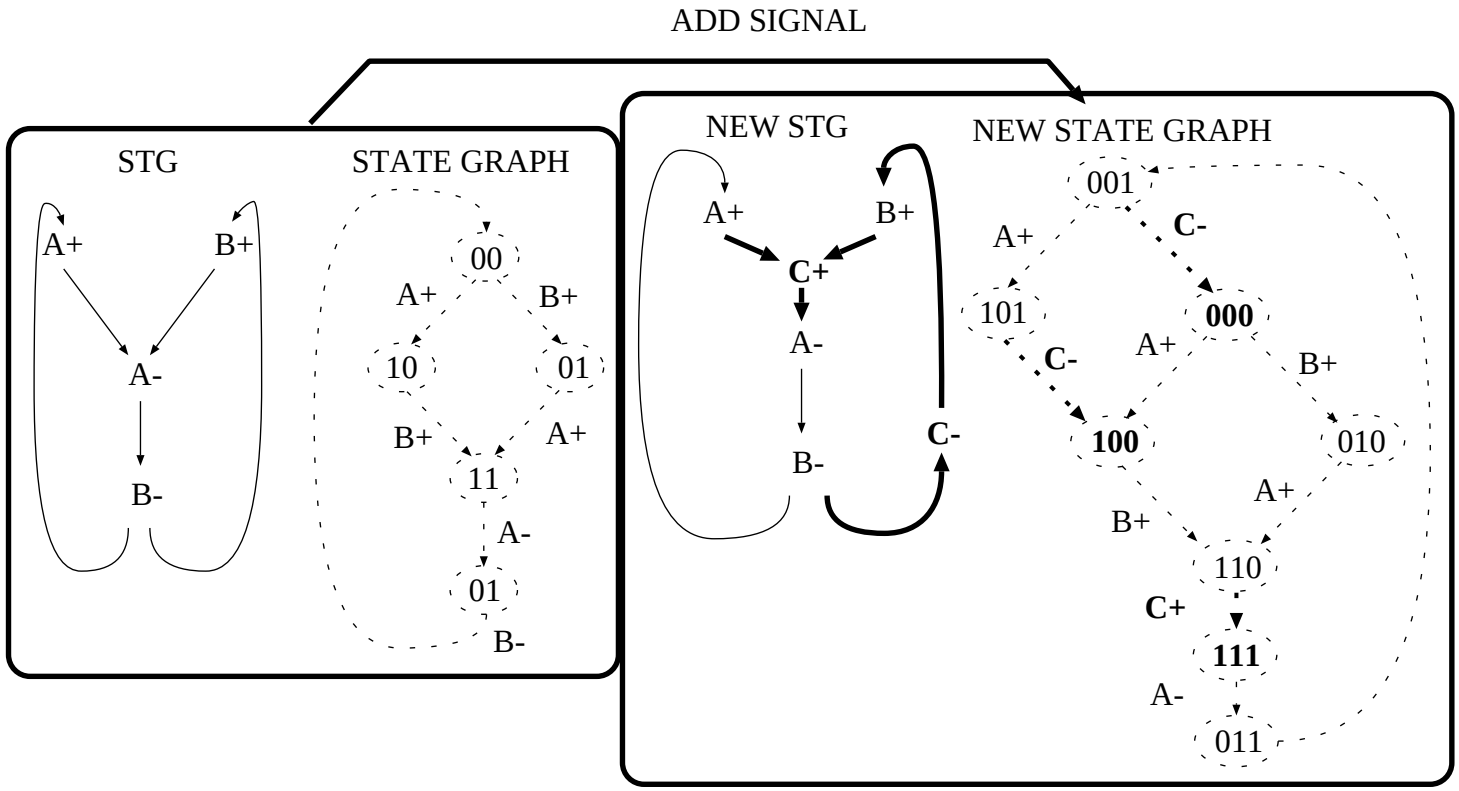
Violations of implementability

Violation of	Meaning	How to correct	Type of implementation
Boundedness	Infinite RG	Change spec	—
Consistency	No binary SG	Change spec	—
CSC (irreducible)	No logic	Add signals	new $I \cup O$
CSC (reducible)	No logic	Add signals	same $I \cup O$
Persistency	Hazards or arbiters	Change spec	not SI or non-determ.

Part 3: Complete state coding

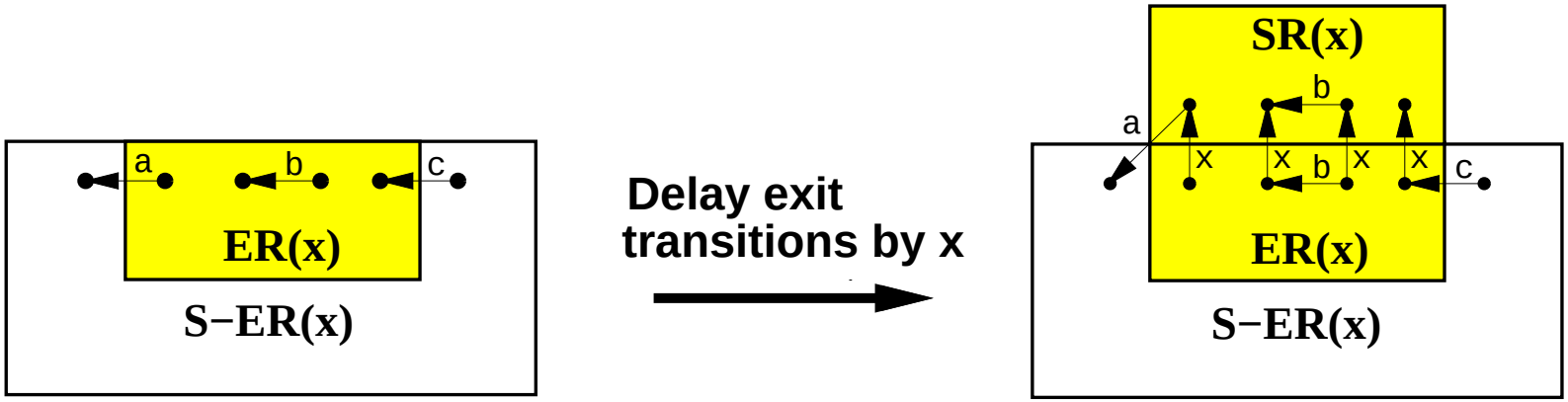
- Signal insertion using regions of states
- SIP-sets (Speed-Independence Preserving sets)
- I-partition and search game
- Estimation of logic
- Examples

Solving CSC by signal insertion



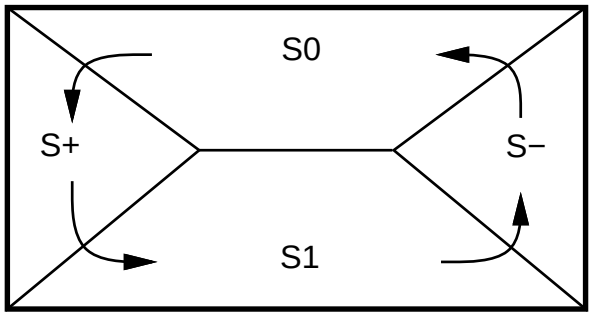
Equivalent transformation – all original traces are preserved

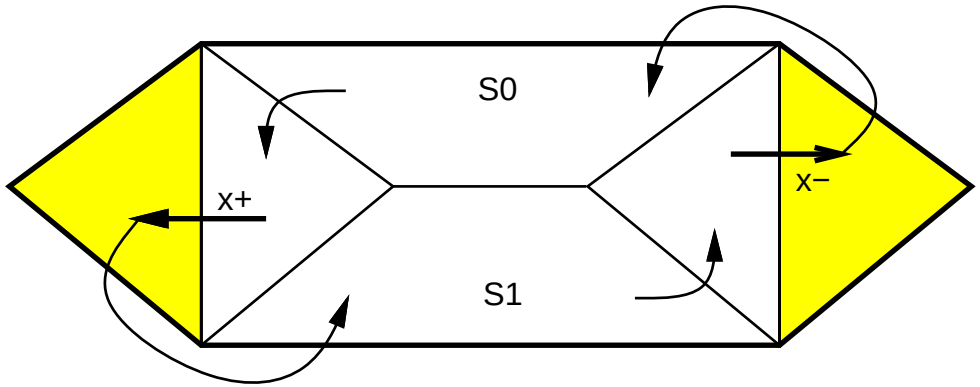
Event insertion



- Choose a set of states = excitation region for a new signal x
- Delay all exit transitions until x fires
- Preserve trace equivalence (or bisimilarity) and speed-independence

Insertion of state signals (I-partition)

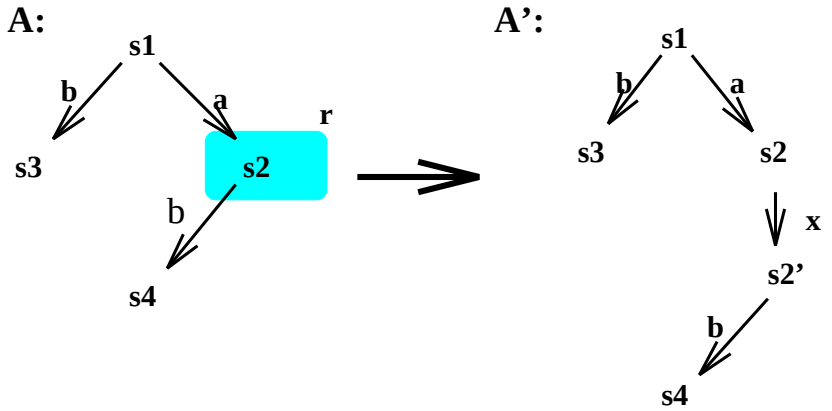




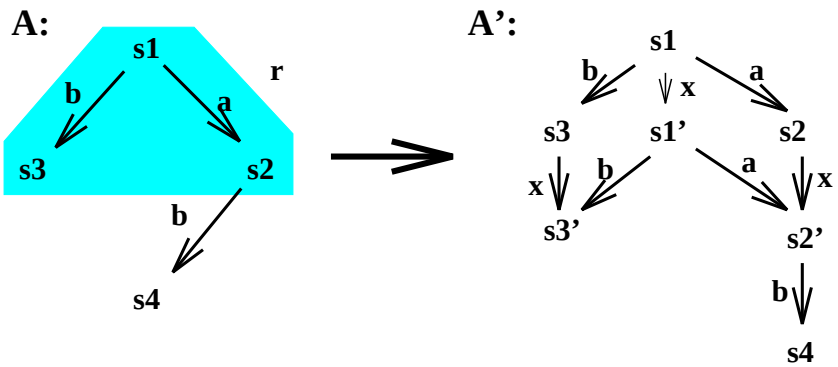
- S^+ and S^- must be SIP (speed independence)
- I-partition must not have illegal arcs (consistency)
  (illegal: $S0 \rightarrow S1$, $S^+ \rightarrow S0$, $S1 \rightarrow S^+$, etc.)
- The event insertion must preserve the behavior of the environment (no exit arcs of *input* events from S^+ and S^-)

SIP violations

Violations of persistency

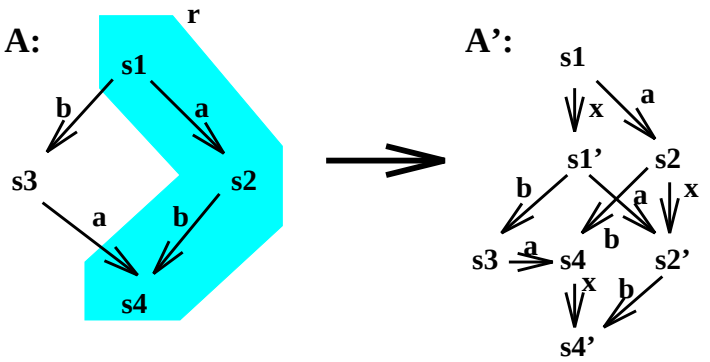


(a)

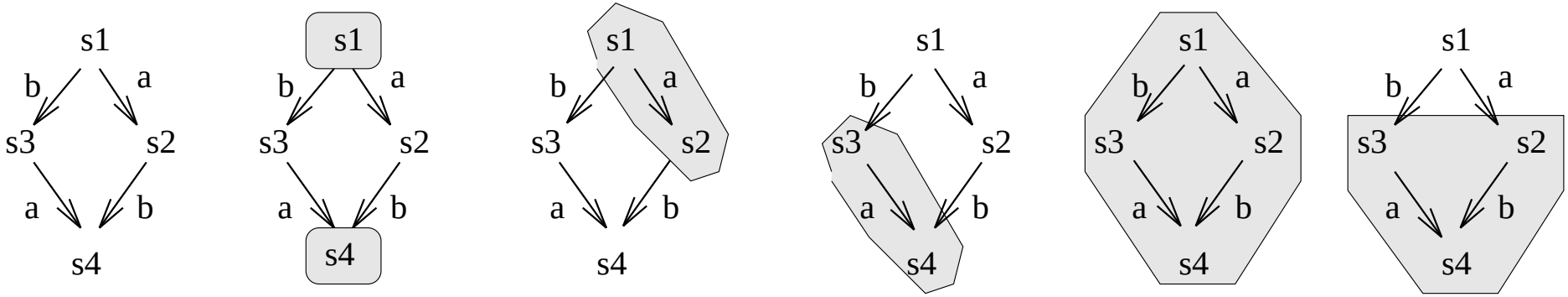


(b)

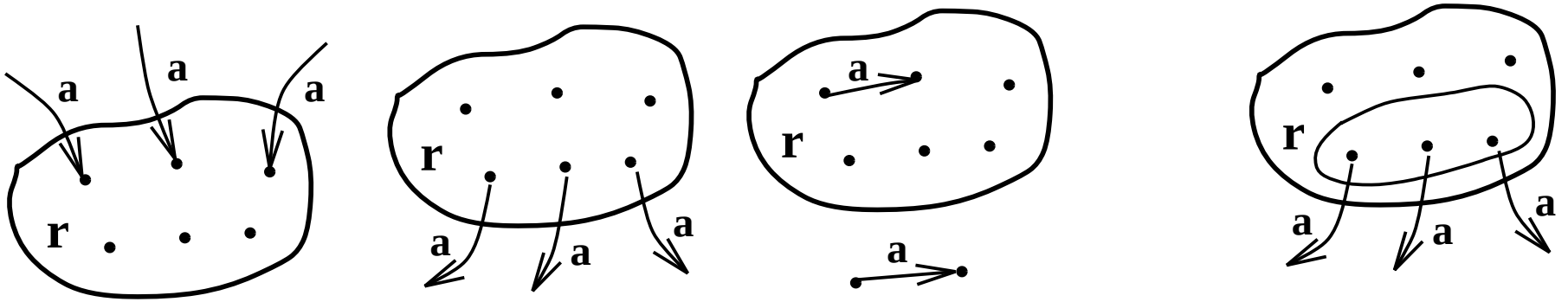
Violations of commutativity



Legal SIP-sets for a state diamond



Regions and excitation regions



enter **exit** **non-cross** **excitation region**

- Region = set of states: each event a can either enter, or exit, or non-cross a region [Ehrenfeucht90, Nielsen92]
- Pre-region = a exits r. Post-region = a enters r.
- Excitation region $ER(a)$: all states that are exited by a; $ER(a)$ is an intersection of pre-regions of a

Any region is a union of minimal regions

Selecting SIP-sets

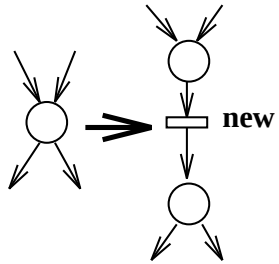
- SIP-sets must be used as excitation regions for new events
- The number of SIP-sets is exponential from the number of states
- Solution: For building SIP-sets use regions and their intersections instead of individual states
- Why this is sound?

USING REGIONS TO SELECT SIP-SETS

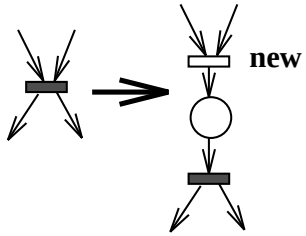
PN-interpretation:

Legal SIP-set:

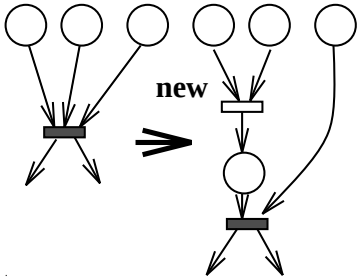
- Region



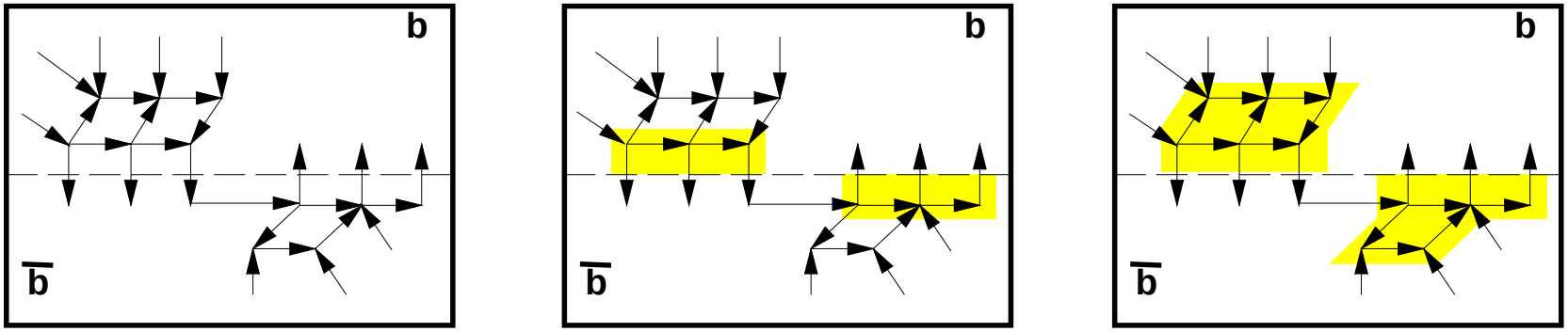
- Persistent excitation region



- Intersection of pre-regions
  (if forward connected)

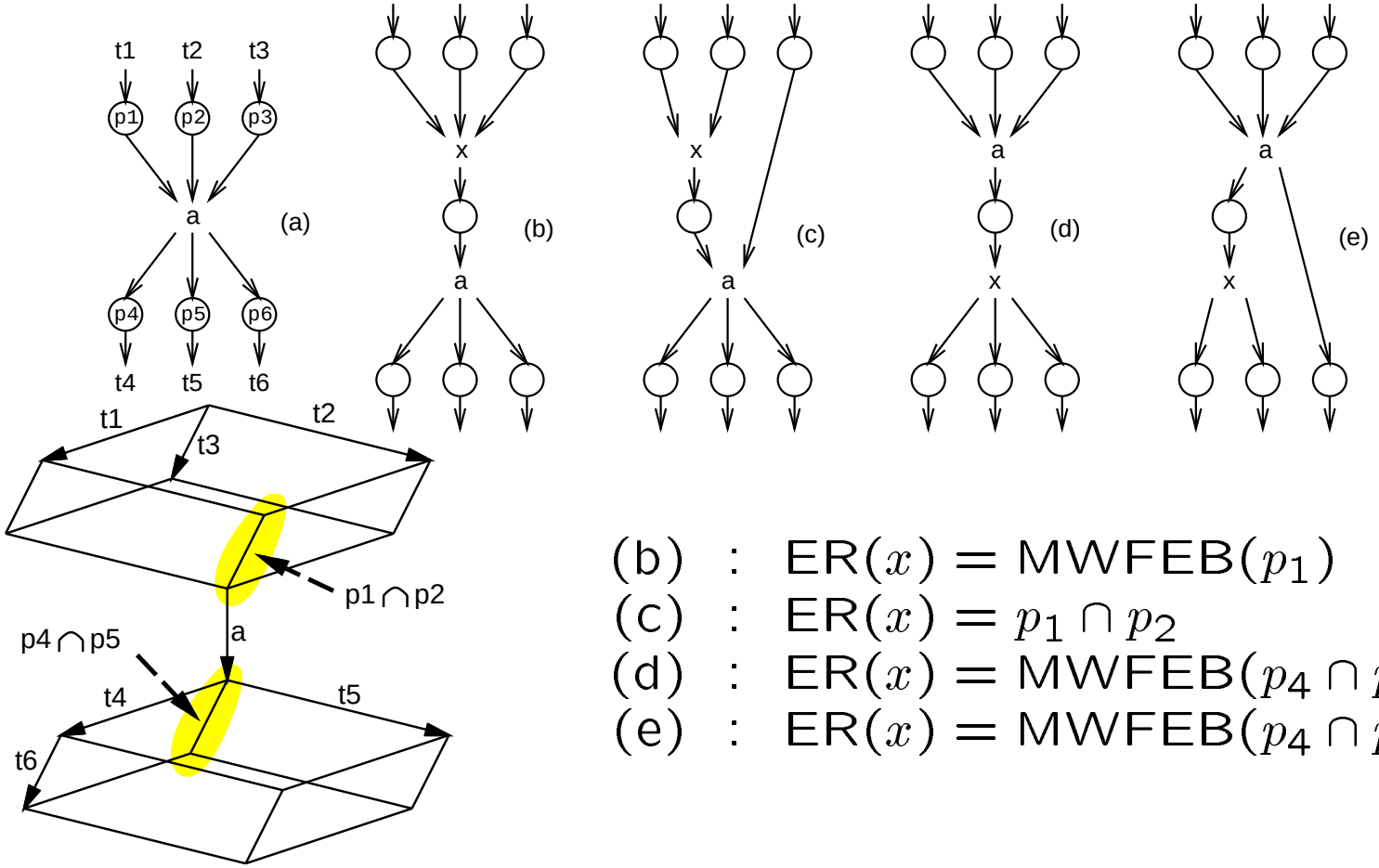


From bi-partition to I-partition



1. Find a bi-partition $\{b, \overline{b}\}$
2. Calculate $EB(b)$ and $EB(\overline{b})$ (similarly for IBs)
3. Extend EBs by backward closure
4. Verify SIP and no exit arcs for input events

Manipulating regions for signal insertion



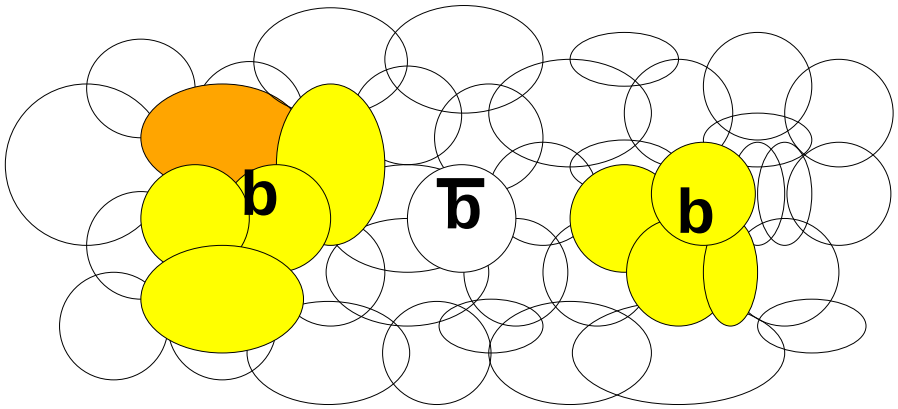
(b) : $ER(x) = MWFEB(p_1)$

(c) : $ER(x) = p_1 \cap p_2$

(d) : $ER(x) = MWFEB(p_4 \cap p_5 \cap p_6)$

(e) : $ER(x) = MWFEB(p_4 \cap p_5)$

The bricks of a block



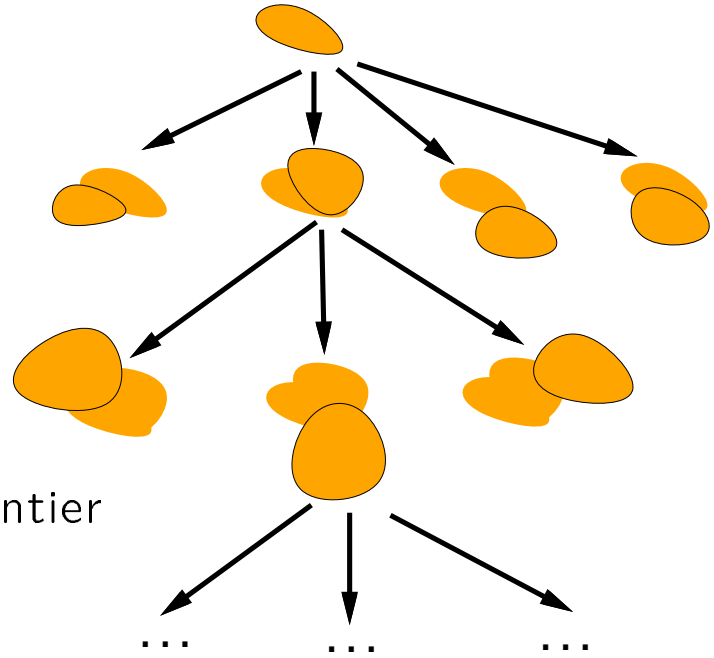
bricks:

- minimal regions
- intersection of pre-regions of the same event
- intersection of post-regions of the same event

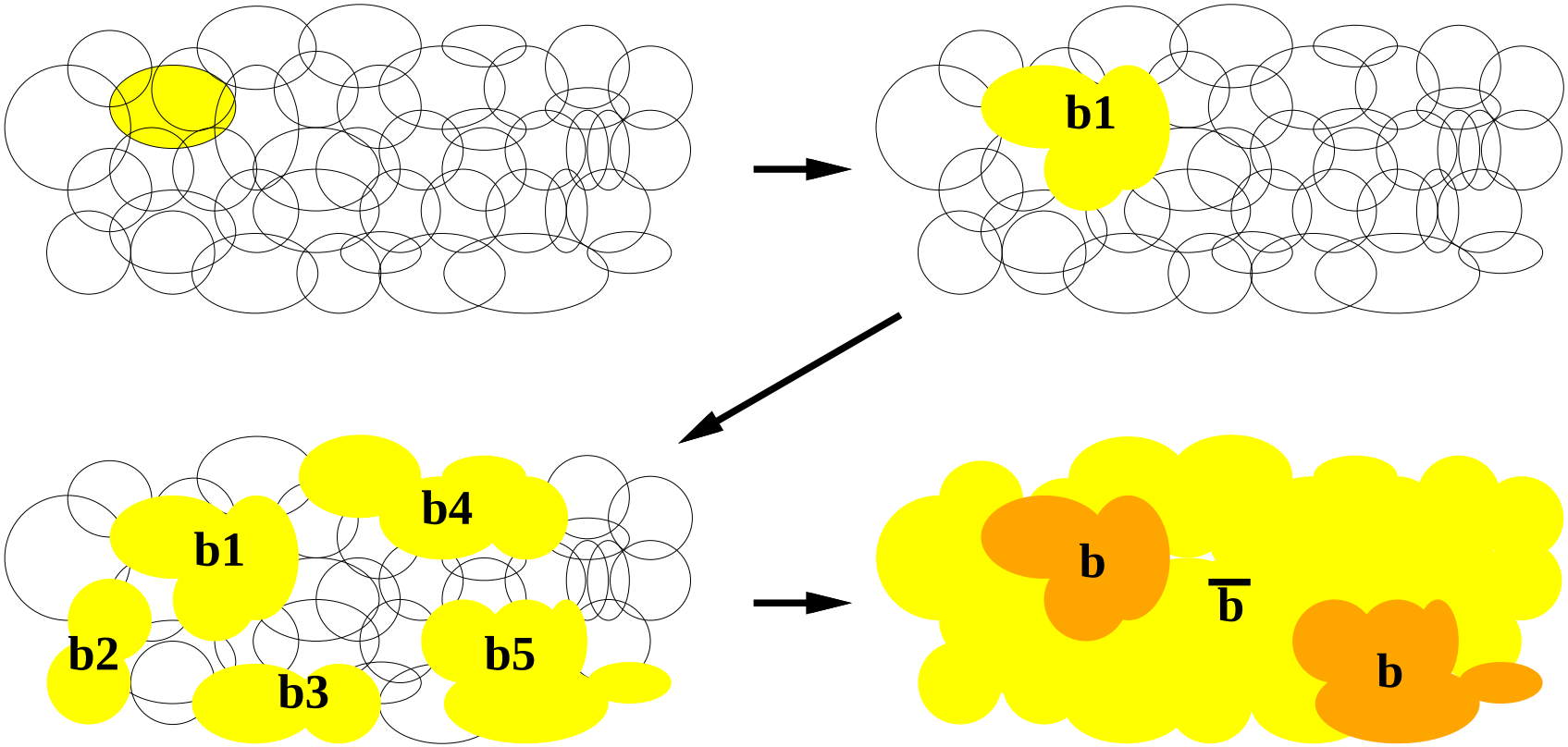
block $=$ $\bigcup$ bricks

Heuristic search: a game-playing strategy

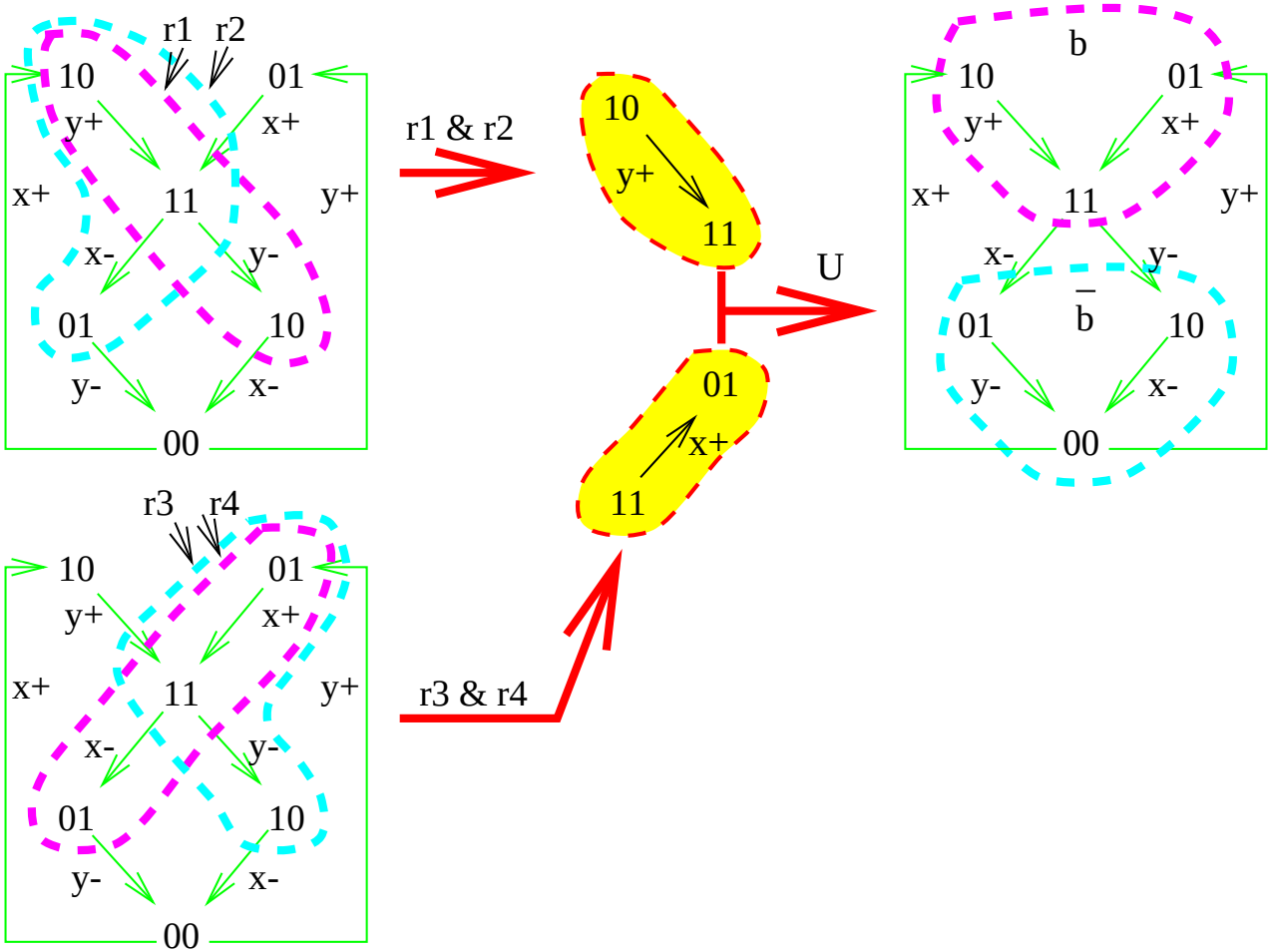
```
bricks = calculate_all_bricks ()
frontier = good_blocks = {the best FW bricks}
repeat /* heuristic search */
    new_frontier = ∅
    for each bl ∈ frontier do
        for each br ∈ bricks adjacent to bl do
            new_bl = bl ∪ br
            if cost(new_bl) < cost(bl) then
                good_blocks = good_blocks ∪ {new_bl}
                new_frontier = new_frontier ∪ {new_bl}
    frontier = select the best FW blocks from new_frontier
until new_frontier = ∅
return the best block in good_blocks
```



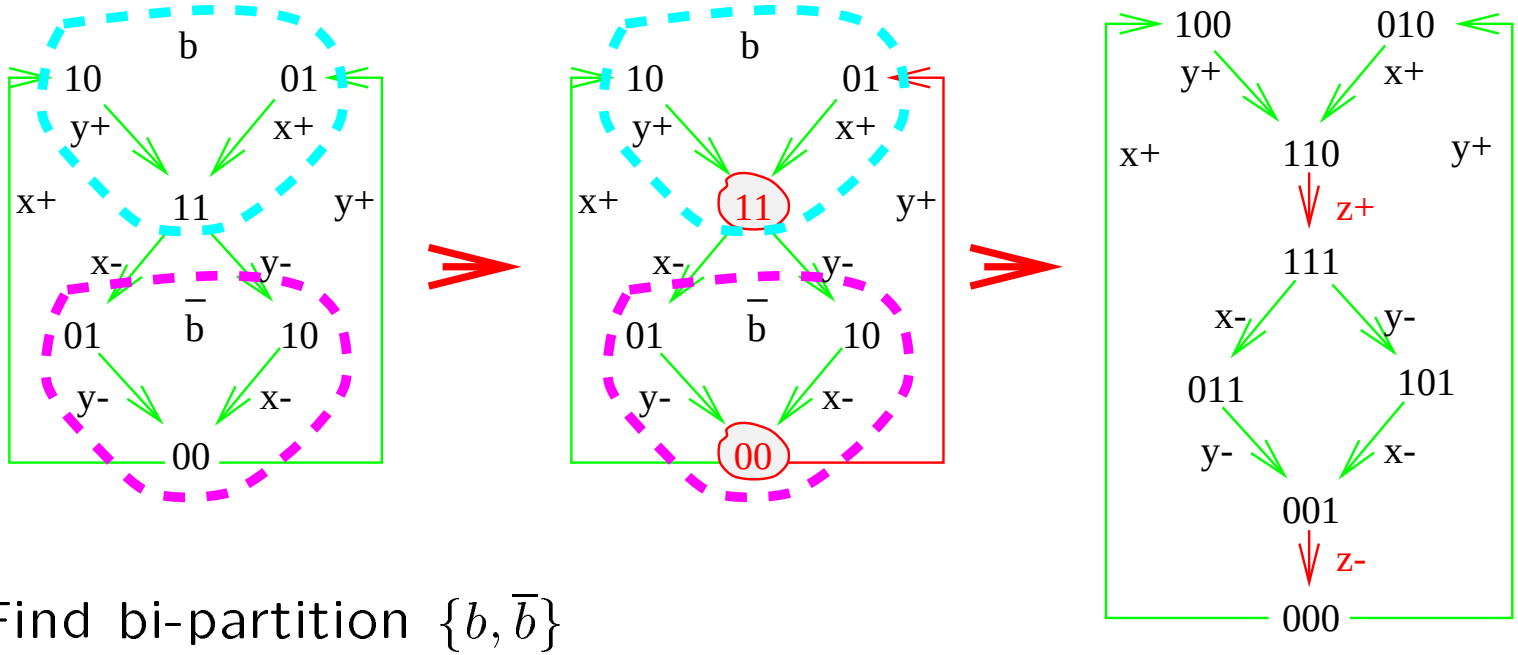
Building blocks and coloring



Example: bipartition for CSC using regions



Example: I-partition for CSC using regions



1. Find bi-partition $\{b, \overline{b}\}$

2. Find by expansion $EB(b)$ and $EB(\overline{b})$ which are well-formed and SIP

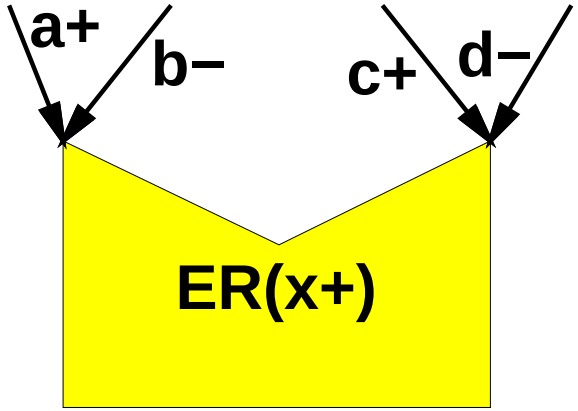
Cost function

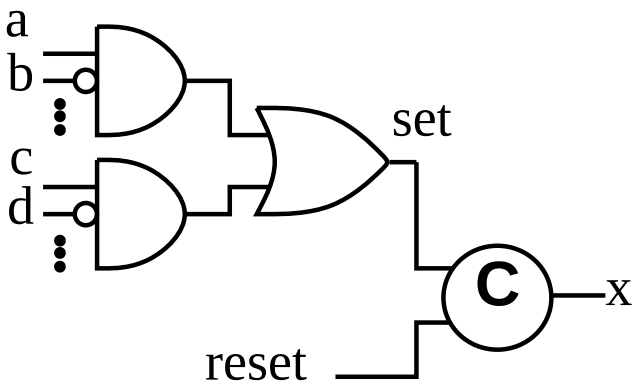
Comparison of two I-partitions:

- Correctness (SIP, well-formedness, behavior of the environment)
- Number of CSC conflicts solved
- Estimation of logic

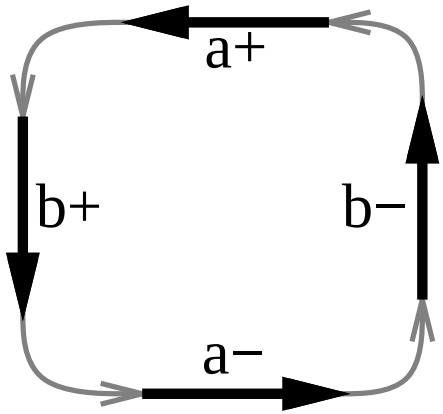
$\Rightarrow$ Trade-off between CSC conflicts and estimated logic

Estimation of logic





trigger signals

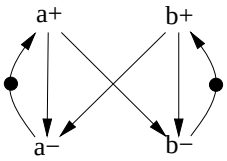


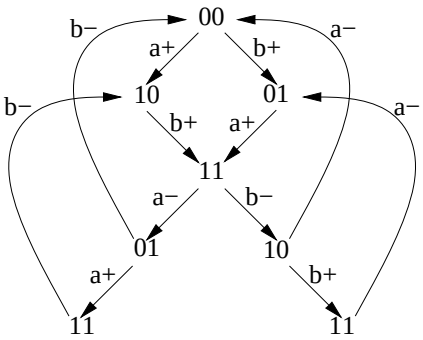
ER($a+$) $\Rightarrow$ $\overline{b}$

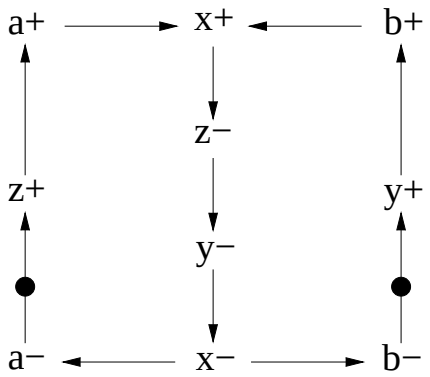
ER($a-$) $\Rightarrow$ b

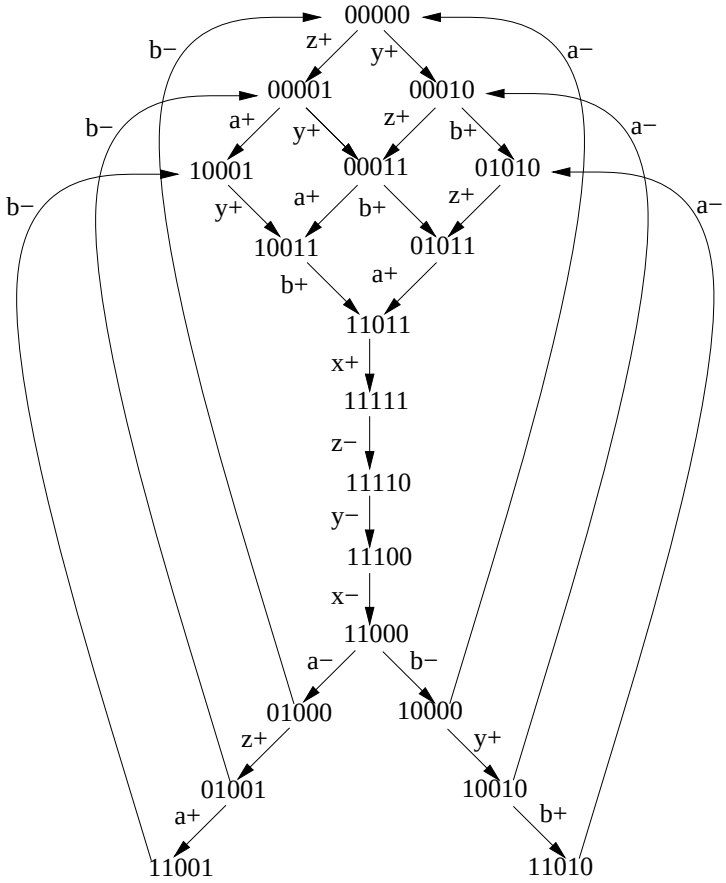
locked signals

Solving examples with CSC-conflicts

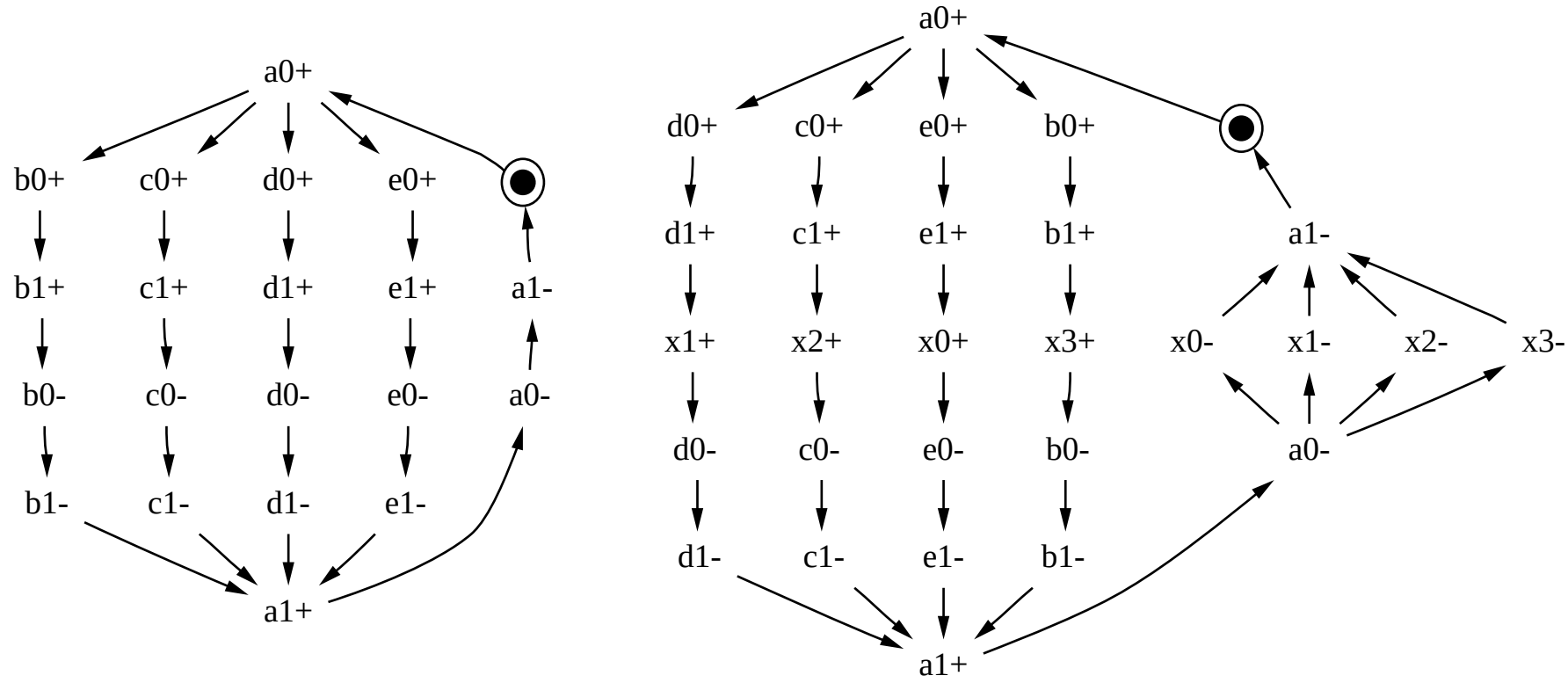






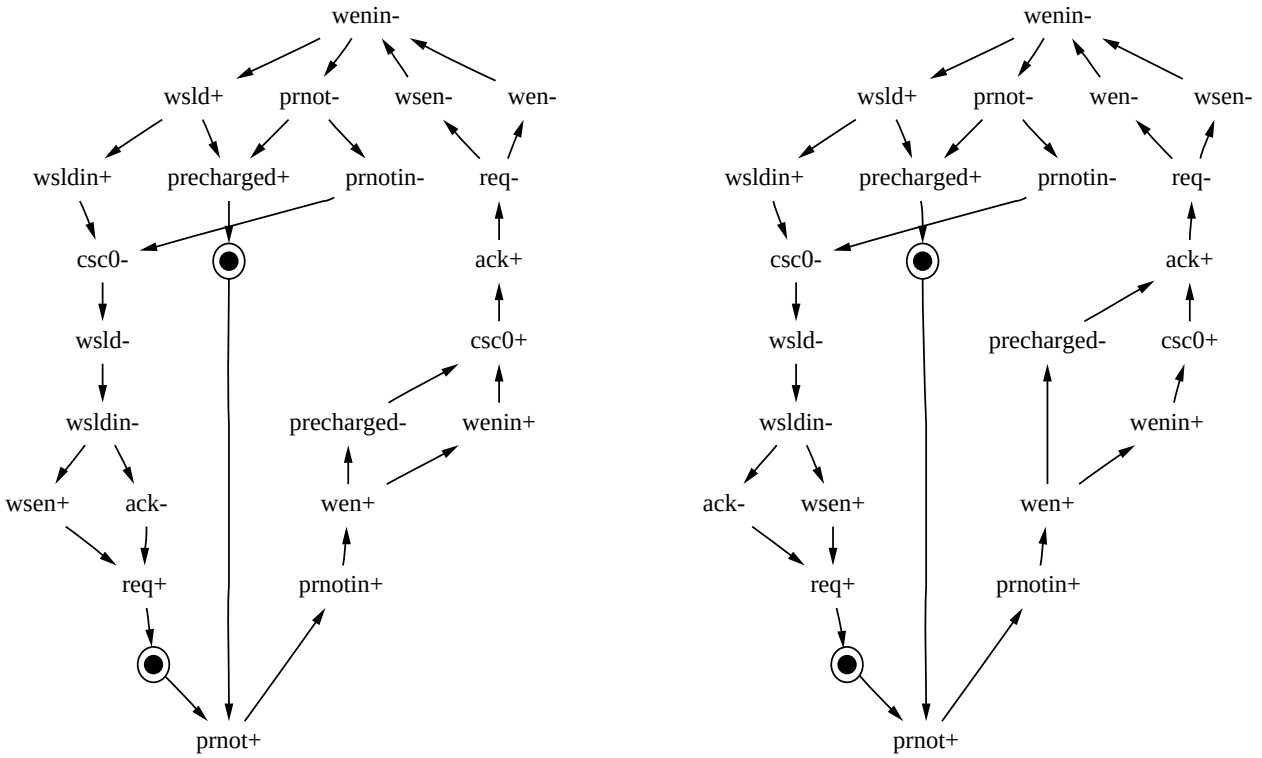


Solving examples with large state space



par16: 83 places, 68 trans., 34 (50) signals
1.5×10^{11} (2.8×10^{12}) states $\Rightarrow < 4h$. CPU time

Manipulating concurrency of inserted signals



ram-read-sbuf: (a) sequential solution (area = 406)
(b) after increasing concurrency (area = 456)

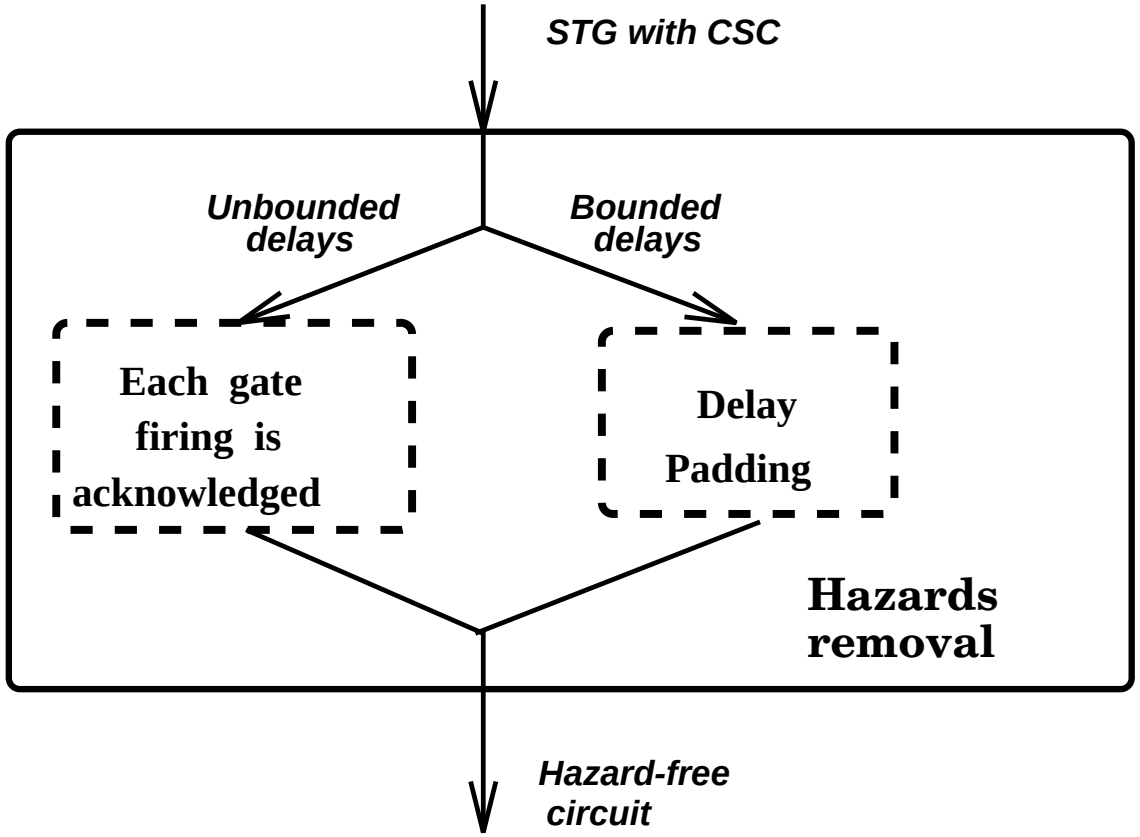
Features of region-based method

- Computationally efficient (search is guided by regions)
- Allows symbolic manipulation with SG (BDD-based)
- Complete (All CSC conflicts are solvable for safe STG)
- Represents the result in STG ($STG \rightarrow SG \rightarrow STG$)
- Implemented in **petrify** tool

Part 4: Logic decomposition

- Problem definition
- Monotonous cover
- Decomposition based on algebraic devision
- Decomposition based on Boolean relations
- Synthesis for bounded gate and wire delays

Hazard-free synthesis



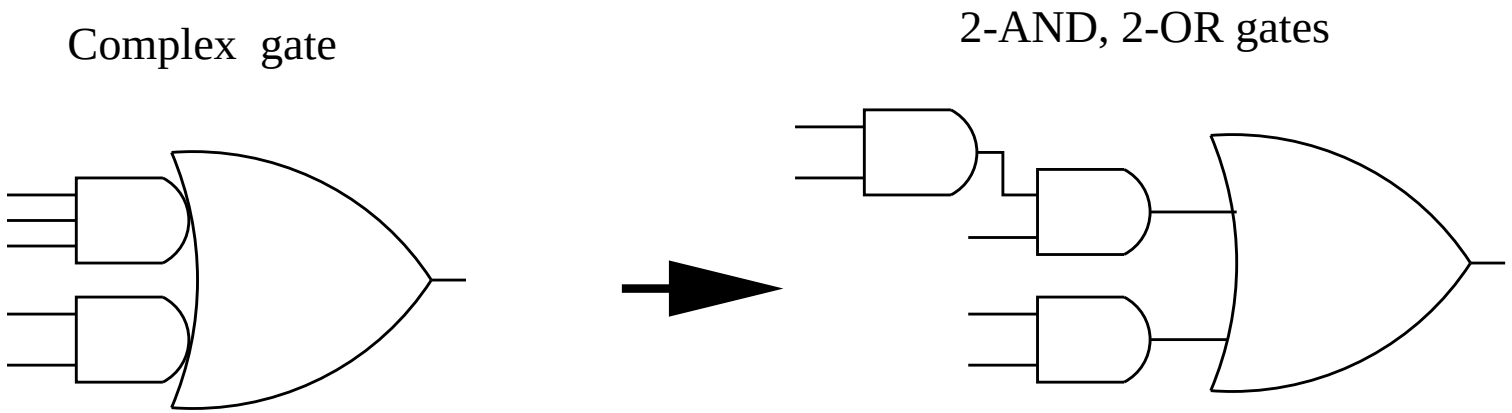
History: synthesis with unbounded gate delays

- Muller (59): formal analysis method, but only design hints
- Martin, Burns (86, ...): syntax-directed translation, then QDI-preserving optimization
- Varshavsky et al. (90): syntax-directed translation from STG
- Beerel (92) and Kondratyev et al. (93, 95): necessary and sufficient conditions for monotonous switching, STG- and SG-level synthesis techniques based on signal insertion.

History: logic decomposition for SI design

- Kishinevsky, Varshavsky (82) – basis of 2-input gates
  (area overhead – only theoretical interest)
- Beerel et al. (ICCAD' 92) – general acknowledgement
  (based on heuristics, no guarantee to find a solution even when it exists)
- Siegel et al. (ICCAD '94) – only local decomposition
  (simple cases, no completeness)
- Myers et al. (London '95) – decomposition + resynthesis
  (local acknowledgement, no effective solution)
- Burns (Async '96) – local two-level decomposition
  (exact and efficient solution, single ack. restriction)
- Cortadella et al. (Async'97, ICCAD'97) – multilevel
  decomposition with multiple acknowledgement based on factoring and
  Boolean relations

Problem formulation for logic decomposition

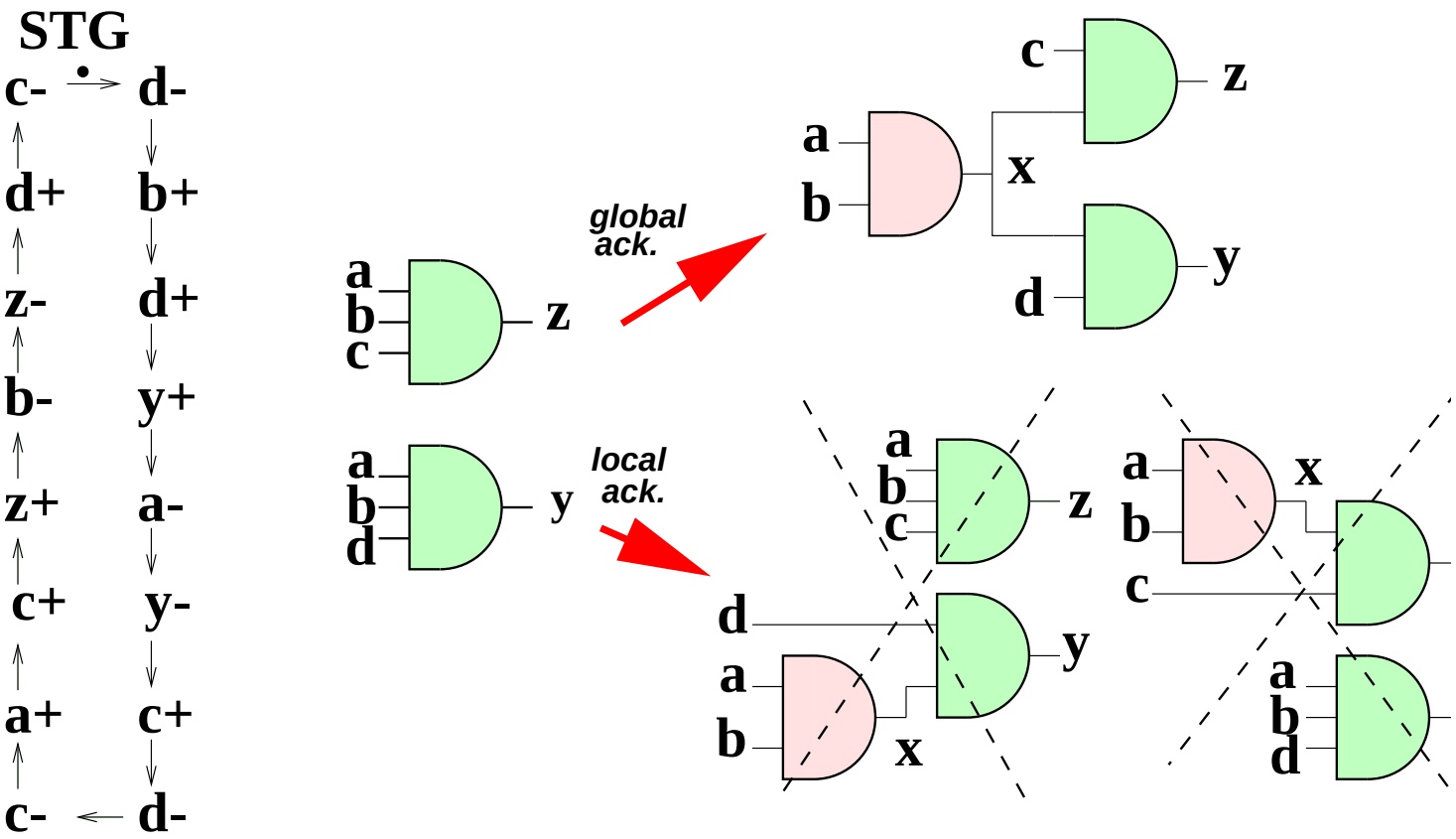


Problem: hazards may appear =

some transitions may not be acknowledged $\Rightarrow$

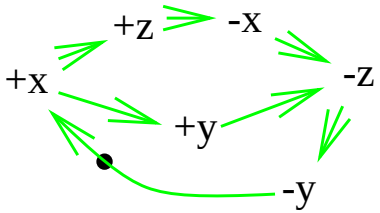
the result is not speed-independent

Sometimes classical decomposition works ...



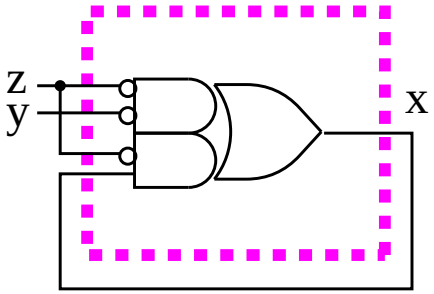
Driving and supporting gates

STG

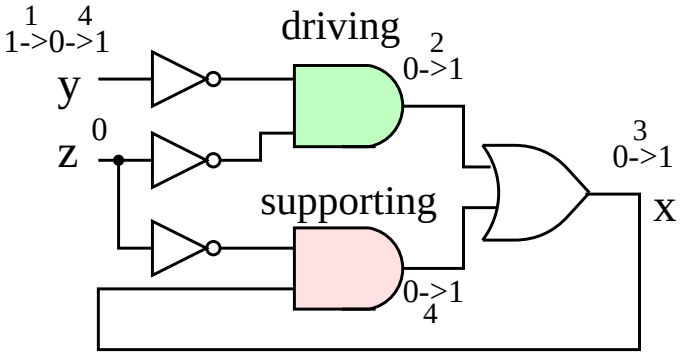


$x = \overline{z}\overline{y} + \overline{z}x$

Complex gate



Simple gate implementation

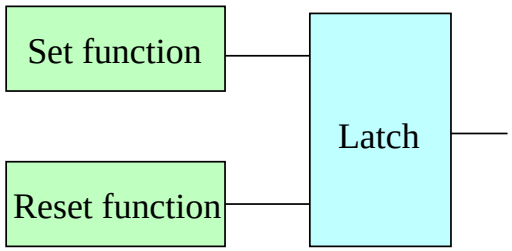


- All internal signal transitions must propagate to the output (acknowledgement principle is applied to individual gates)

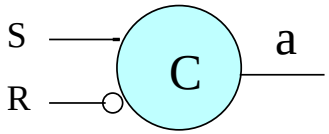
- Driving gates: "good", supporting gates: "bad"

Implementation structures

Signal implementation



C-latch



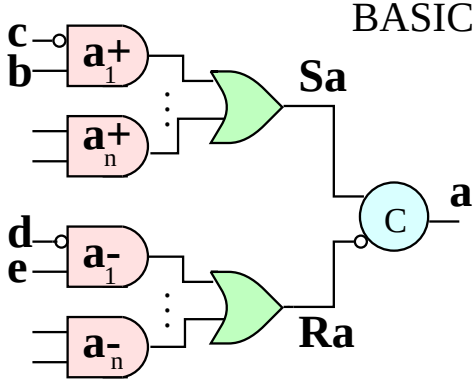
S=1, R=0 ⟹ a+

S=0, R=1 ⟹ a-

Each signal transition corresponds to an AND gate

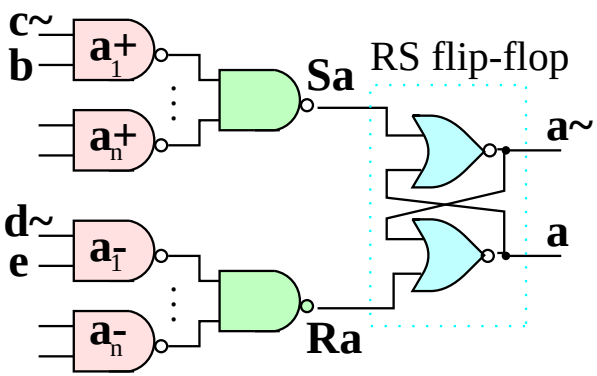
- $a+$ sets the latch
- $a-$ resets the latch

BASIC ARCHITECTURES



with input inverters

RS flip-flop

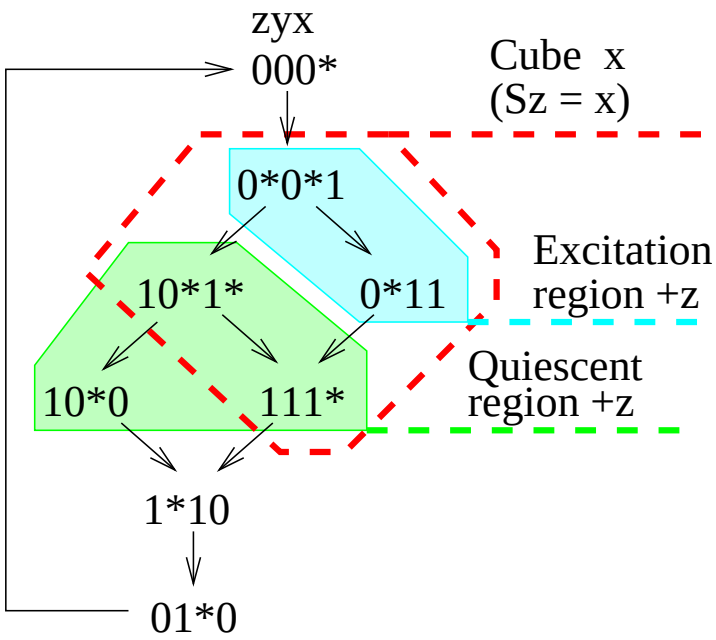


without input inverters

Regions of a state graph

Synthesis idea:

transition ⇒ cover cube in R or S function ⇒ driving gate

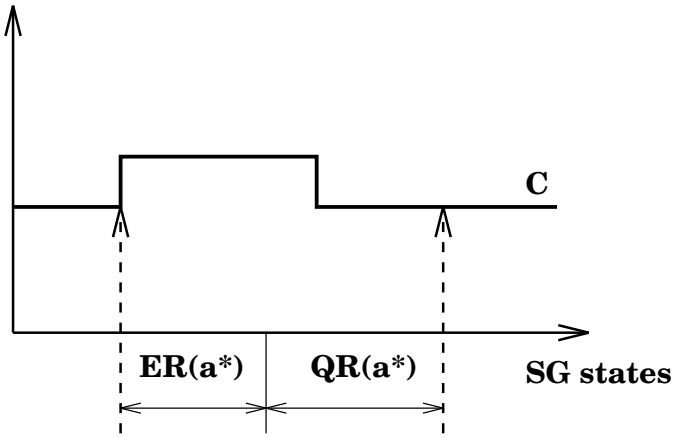


- Excitation region (ER) must be covered by **one** cube
- Quiescent region (QR) is a *don't care set* for a cover cube

Monotonous cover conditions

Cover cube C is a **monotonous cover** for $ER(a*)$ iff:

1. C covers all states $ER(a*)$
2. C covers no states outside $ER(a*) \cup QR(a*)$
3. C changes only once inside $QR(a*)$

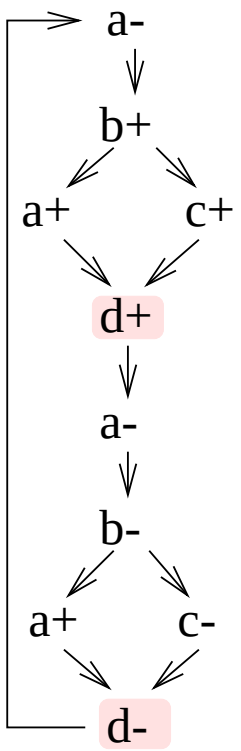


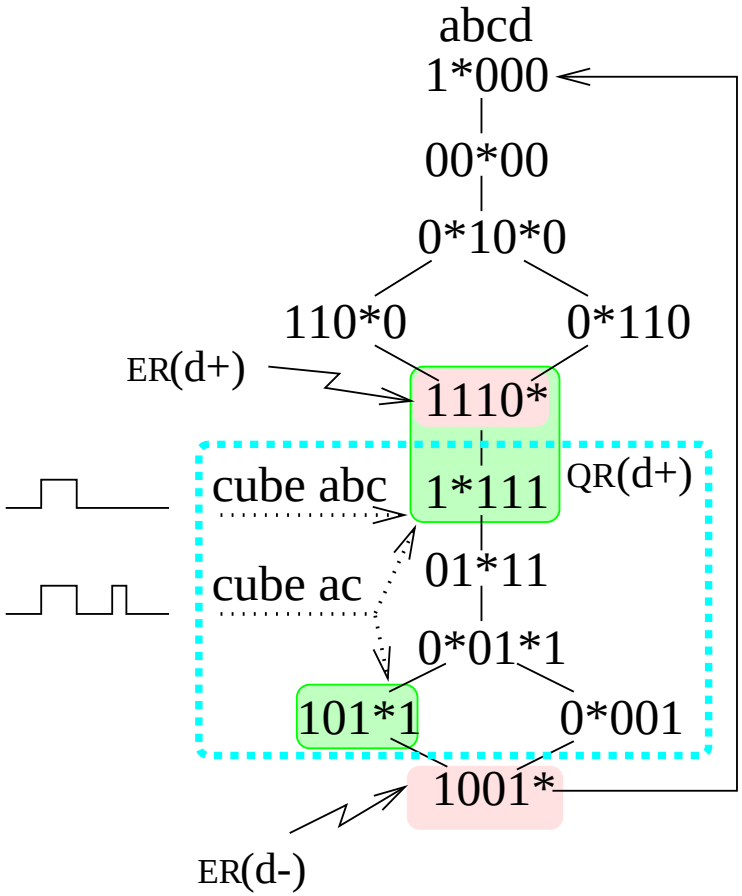
- Monotonous cover $\Rightarrow$ SI-implementation on simple gates
- Restricted (but useful and realistic) architecture

Monotonous cover example

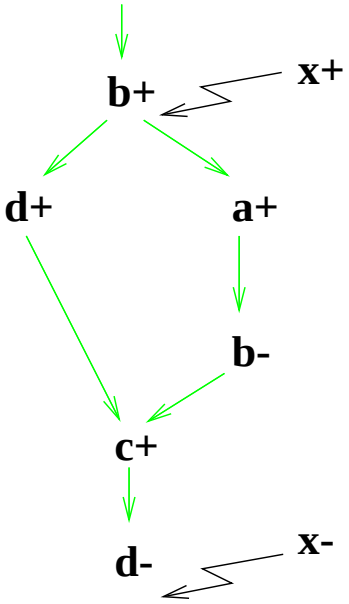
If a cover cube is not MC ⇒
reduce it by adding literal

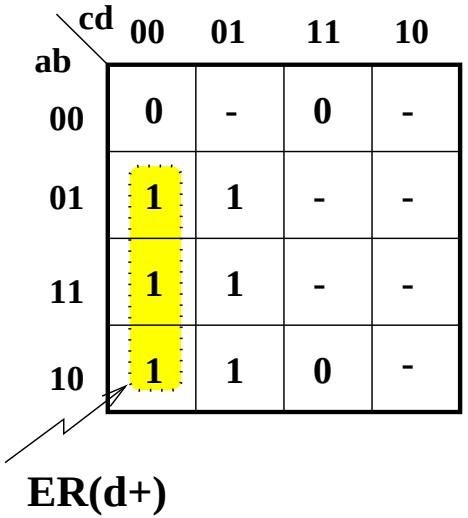
If it does not help ⇒
add signals





Reduction to monotonous cover form





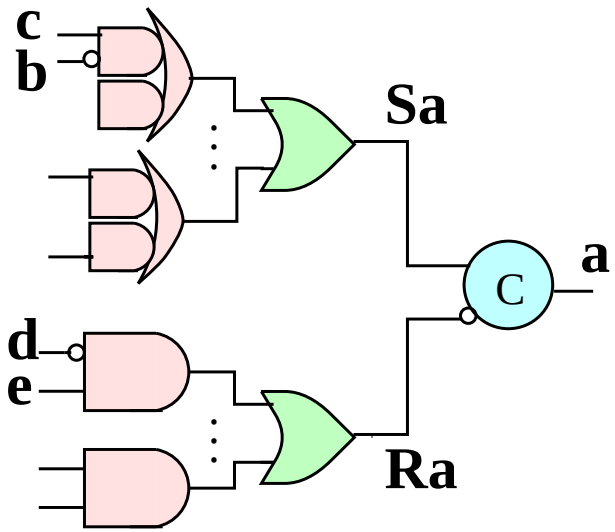
- $ER(d+)$ cannot be covered by one cube
  (minimal cover for $ER(d+)$ is $b+$ $a\overline{c}$)
- After inserting signal x:
  minimal cover for $ER(d+)$
  is $x\overline{c}$
- Any MC-conflicts can be removed by adding signals

Trace equivalence is preserved

Extended MC conditions

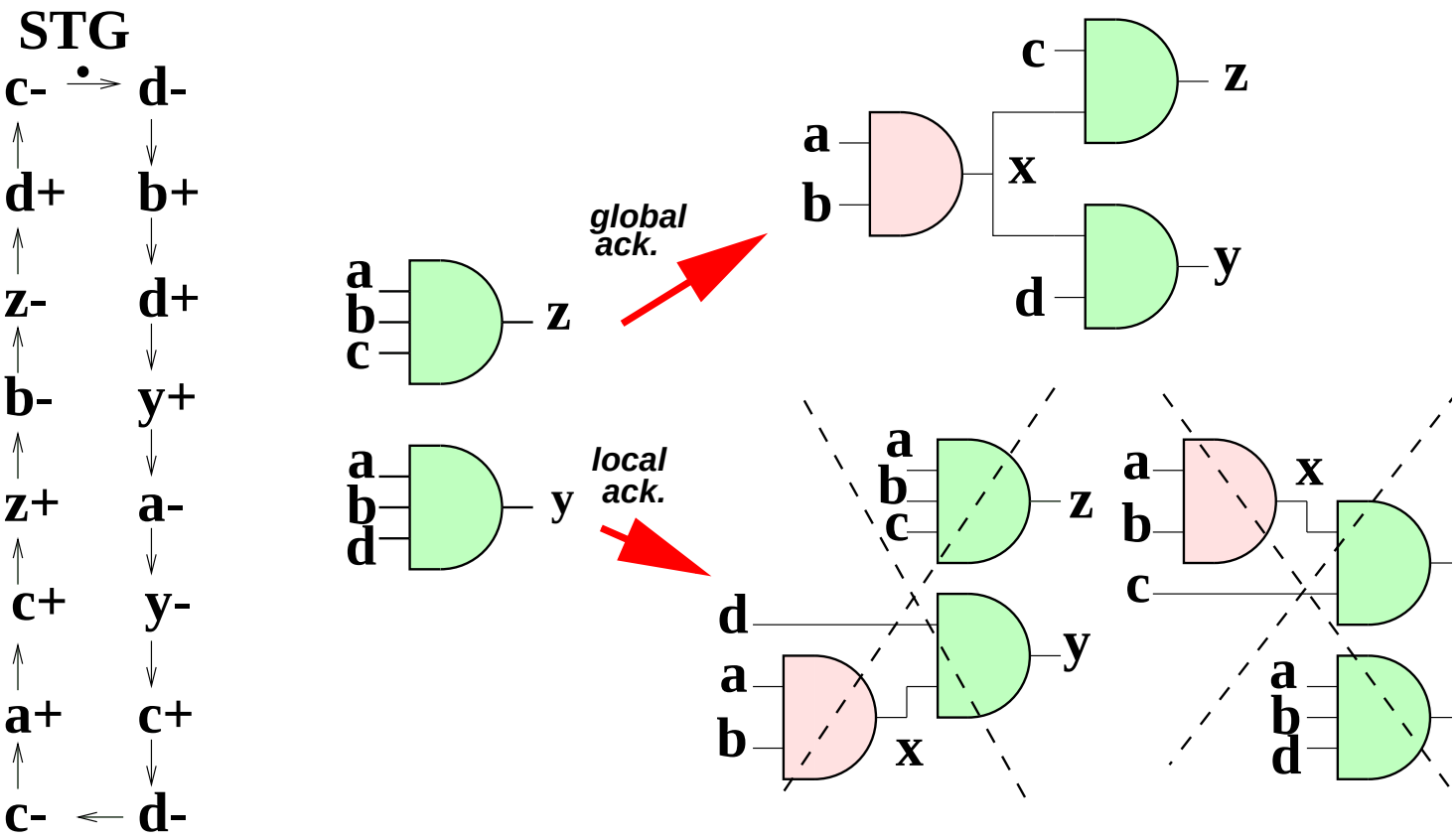
Basic MC conditions are limited:

- Unique entry condition:
  (No OR-causality is allowed)
- No complex gates in SOP logic
- Sufficient but not necessary
  (one literal cubes, don't cares for C-elements)

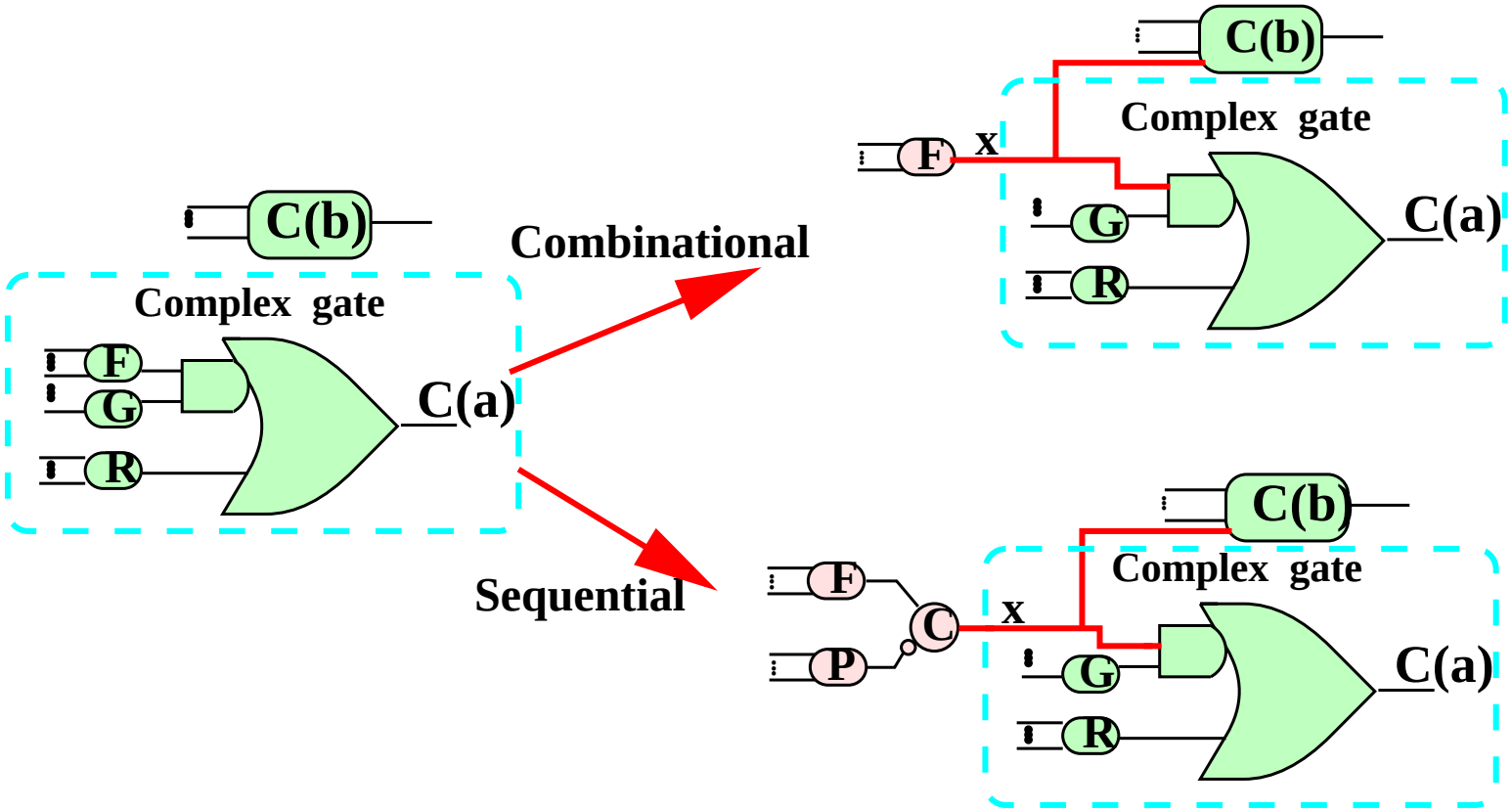


Monotonous cover ⇒ Extended monotonous cover

Global acknowledgement is important



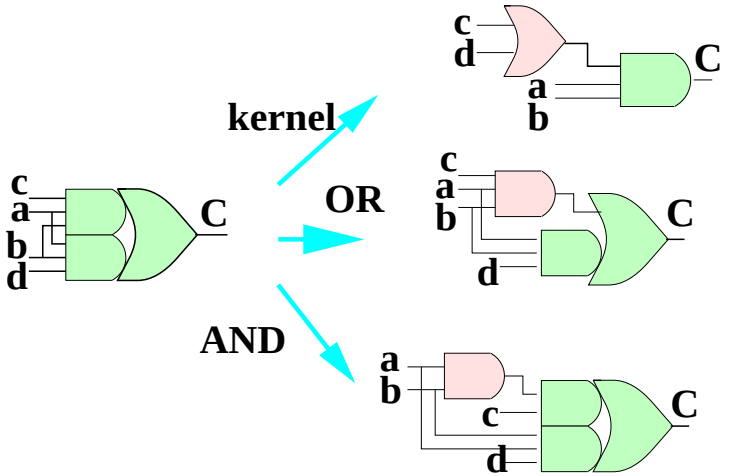
Types of decomposition



Algebraic factorization

Algebraic division $C = F \times G + R$

- Cover: $C = abc + abd$
- Kernel, cokernel: $C = ab(c + d)$
- OR decomposition: $C = (abc) + abd$
- AND decomposition: $C = (ab)c + abd$

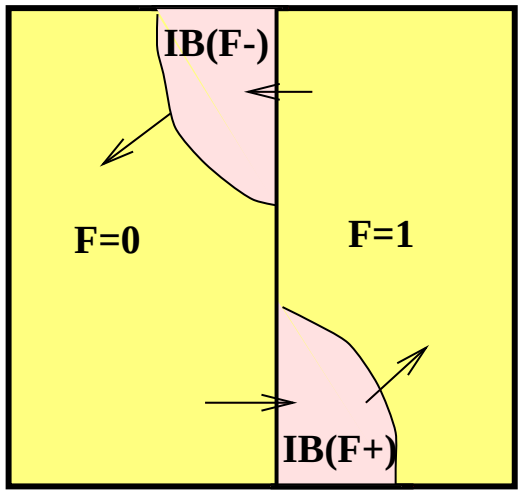


I-partition defined by a function

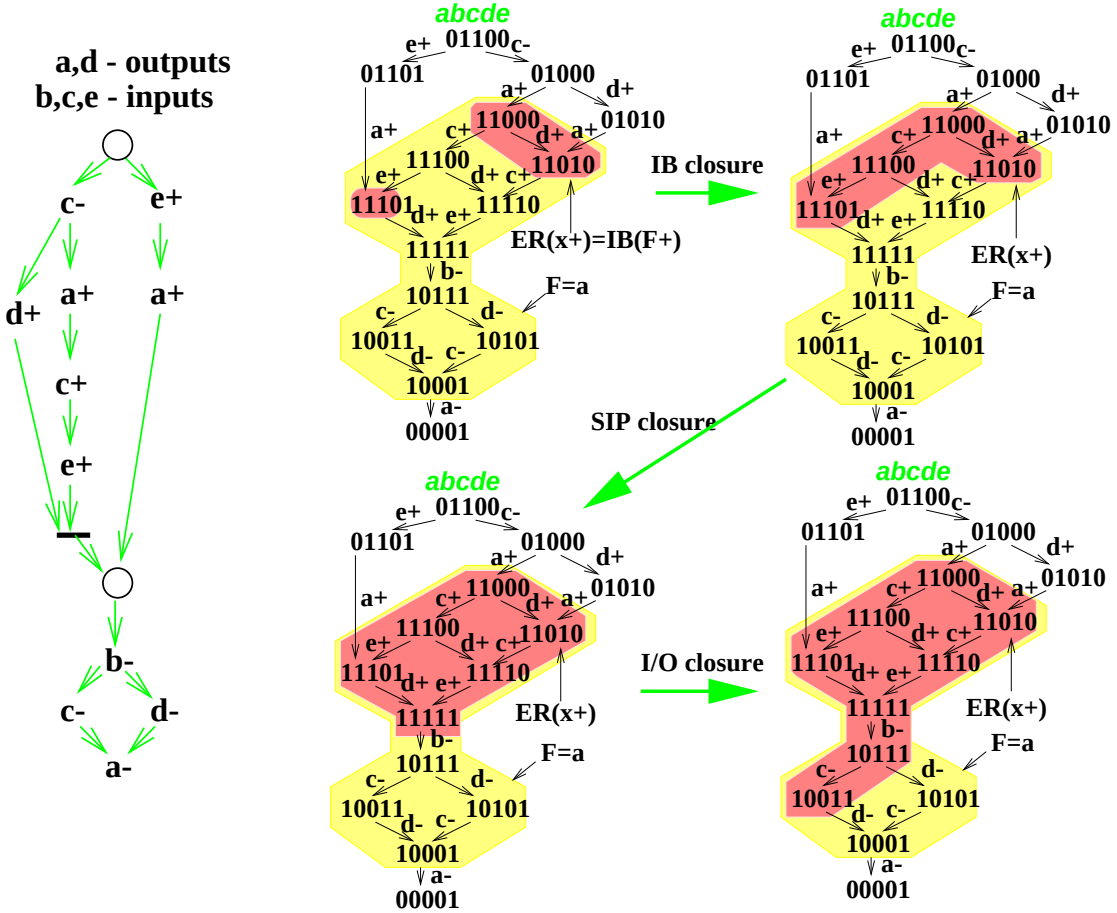
- Divisor $\Rightarrow$ State space partition

  $S = \{F^0, IB(F^+), F^1, IB(F^-)\}$

- SIP conditions to insert events (speed-independence)
- Input border closure
  - Preserve consistency ($x+$ and $x-$ alternate)
  - Preserve I/O interface (input signals are not delayed)



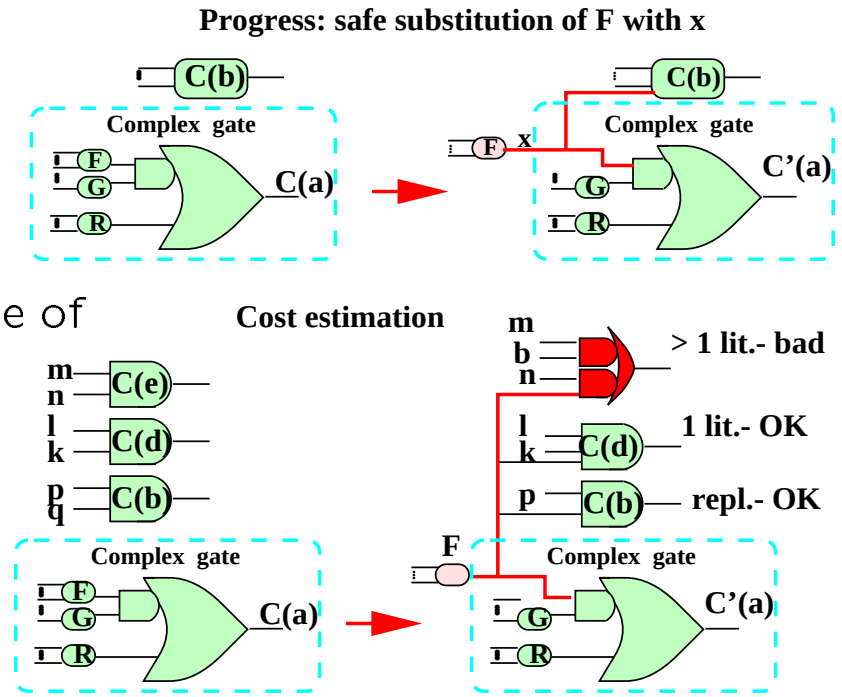
Example: construction of SIP sets



Progress in decomposition

$C(a) = F * G + R \Rightarrow$
$x = F;\ C'(a) = x * G + R$
x – inserted signal

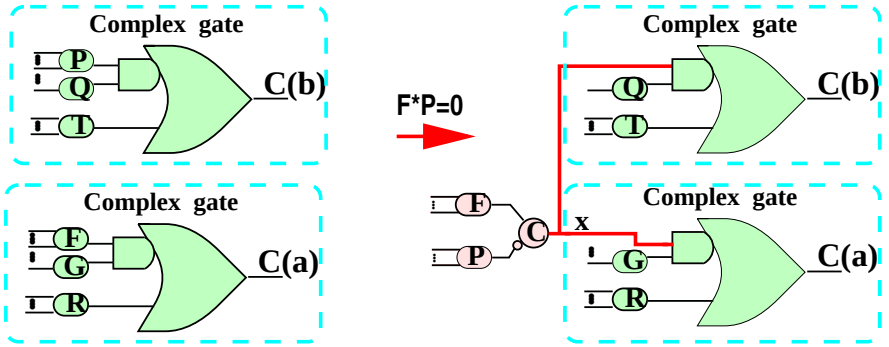
- SIP guarantees speed-independence for signal x
- Does not guarantee speed-independence of $C'(a)$ (progress conditions)
- To acknowledge x other functions can be changed (estimation of decomposition cost)



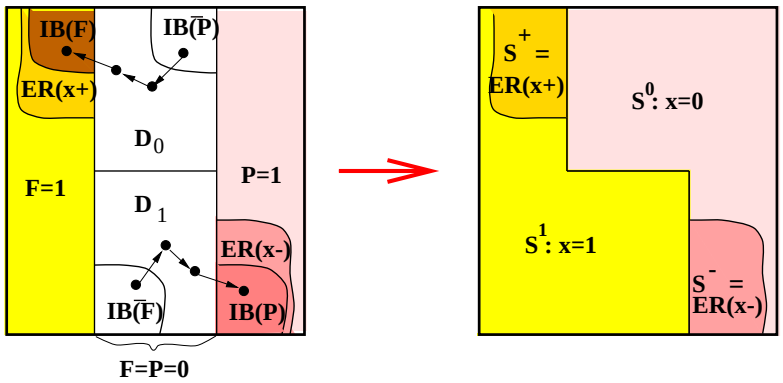
Sequential decomposition

Shortcomings
of combinational decomposition:

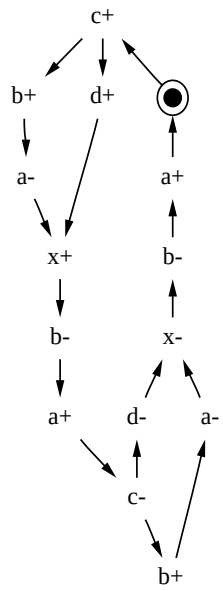
- Only $x+$ is used for simplification (no useful job by $x-$)
- No freedom for choosing $ER(x-)$ (defined by divisor F)

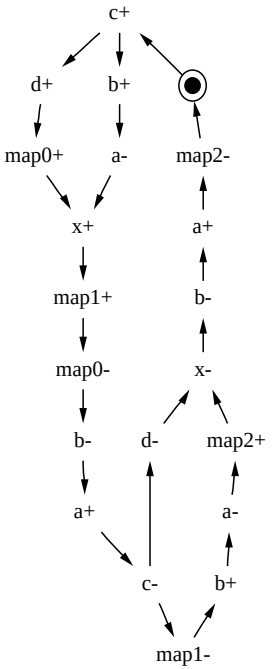


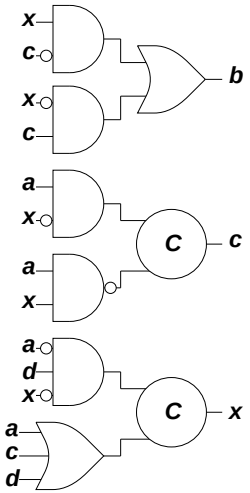
Correctness conditions:
(1) $D1 \cap D2 = \emptyset$
(2) $Succ(D1) \subset IB(P)$
(3) $Succ(D2) \subset IB(F)$

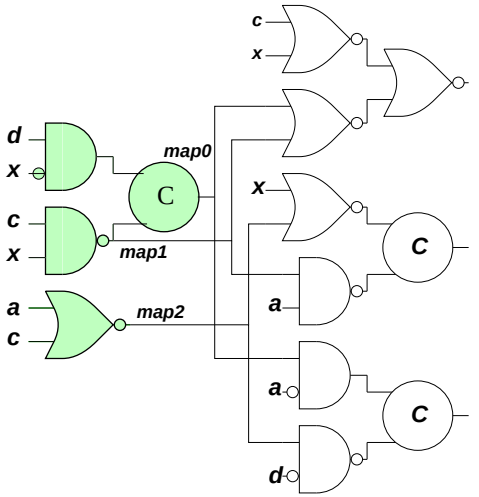


Example of decomposition. I

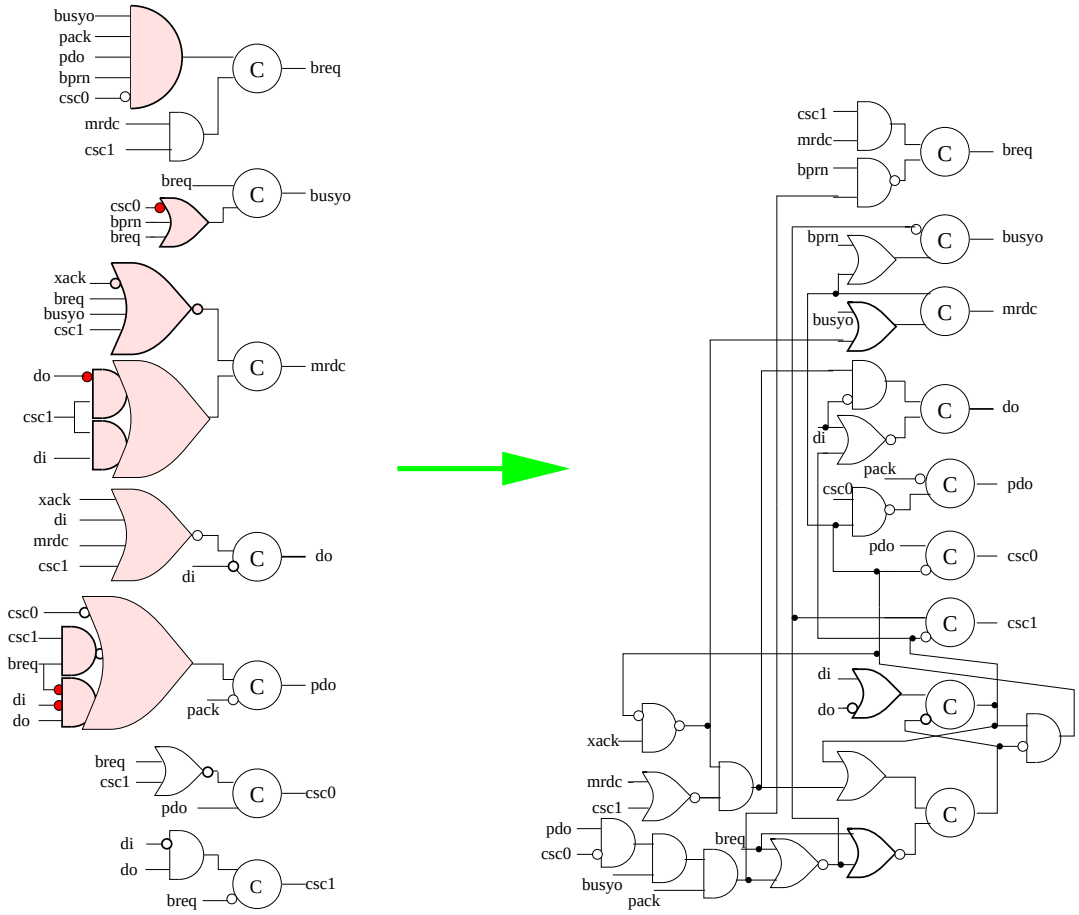




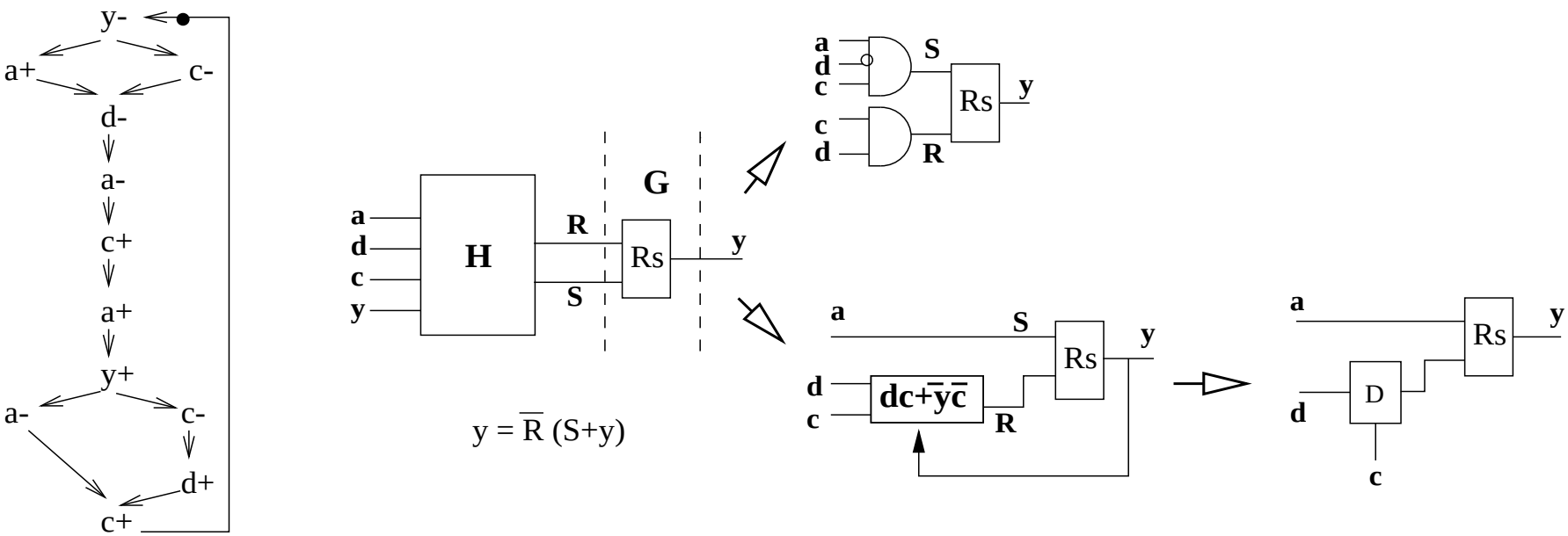




Example of decomposition. II



Decomposition based on Boolean Relations: example (I)



Decomposition based on Boolean Relations: example (II)

dy \ ac	00	01	11	10
00	0	0	1	0
01	1	1	1	1
11	1	0	-	1
10	0	0	0	0

y = acd' + y (c'+d')

dy \ ac	00	01	11	10
00	1--0	1--0	01	1--0
01	0-	0-	0-	0-
11	0-	1-	--	0-
10	1--0	1--0	1--0	1--0

R=cd; S=acd'
R=cd+c'y'; S=a

0 -> 0: RS=1-,-0
0 -> 1: RS=01
1 -> 0: RS=1-
1 -> 1: RS=0-

Boolean Relations for different latches and gates.

Region	Trans.	C-element H_1, H_2	D-latch C, D	Rs R, S	Sr S, R	AND H_1, H_2	OR H_1, H_2
$ER(y+)$	$0 \rightarrow 1$	11	11	01	1−	11	$\{1-, -1\}$
$QR(y+)$	$1 \rightarrow 1$	$\{1-, -1\}$	$\{0-, -1\}$	0−	$\{1-, -0\}$	11	$\{1-, -1\}$
$ER(y-)$	$1 \rightarrow 0$	00	10	1−	01	$\{0-, -0\}$	00
$QR(y-)$	$0 \rightarrow 0$	$\{0-, -0\}$	$\{0-, -0\}$	$\{1-, -0\}$	0−	$\{0-, -0\}$	00
unreach.		−−	−−	−−	−−	−−	−−

C element: $y = H_1H_2 + y(H_1 + H_2)$

D latch: $y = CD + \bar{C}y$

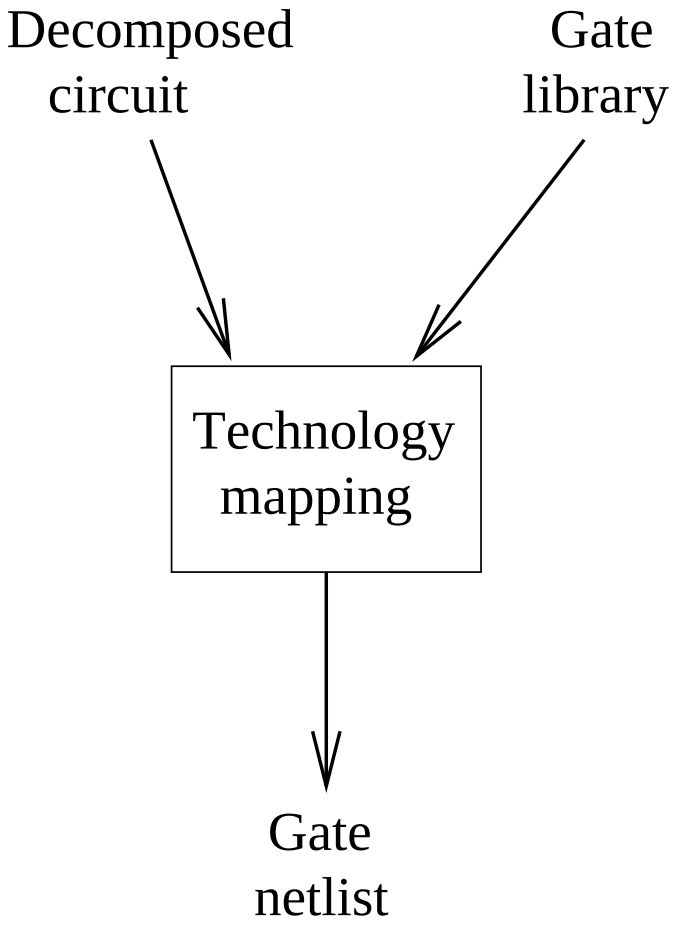
Rs latch: $y = \bar{R}(S + y)$

Sr latch: $y = S + \bar{R}y$

AND gate: $y = H_1H_2$

OR gate: $y = H_1 + H_2$

Technology mapping



- Logic decomposition
- Graph covering based on
  - Tree matching
  - Boolean matching

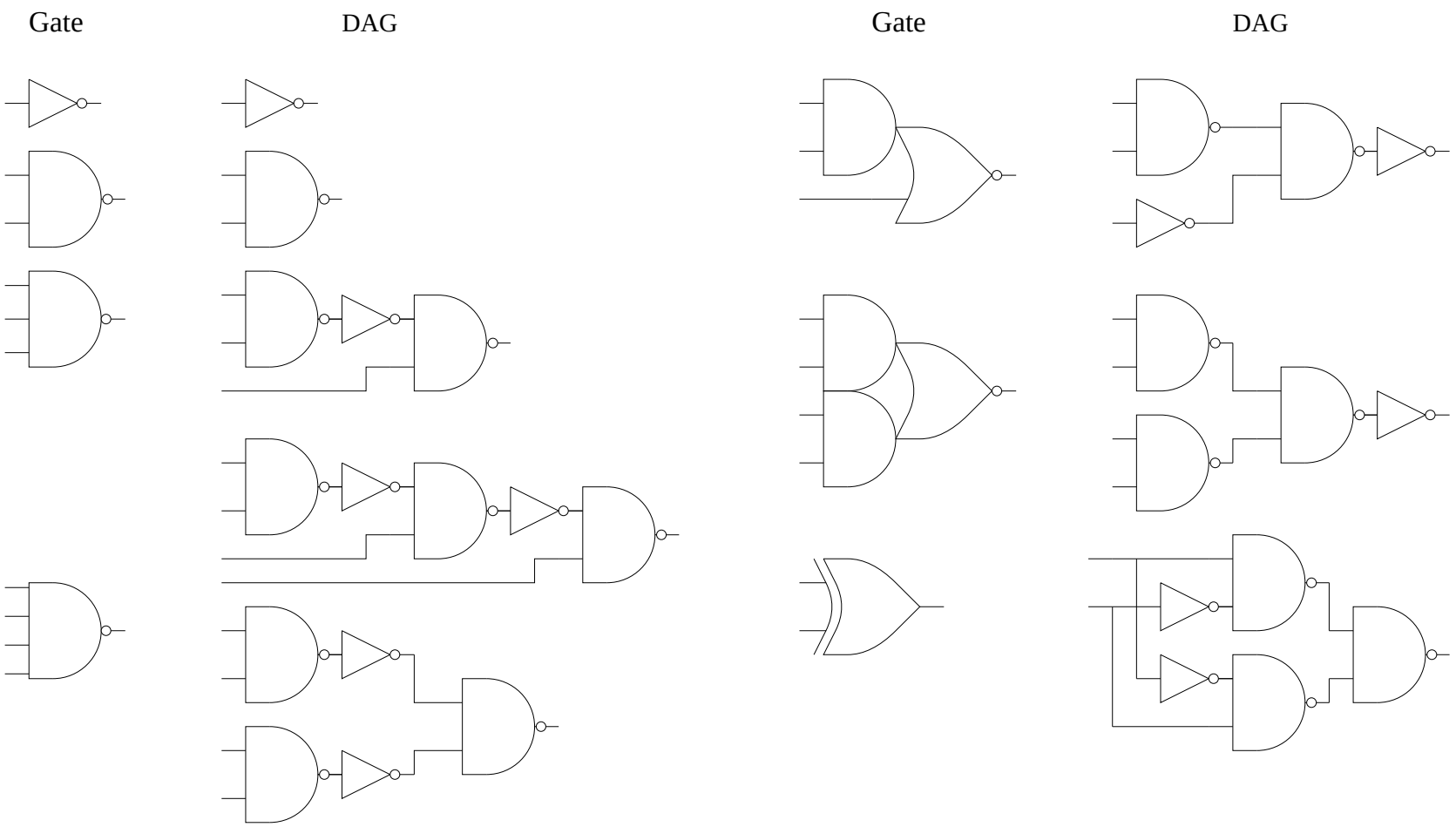
References:

- Keutzer 87
- De Micheli 96.

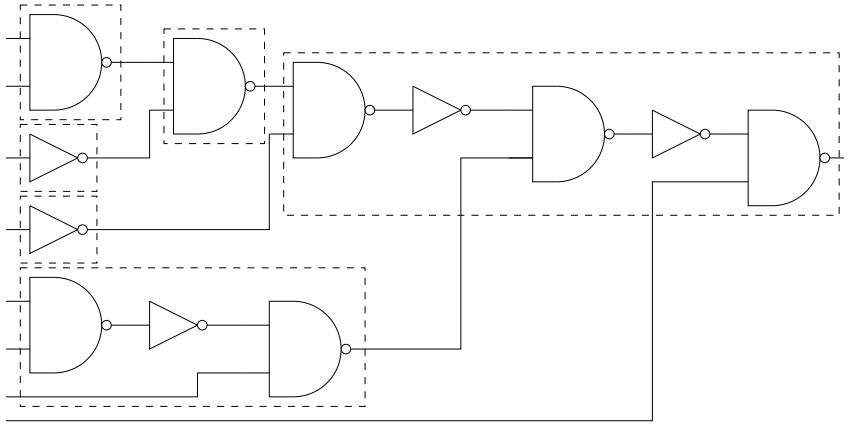
Additional complexity for SI:

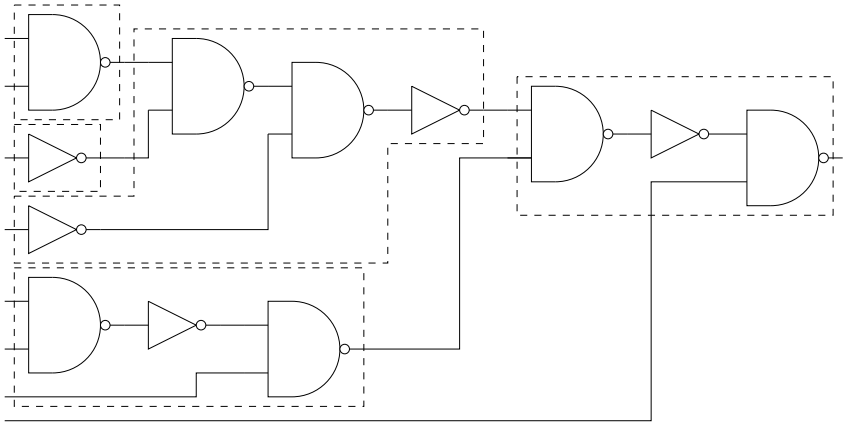
- SI-preserving decomposition

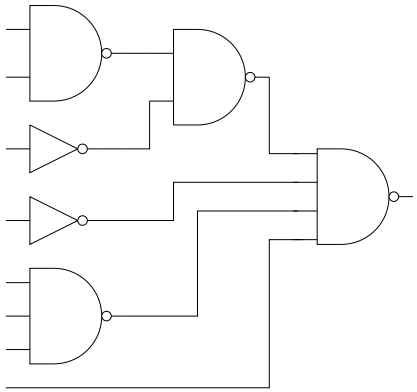
Library for technology mapping

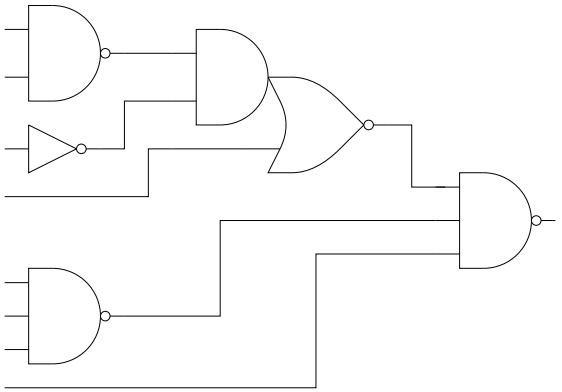


Technology mapping: graph covering

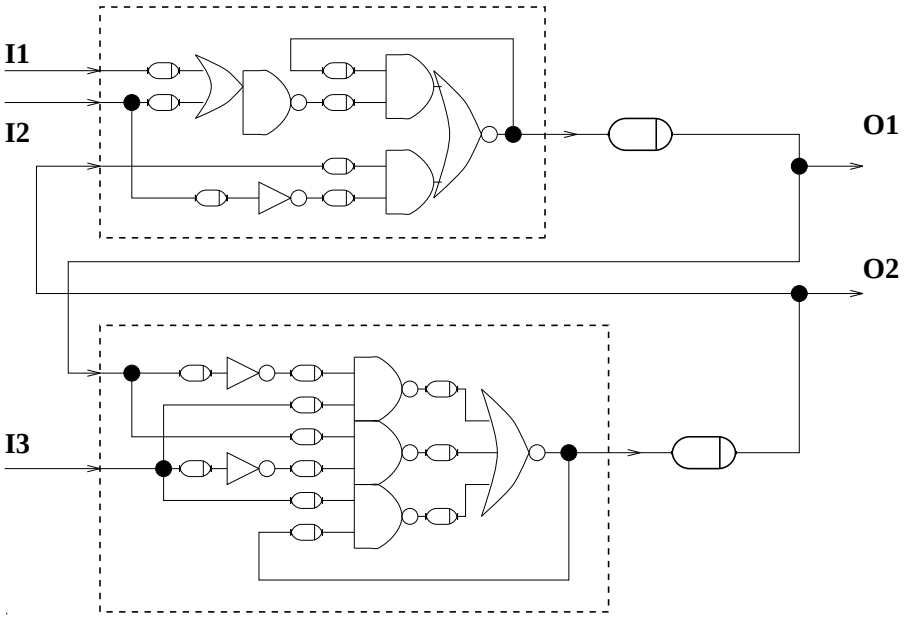








Synthesis of bounded-delay circuits

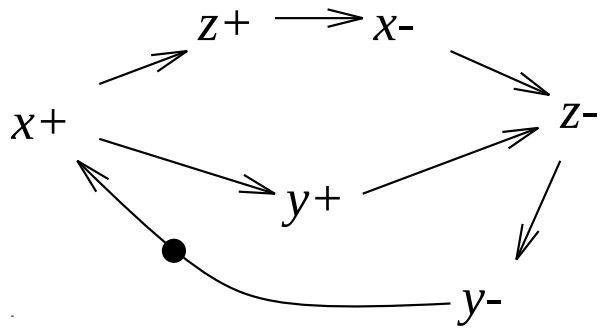


- Lavagno'91
- Nowick'92
- Myers'94

- One combinational logic block for each STG non-input signal
- Decouple hazards from races

Synthesis algorithm properties

- Two classes of hazards:
  - from concurrent transitions
  - from ordered transitions

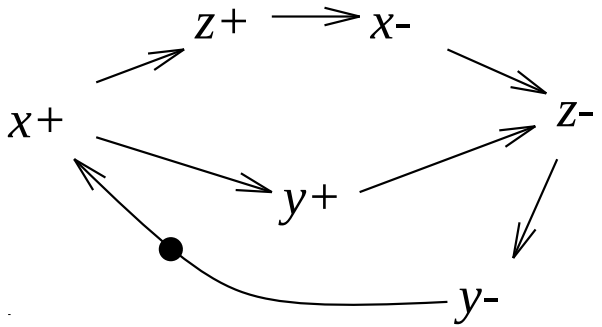


- The initial synthesis algorithm guarantees no hazards from *concurrent* transitions (condition similar to FSM)

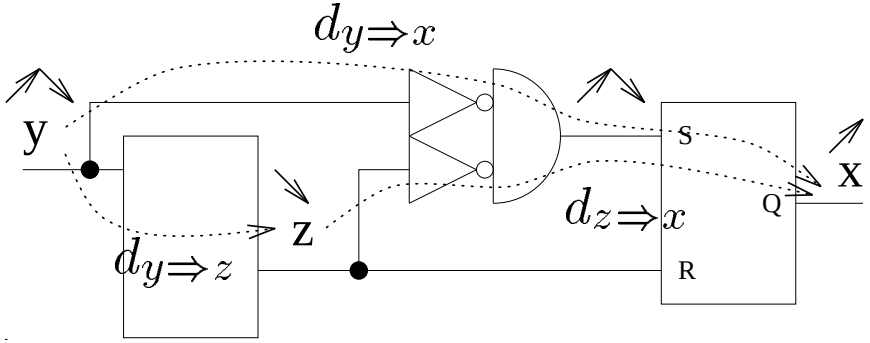
  (for concurrent $z+$ and $y+$ cube x is added to f_z e.g.)

Remaining hazards

- Ordered transitions: $y+ \rightarrow z-$ (x should not be affected)



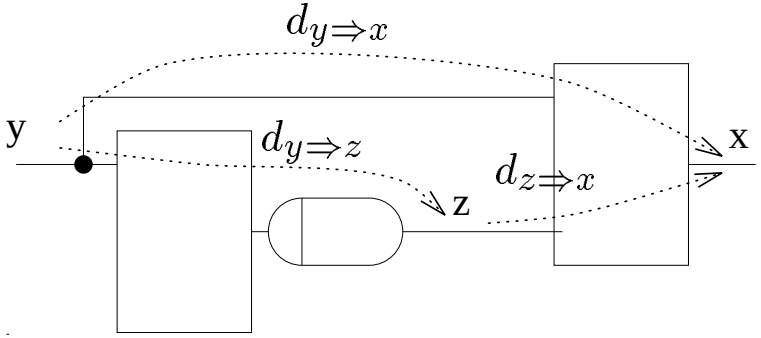
- Corresponding circuit:



- Hazard if $d_{y \Rightarrow x} > d_{y \Rightarrow z} + d_{z \Rightarrow x}$ (transition order **reversed** for x)

Hazard elimination idea

- For each case in which a hazard exists if $d_{y \Rightarrow x} > d_{y \Rightarrow z} + d_{z \Rightarrow x}$
  - if possible, balance $d_{y \Rightarrow x}$ and $d_{z \Rightarrow x}$
  - otherwise, increase $d_{y \Rightarrow z}$



- Eliminating one hazard does not make any other hazard worse:
  - $d_{y \Rightarrow x}$ and $d_{z \Rightarrow x}$ are measured *before* the padded delay
  - $d_{y \Rightarrow z}$ is measured *after* the padded delay

Analogy with synchronous circuits

- In classical synchronous circuit synthesis:
  - slow down *the clock* until *all events* complete propagation
- In bounded delay asynchronous circuit synthesis:
  - slow down *each signal* until *all events that caused its transition* complete propagation
- We can use similar timing analysis techniques for the combinational logic blocks...

Summary of logic synthesis

- Different algorithms for different delay models
  - neglecting wire delays, robust with respect to gate delays
  - considering wire delays but assuming bounds on them
- In any case, post-layout timing analysis is required
- Hierarchical decomposition:
  - bounded delays within blocks
  - unbounded wire delays between blocks
- Choosing the right granularity is important

Part 6: Verification and validation

- What is verification
- STG implementability
- Verification by state models
- Circuit analysis
- Fighting with state explosion
- Verification by event models
- Simulation

Verification

- Checking properties of a **specification**

  Example: Given an STG describing a bus protocol, check that

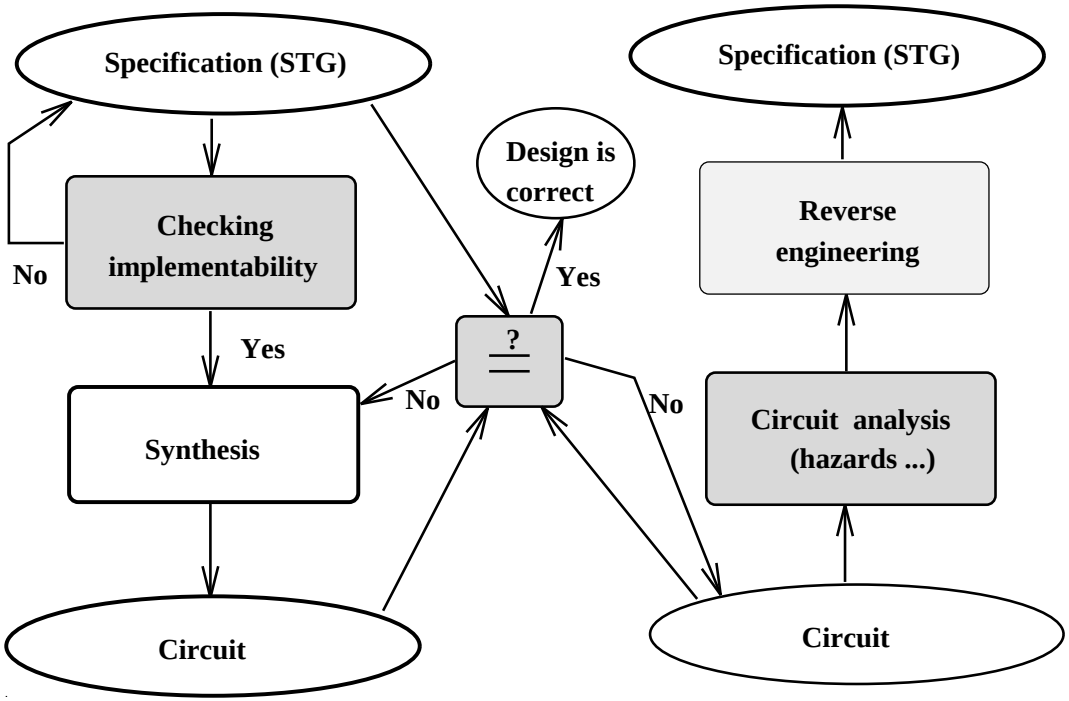
  - it does not deadlock (property verification)
  - it can be implemented by an asynchronous circuit (implementability)

- Checking properties of an **implementation**

  Example: Given a circuit check that

  - it is speed-independent (property verification)
  - it correctly implements a given STG specification (implementation verification)

Verification in design flow



Verification is needed both for top-down and bottom-up design

Verification of STG specifications

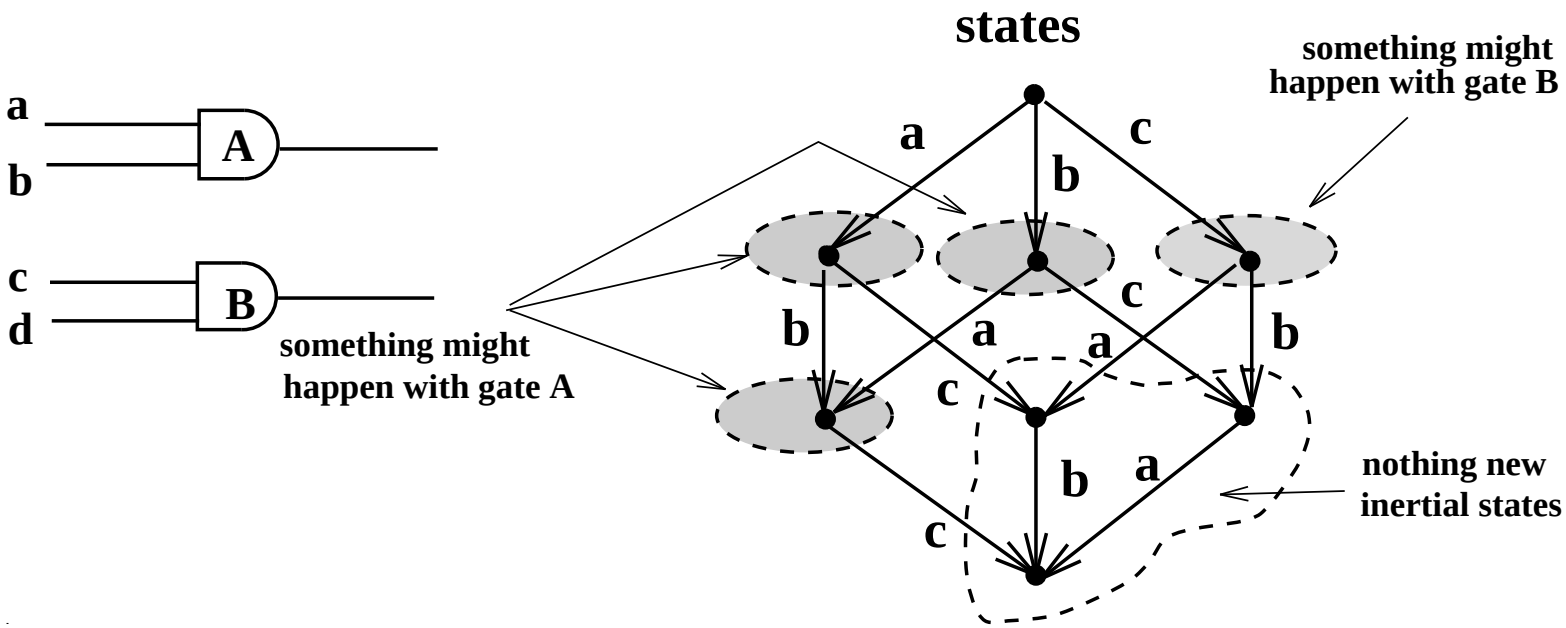
- Property verifications
  - Safety properties: deadlocks, mutual exclusion, concurrency, preceding between events etc.
  - Liveness properties: progress and fairness conditions
  - Structural invariants and traps based on theory of Petri Nets
- Implementbility verifications
  - Boundedness
  - Consistensy of state encoding
  - Completeness of state encoding, reducability of CSC-conflicts
  - Persistency

Fight with state explosion

- Efficient state representation
  - BDD-based techniques (Bryant, Cortadella et al.)
  - State space reduction (Kishinevsky)

- Use of event-based models
  - Unfoldings of Petri Nets and STGs
    (McMillan, Kondratyev et al., Esparza)
  - Stubborn sets (Valmari)
  - Partial orders (Probst, Godefroid)
  - Reduction of nets (Murata, Esparza)

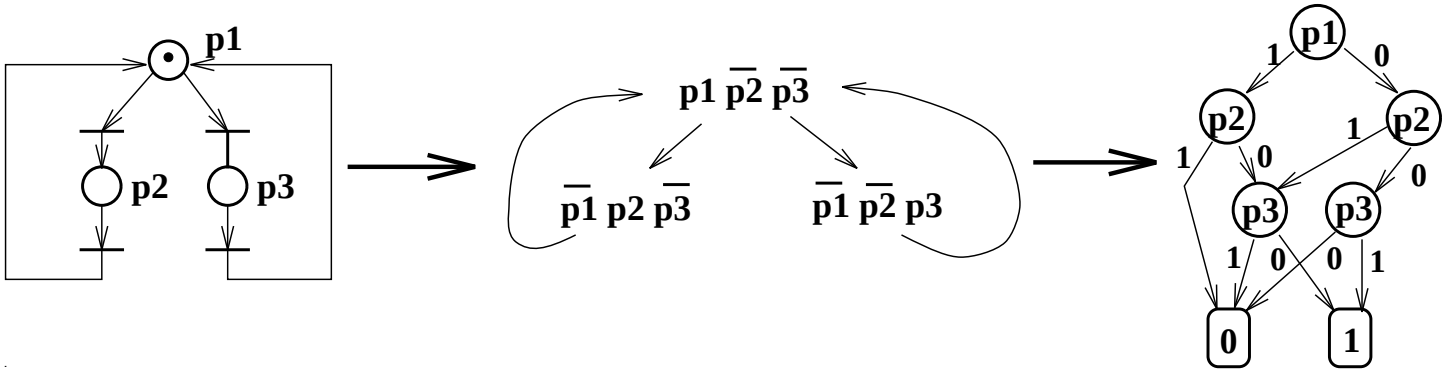
State reduction



- Only transitions on gate inputs may cause an output transition
- Micropipeline control queue: run time reduced from 1 hour to 1 sec
- Efficient for fighting with concurrency. Choice is difficult to handle

BDD representation of reachable states

All reachable markings (**reachability set**):
$p1\overline{p2}\ \overline{p3} + \overline{p1}p2\overline{p3} + \overline{p1}\ \overline{p2}p3$

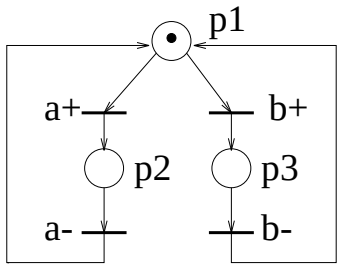


The characteristic function of the reachability set can be represented by a reduced ordered BDD

Symbolic traversal of STG

Each property is represented by a characteristic function

Full state = marking + binary state of signals



$$M_0 = p_1\overline{p}_2\overline{p}_3$$

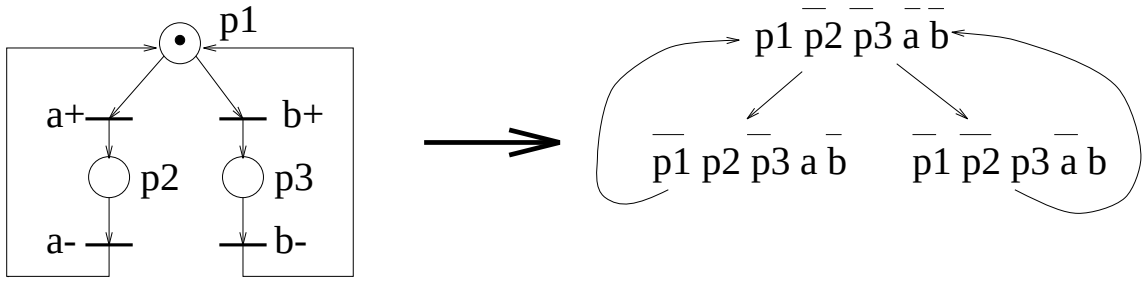
$$S_0 = p_1\overline{p}_2\overline{p}_3\overline{a}\overline{b}$$

$$\mathsf{E}_t = \prod_{p_i \in {}^\bullet t} p_i \quad (t \text{ enabled}) \qquad \mathsf{ASM}_t = \prod_{p_i \in t^\bullet} p_i \quad (\text{succ. marked})$$

$$\mathsf{NPM}_t = \prod_{p_i \in {}^\bullet t} \overline{p_i} \quad (\text{pred. unmarked}) \qquad \mathsf{NSM}_t = \prod_{p_i \in t^\bullet} \overline{p_i} \quad (\text{succ.unmarked})$$

Checking properties via traversal

One-step reachability: $\delta_N(M,t) = (M_{\mathsf{E}_t} * \mathsf{NPM}_t)_{\mathsf{NSM}_t} * \mathsf{ASM}_t$



Consistency: $\text{Inconsistent(a)} = E(a+) * a \; + \; E(a-) * \overline{a}$

Persistency: $\delta_N(\ \mathsf{E}_{a+}, b+) * \overline{E_{a+}} \not\equiv 0$

Specs with 10^{23} states were checked by BDD-based traversal!

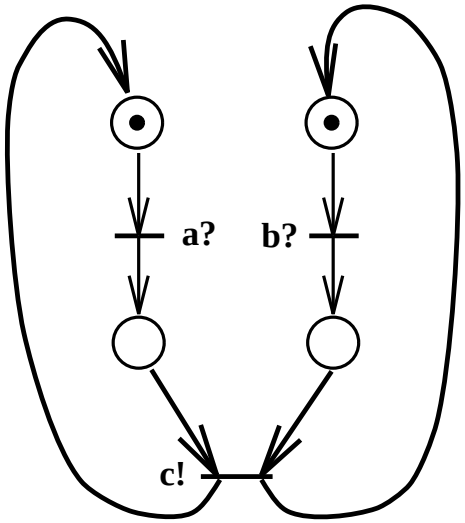
Verification in trace theory

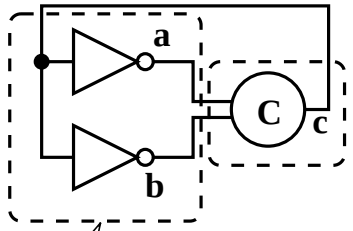
Dill, Rem, Udding, van de Snepscheut, Ebergen

- Specification of Join:
  $pref * [a?; c!] || pref * [b?; c!]$
  $a?, b?$ are input; $c!$ is output

- Mirror of the spec = environment:
  inputs $\leftrightarrow$ outputs:
  $pref * [a!; c?] || pref * [b!; c?]$

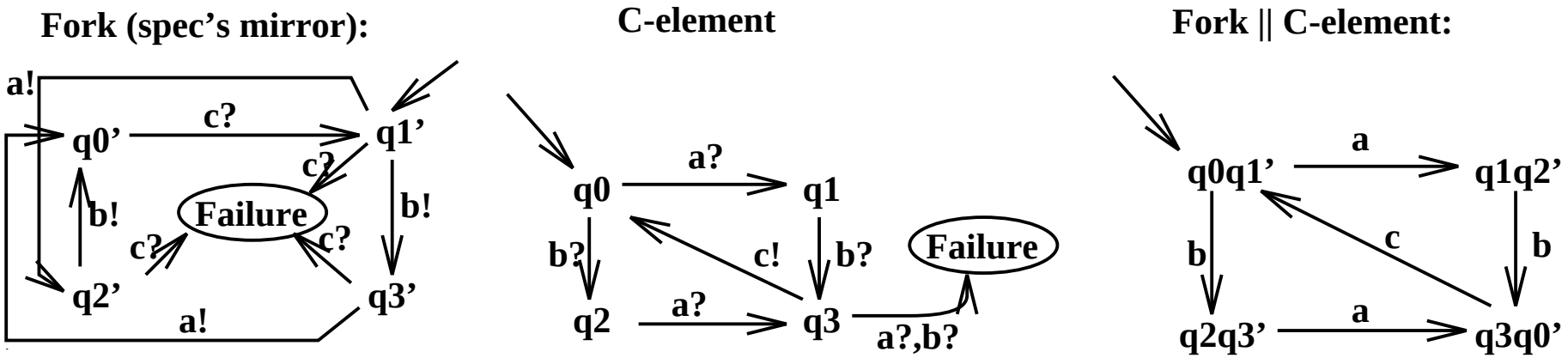
- Does a C-element implement the Join?





circuit = mirror of the spec

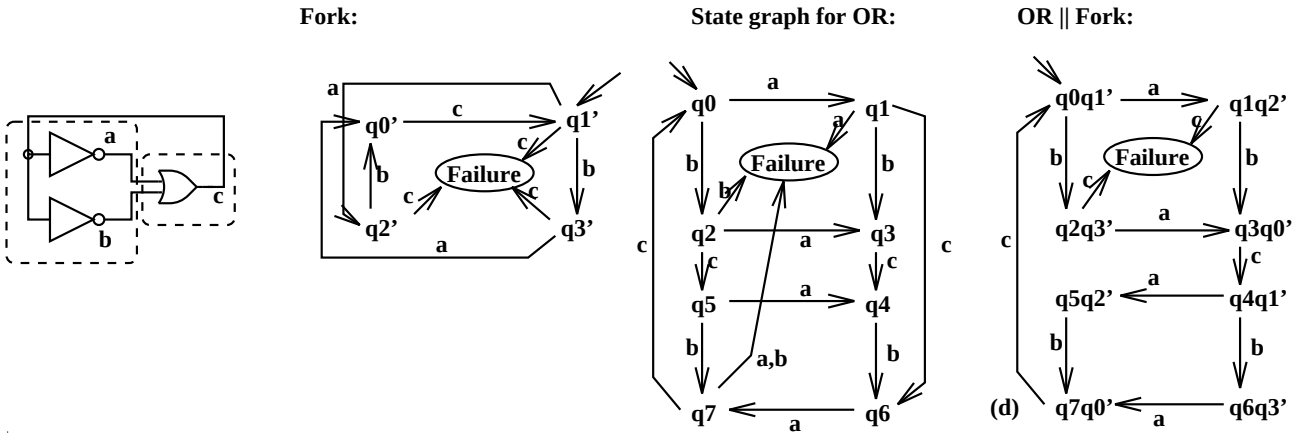
Failure states and hazardous behavior



Hazardous behavior (non speed-independence) =
failure states are reachable in the composite state graph

It also shows that the circuit does not implement the spec

Incorrect implementation



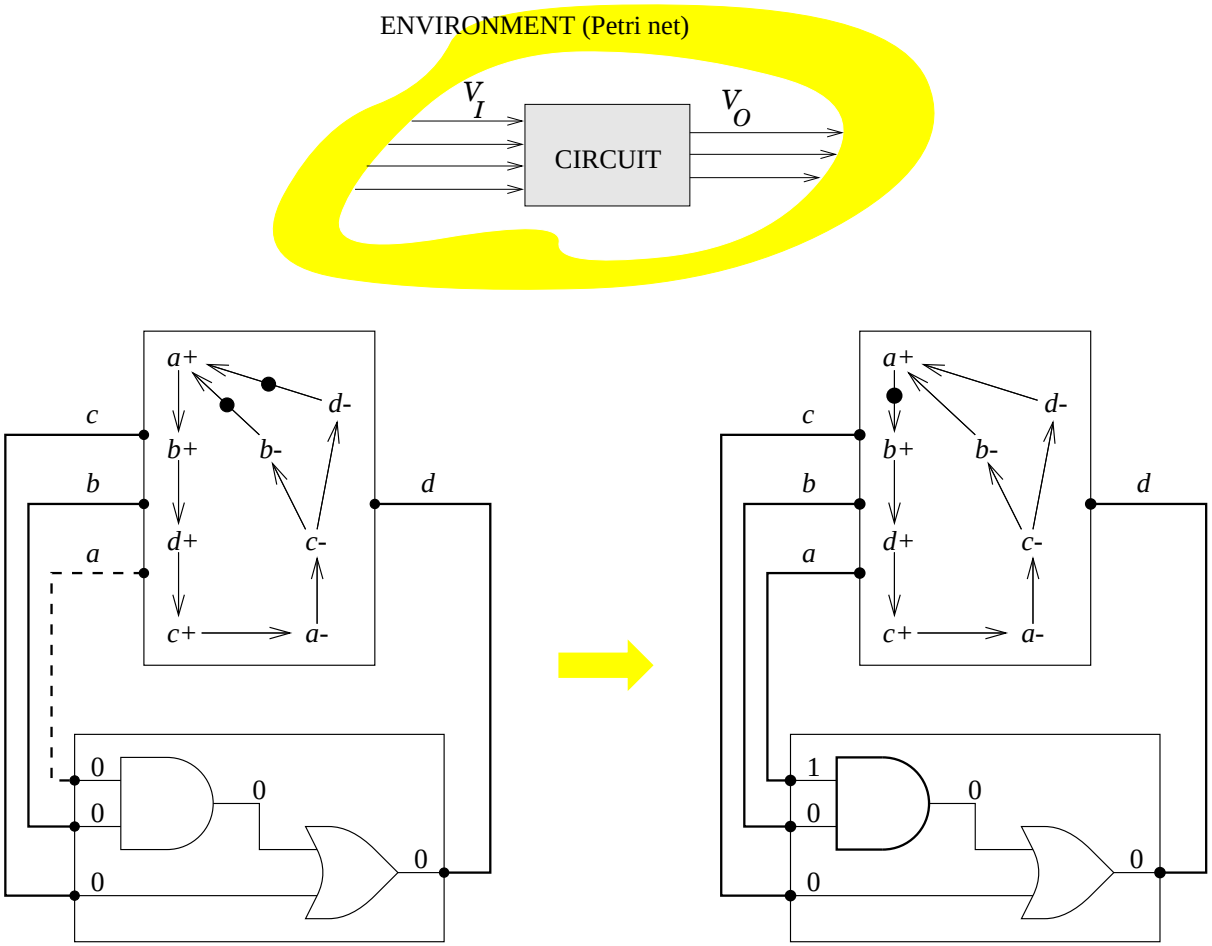
OR-gate is not an implementation for the Join

Failure state is reachable $\Rightarrow$ an oscillator OR-gate + two inverters is not speed-independent

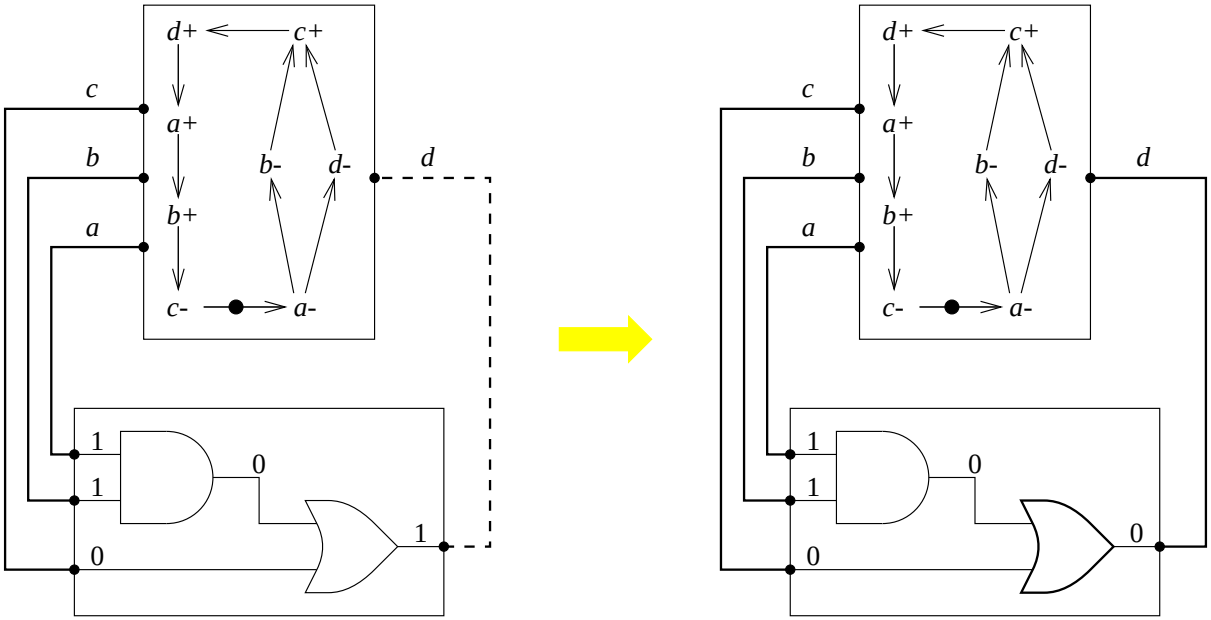
Compare with speed-independence analysis

Parallel composition of state graphs is inefficient

Verification via composition environment/circuit



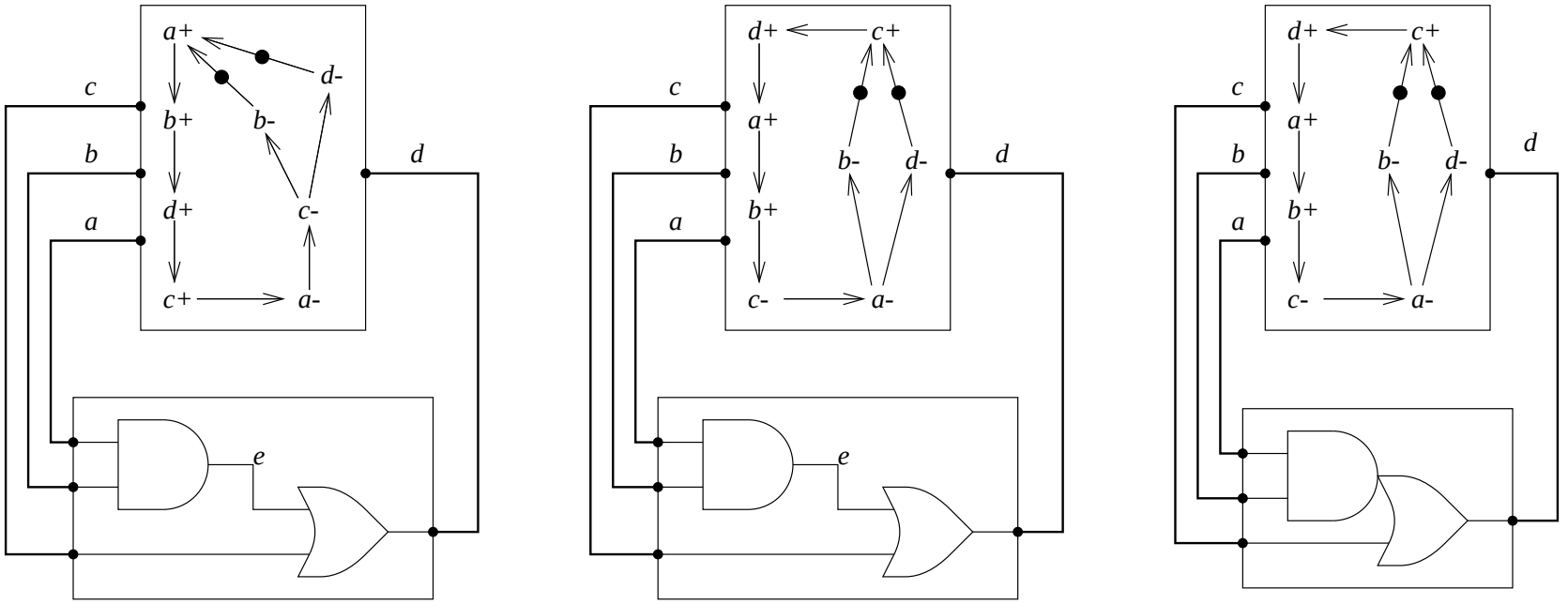
Verification: failure states



Failure state: circuit produces unexpected output transition (enabled in the circuit, but disabled in the environment)

Diagnosis: find a trace of events from initial to failure state (important for circuit redesign)

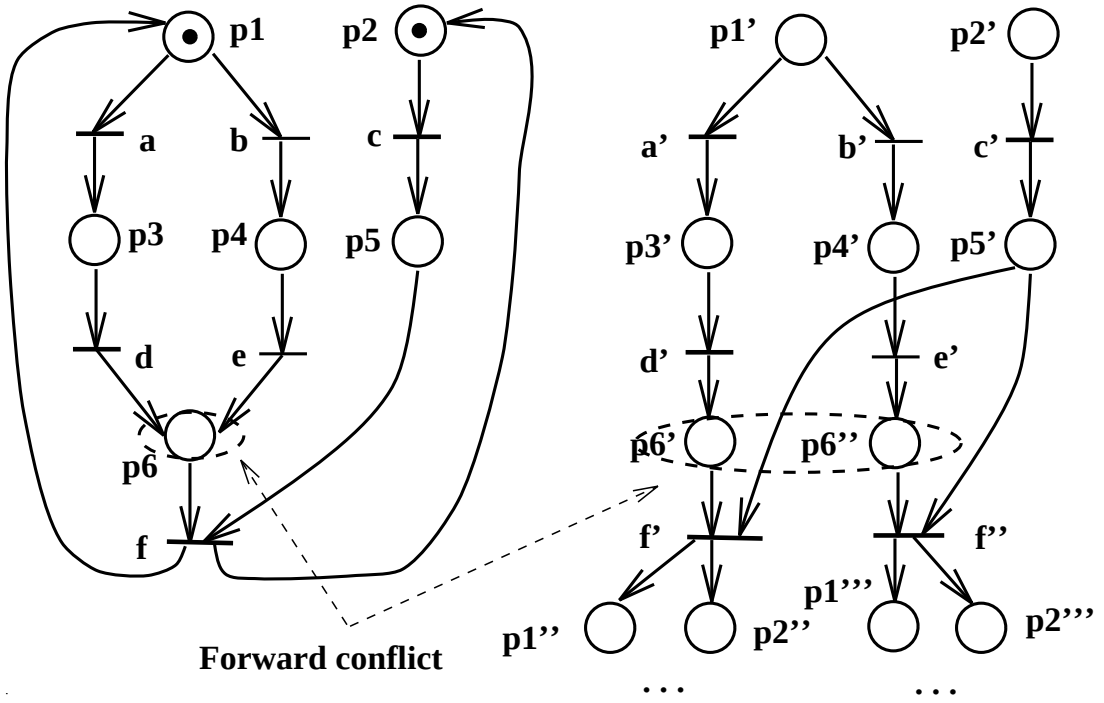
Correctness environment/circuit: examples



Correctness is not a property of a circuit but of the interaction of a circuit with an environment.

Unfolded Petri net

- Occurrence net = an *infinite* unfolded Petri Net
- All forward conflicts are split

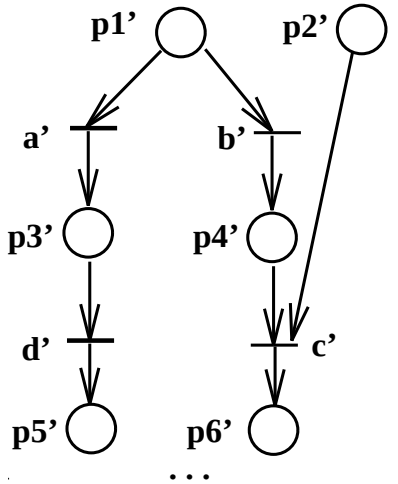


Truncating occurrence nets

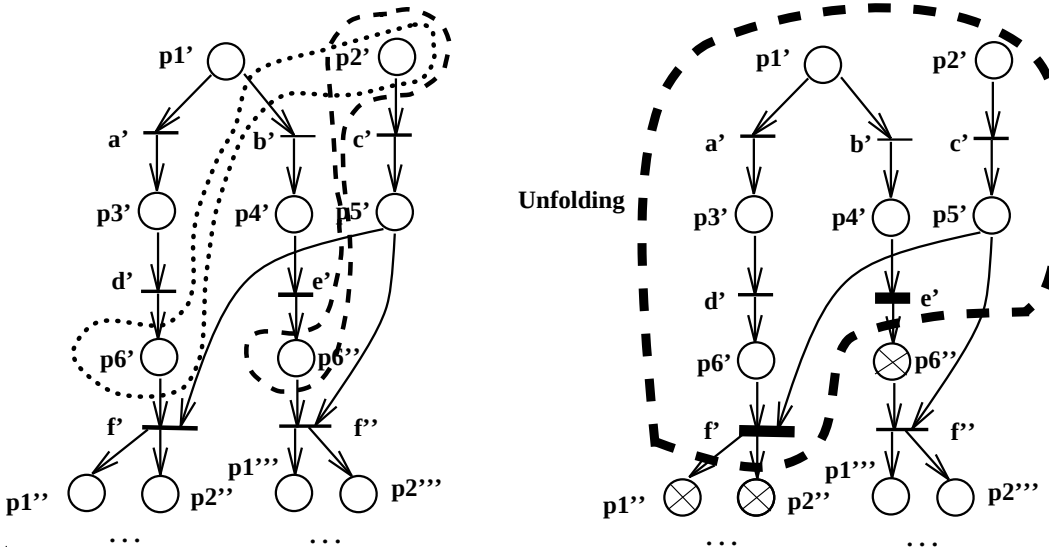
- **Unfolding** is a finite prefix of the occurrence net
- **Completeness**: no reachable marking of PN is missing
- **Configuration** of t' = all transitions that must fire before t' (Conf. $d' = \{a'\}$)
- **Basic marking** of t' = marking after all transitions from the local configuration of t' have fired ($BM(d') = p5'p2'$)
- **Cutoff** is a transition whose successors can be removed:

if basic-marking(t')= basic-marking(t'') **and** size-of-configuration(t') < size-of-configuration(t'') **then** t'' – cutoff

(More efficient criteria exist)



Unfoldings



- Basic markings of f' and f'' are equal

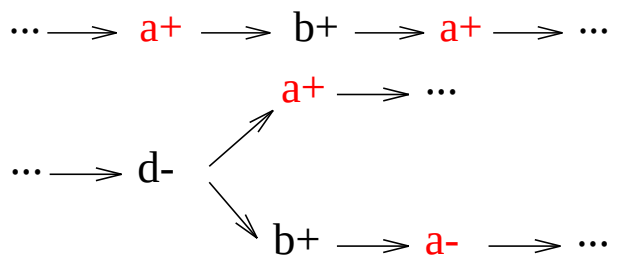
- **Ordering relations** are easy to derive:
  (a' and c' are concurrent, a' precedes f', a' and e' are in conflict)
- All markings are in unfolding $\Longleftrightarrow$ all PN properties can be studied
- In many cases it is more efficient than BDD traversal

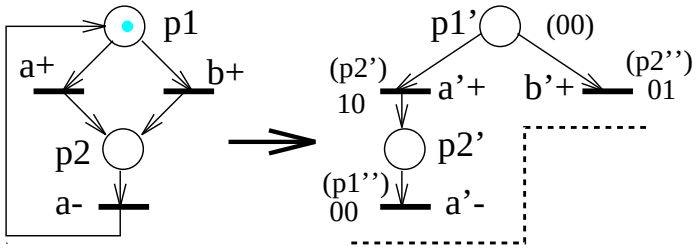
Ordering relations in unfolding can be analyzed with $O(N^3)$ complexity

STG verification by unfolding: consistency

- **Sign alternation (SA)**
- **Non-autoconcurrency (NA)**
- **Proper assignment (PA)**

  (same basic marking – same binary state)



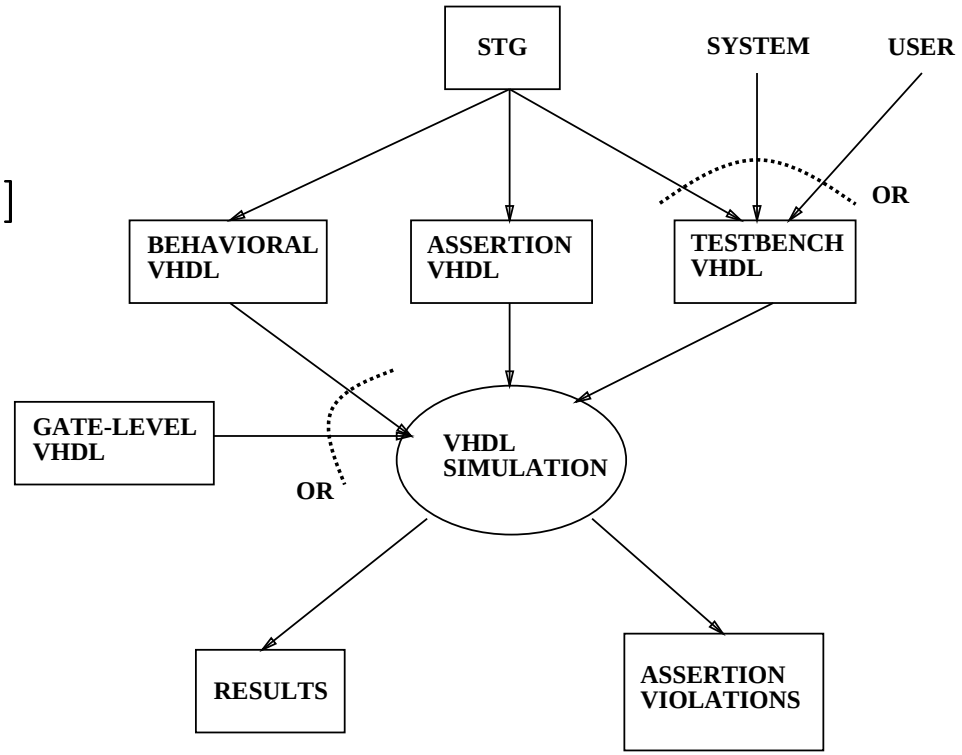


SA + NA + PA $\Longleftrightarrow$ STG is consistent

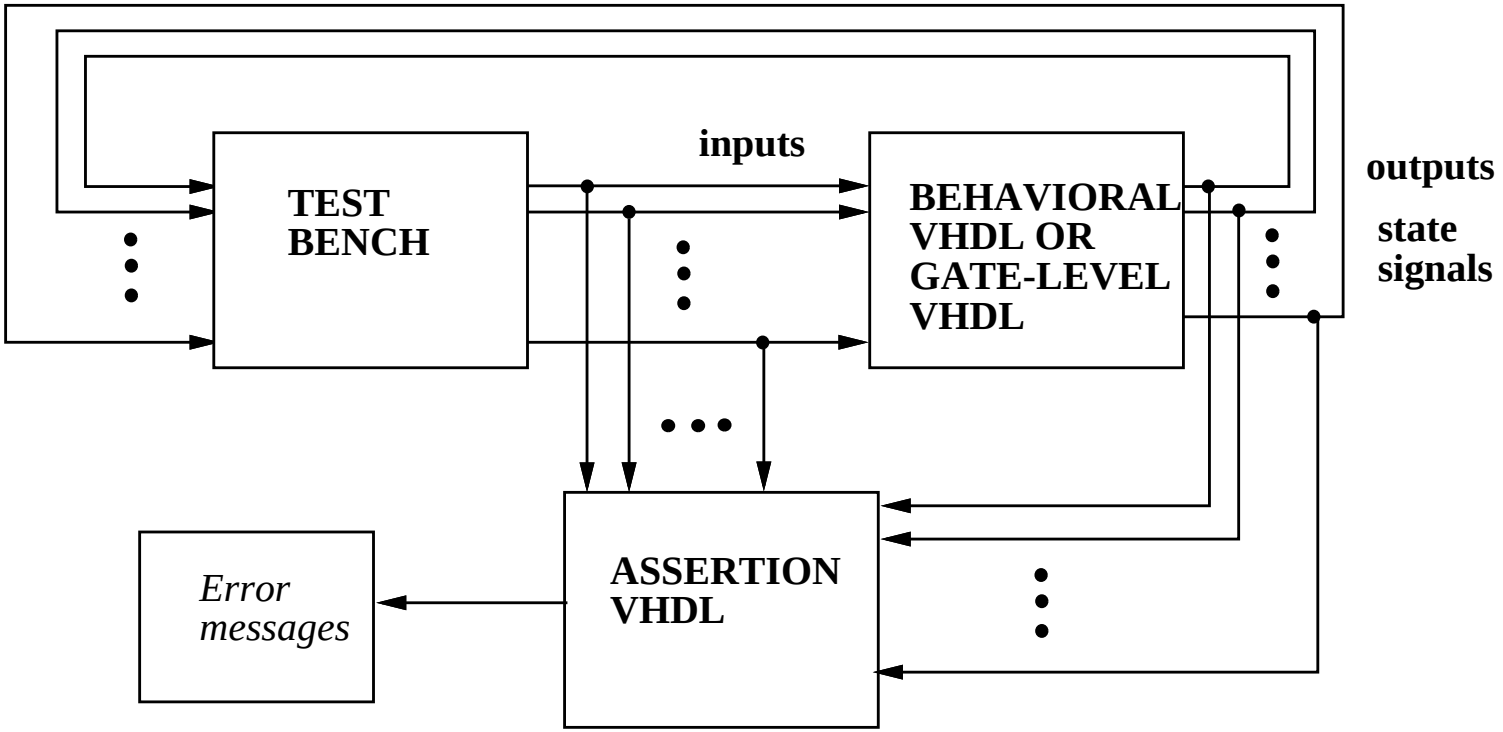
- Autoconcurrency = particular case of concurrency
- Sign alternation = particular case of precedence
- Proper assignment reduces to precedence checking

SIMULATION ENVIRONMENT

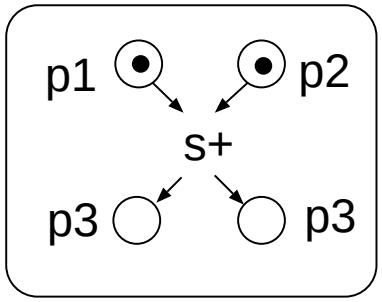
[Vanbekbergen 95]



ARCHITECTURE

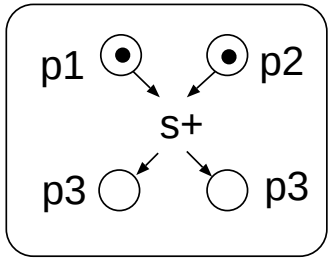


VHDL MODEL



- State = set of tokens in places
- A vector of Booleans: places
  - $places(1) = 1$ if place p_1 contains a token.
  - $places(1) = 0$ if place p_1 does not contain a token.

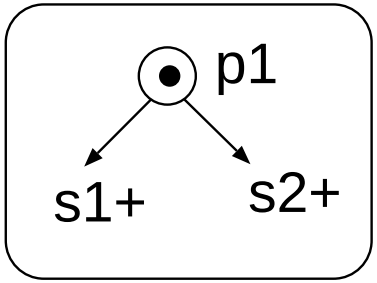
VHDL MODEL(2)




```
BLOCK (places(1) = '1' AND places(2) = '1')
BEGIN
    places(1) <= GUARDED '0';
    places(2) <= GUARDED '0';
    places(3) <= GUARDED '1';
    places(4) <= GUARDED '1';
    s <= GUARDED '1';
END;
```

- Every transition possibly concurrent with any other transition
- ONE block per transition
- Token flow modeled inside the block

CONDITIONS IN VHDL



pcond controls conditional execution

enables a different transition for each "pass"

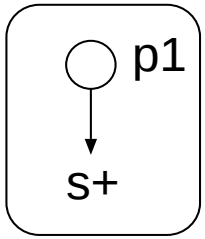
```
BLOCK (places(1) = '1' AND pcond = '0')
BEGIN
    places(1) <= GUARDED '0';
    s1 <= GUARDED '1';
    pcond <= GUARDED '1';
END;

BLOCK (places(1) = '1' AND pcond = '1')
BEGIN
    places(1) <= GUARDED '0';
    s2 <= GUARDED '1';
    pcond <= GUARDED '0';
END;
```

ASSERTION

- All blocks are possibly concurrent.
- In VHDL a resolution function is needed.
- STG is only correct if no two transitions of the same signal are enabled at the same time.
- Assertion in the resolution function that there are no two simultaneous assignments to the same signal.

ASSERTION(2)



ASSERT (s'STABLE = TRUE OR places(1) = '1' OR ....)

- Gives info about
  - where?
  - which signal?
  - which type of violation?
- Debugging circuit AND environment

TESTBENCH

- Testbench = behavioral VHDL of "inverse" STG (inputs and outputs switched).
- Use of same procedure as the one generating behavioral VHDL (not written by designer)
- Assumes that the environment is the fastest possible.
- Not complete (like verification), but many errors found this way.

Part 6: Testing

1. What do we know about asynchronous testing?

2. Type of faults and why do we need to test delay faults for "delay-insensitive" circuits

3. Robust path delay fault testing

4. How to achieve high testability:
   extra inputs, full scan, partial scan

5. Test generation in synchronous mode

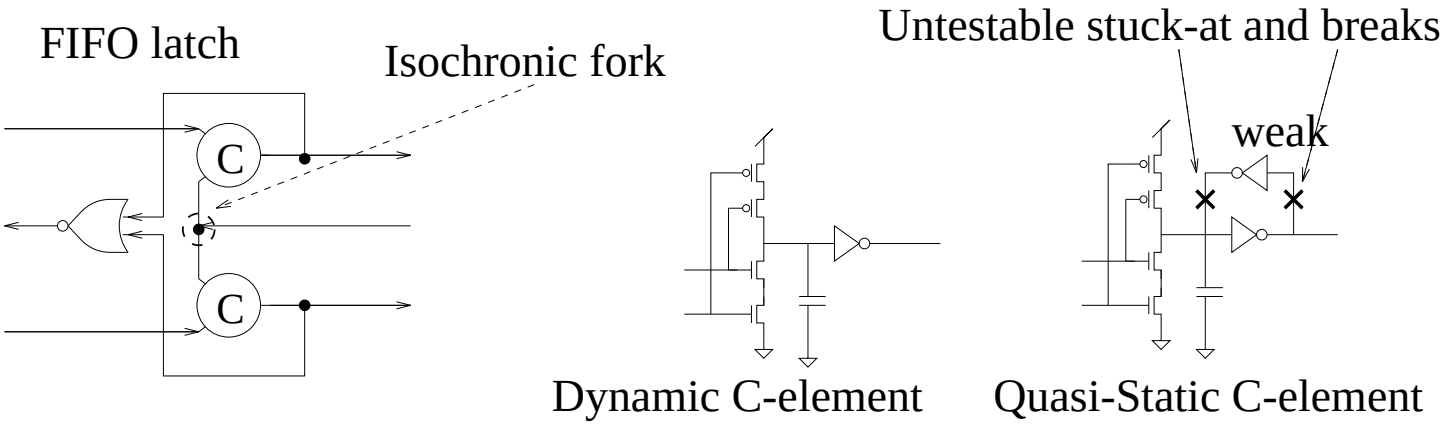
Asynchronous circuit testing (1)

- Traditionally considered *difficult*
- Not much worse than synchronous case if a *systematic design methodology* is followed
- Delay-fault testing is generally required: *correctness only under specific delay hypotheses* (e.g., zero or bounded wire delay, isochronic forks, etc.)

Asynchronous circuit testing (2)

- Speed-independent circuits are self-checking (Armstrong 69, Varshavsky 76, Taubin 80, Beerel 91, ...), but only
  - for *output* stuck-at faults
  - if delay-faults do not invalidate the gate delay model
- Full-scan decomposition-based methodology (Keutzer 91)
- Full-scan phase splitting-based methodology (Lavagno 94)
- Partial-scan of sequential asynchronous nets (Kishinevsky 96)
- Synchronous ATPG for asynchronous circuits (Roig 97)
- Delay-fault testing for the Fundamental mode (Nowick 96)
- Fast test generation for handshake circuits (Roncken 94-96)

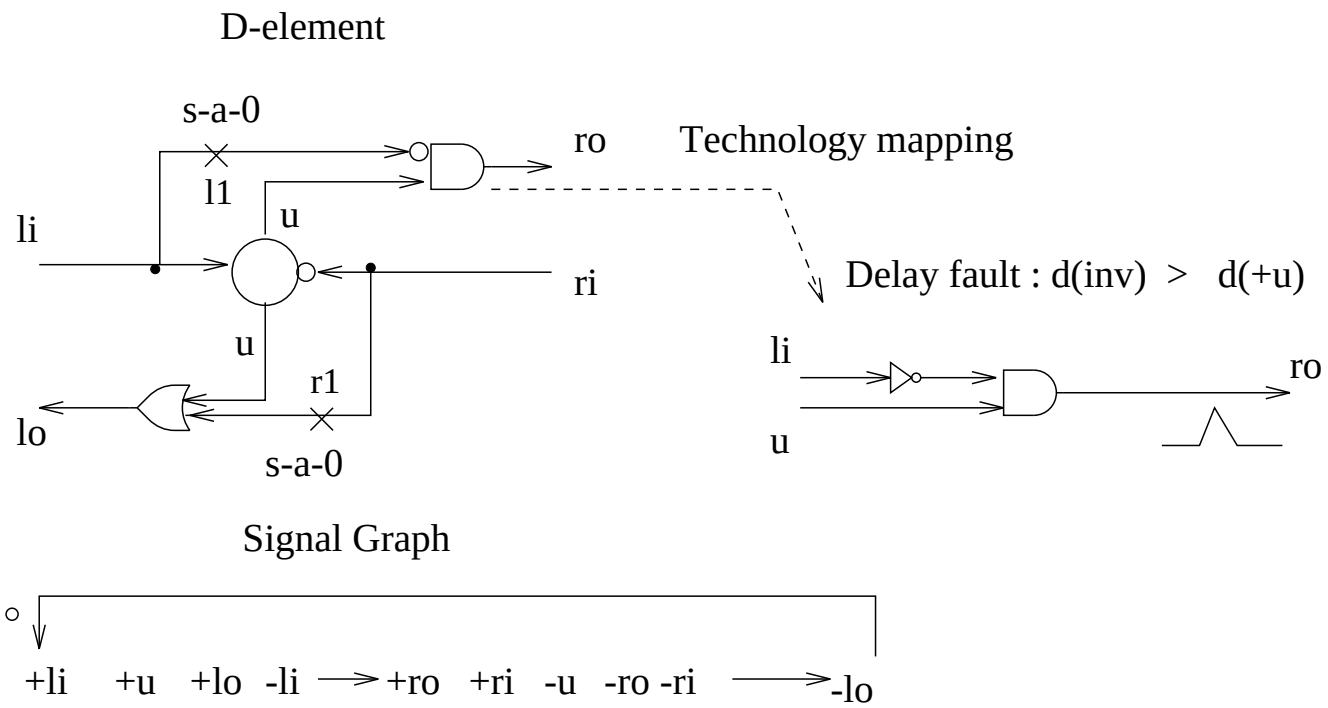
Problem 1: sequential gates



At the gate level: a FIFO latch is *input* stuck-at testable

After any technology mapping – the latch is not stuck-at testable

Problem 2: delay faults within a gate

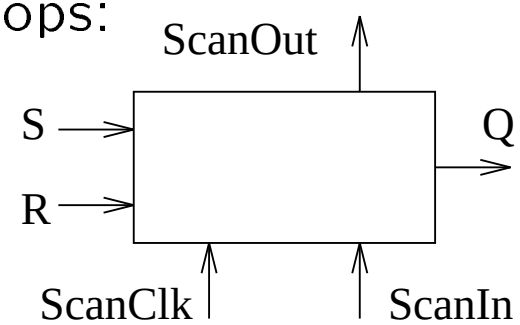


(1) $l1$ stuck-at-0 is a premature fault (Hazewindus, 91):
$+li \rightarrow +u \rightarrow +r0$

(2) A delay-fault of the input inverter may cause hazards

Hazard-free testing vs. operation

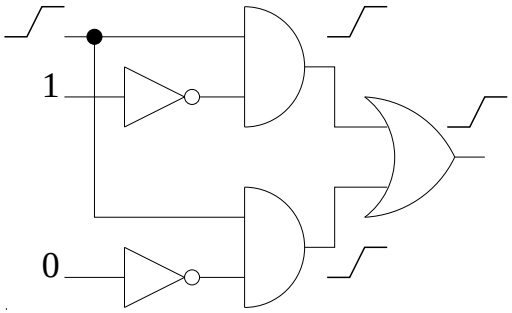
- Hazard-free testing: for each fault:
  - there exists a sequence of vectors that do not cause hazards and test the fault under every timing condition
  - the vectors are produced by scan flip-flops:



- Hazard-free operation: for each vector sequence:
  - that conforms to the circuit specification
  - the sequence cannot cause a hazard under any timing condition

Definitions (1)

- Path: sequence of gates and wires
- Vector pair: pair of value assignments to inputs
- Event: $0 \rightarrow 1$ or $1 \rightarrow 0$ transition on a gate
- Event-sensitizable path: an event can propagate along it
- Robust propagation: independent of other delays

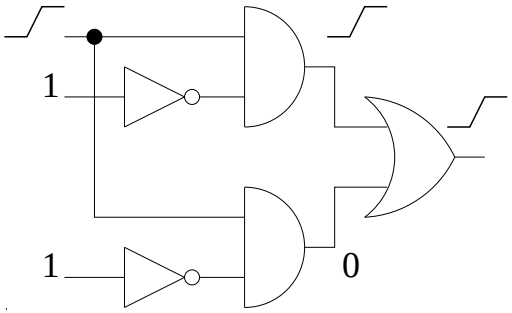


Definitions (2)

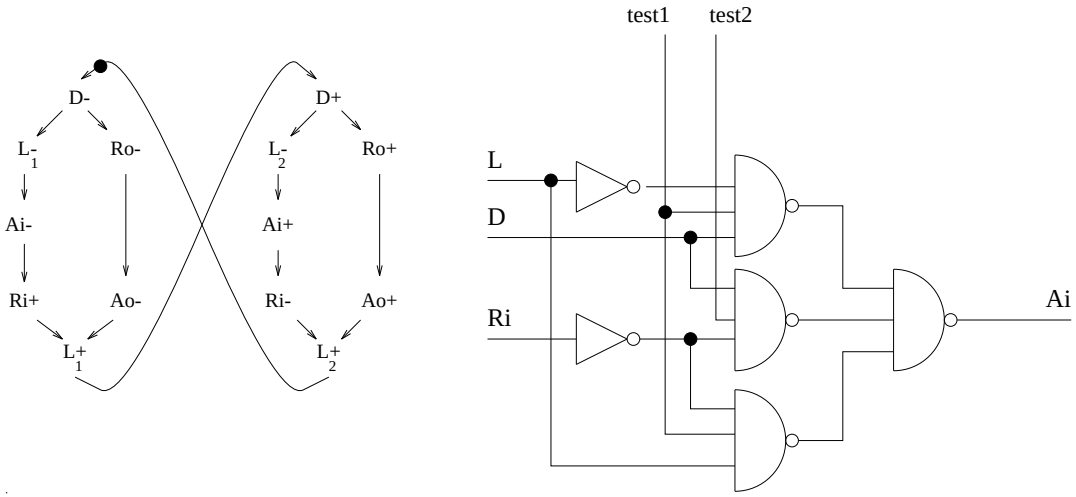
- Path-delay fault: an event is too slow or too fast propagating down the path

- Robust path-delay-fault test: a pair of vectors that robustly propagates an event down the path. Hazards cannot force false positives.

- Hazard-free robust path-delay-fault test: a pair of vectors that robustly and without hazards propagates an event down the path

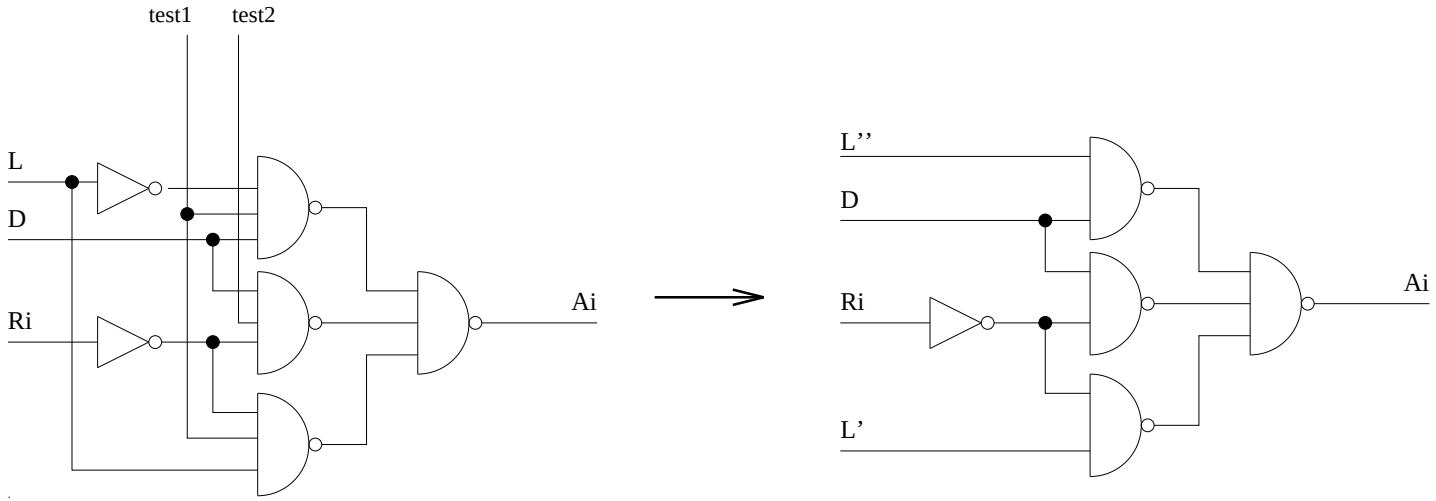


Path delay fault testing with extra test inputs to select paths



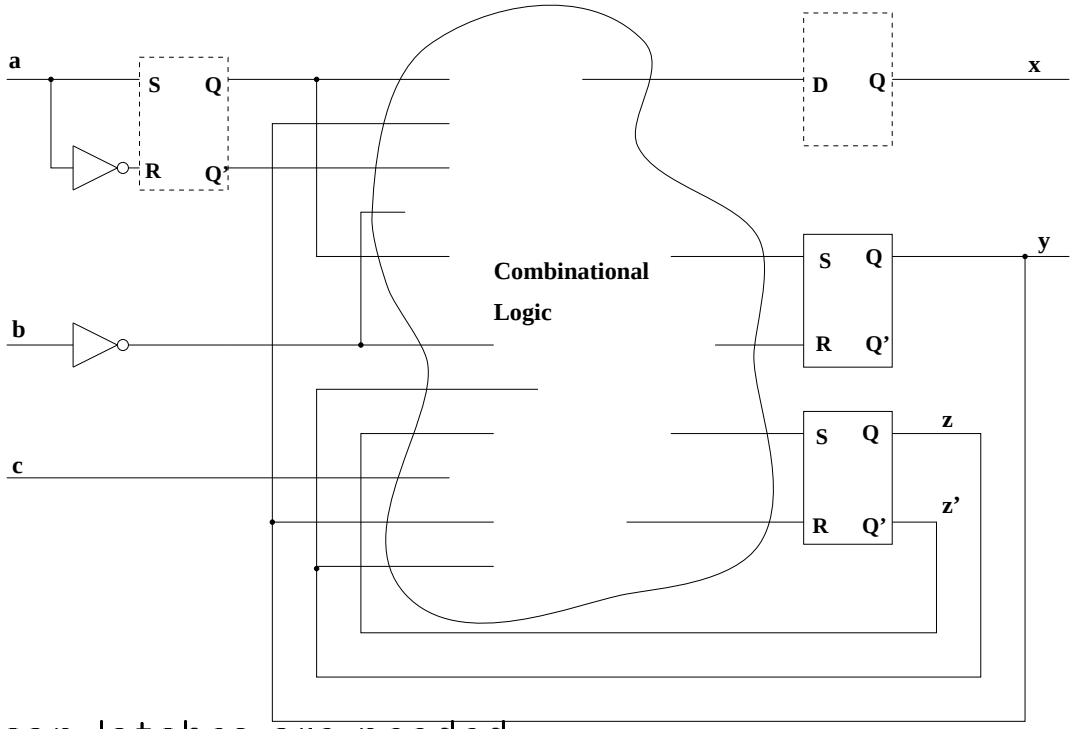
Luciano Lavagno and Kurt Keutzer, 1991
Redundant Boolean function F with binate x: $F = xG + \bar{x}H + R$
Hazard-preserving transformations $\rightarrow$ minimize number of test points

Variable phase splitting



Signal L is splitted into L' and L''.
The cover becames prime and irredundant
Additional testing points are not needed

Circuit architecture and testing strategy

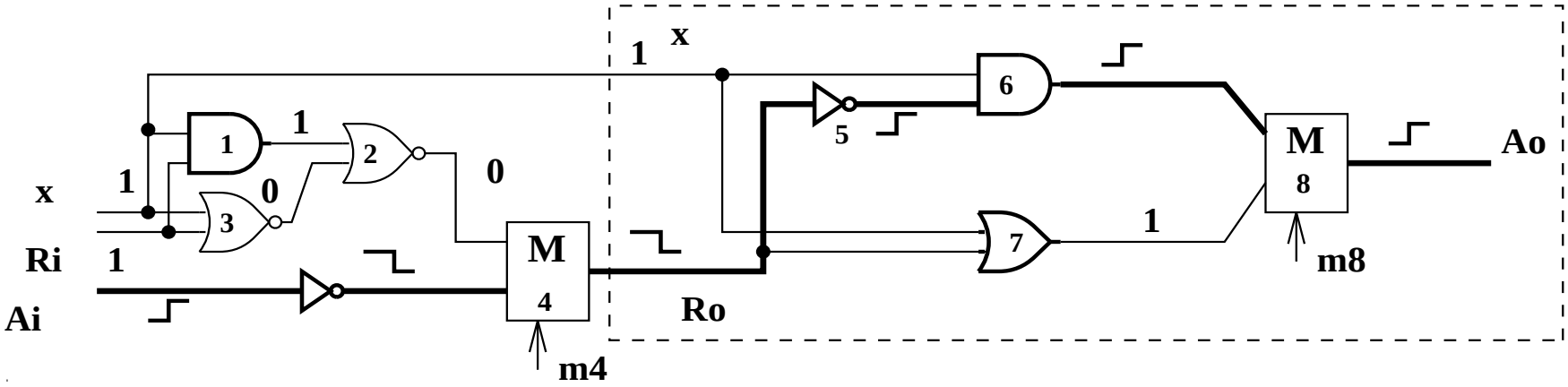


Asynchronous scan latches are needed
Some of binate primary inputs may need to be splitted
Non-observable outputs may require standard scan D-latch

Partial scan based on asynchronous nets

- Asynchronous net: **feedback allowed only inside gates**
- Generalization of combinational circuit
- Can be obtained from asynchronous circuit by cutting global feedback (*partial scan*)
- Two-step procedure:
  1. Initialize all non-scan sequential elements, by means of a *vector sequence*
  2. Test the relevant path(s), by means of a *vector pair*
- Conditions for RPDFT of asynchronous nets can be formulated and checked efficiently by reduction to a combinational synchronous circuit

RPDFT testing of asynchronous nets

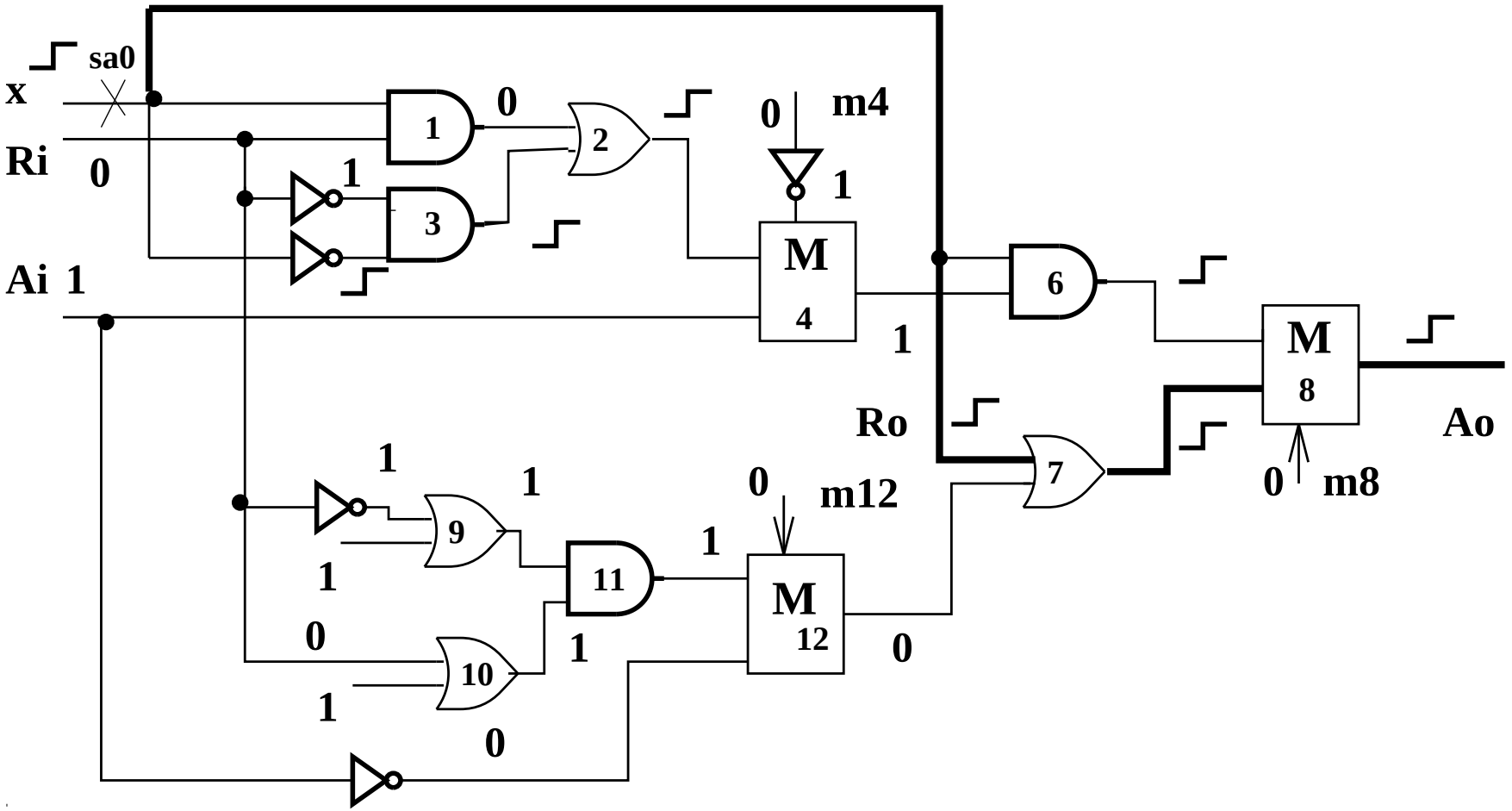


Replace each C element with *majority gate*
(additional input is never used for test generation)

Test pattern generation (1)

- Can be done by using *combinational stuck-at* ATPG techniques
- Transform the net into a *leaf-DAG* (fanout only from primary inputs)
- For rising transition, replace the initial lead of each reconvergent side-input to OR gate by 1
- Find a test for SA-0 on the initial lead
- Forces to find a test that keeps risky reconvergences that may course hazards "shut off"

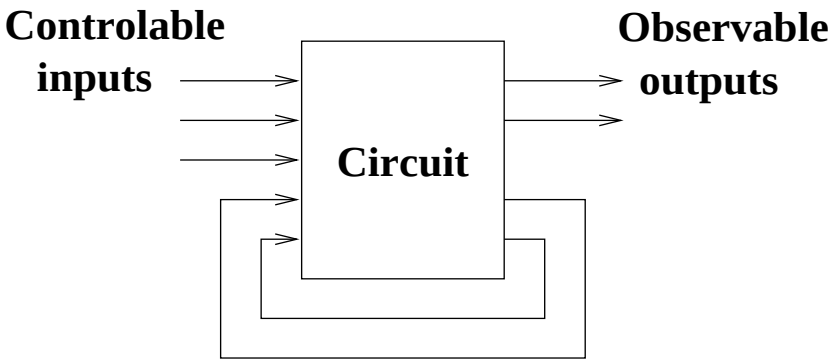
Test pattern generation



Initialization conditions

- (HF)RPDFT is valid only if initialization is consistent with test
- May not be trivial with *partial scan*
- Can always fall back to full scan...
- Classical procedure: unfolding and exhaustive enumeration
- *Monotonous initialization* can often be more efficient

Synchronous test patterns



Strategy for synchronous test:

- Apply input pattern
- Let the circuit stabilize
- Observe outputs

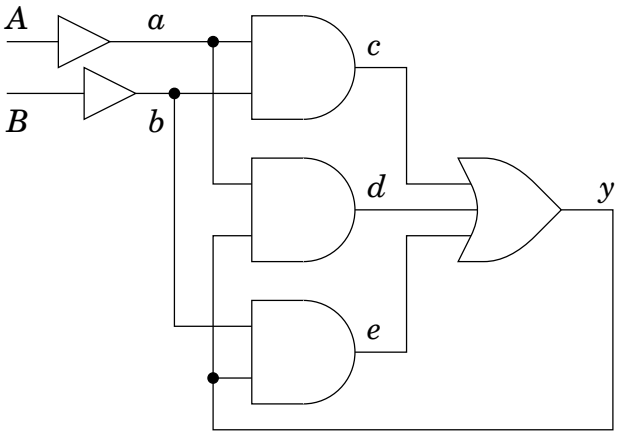
Good news:

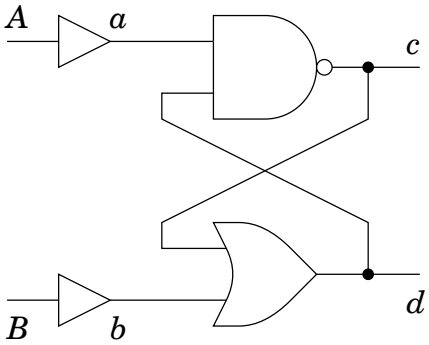
- ATPG techniques for synchronous FSMs can be applied
- SI circuits are almost 100% input stuck-at testable

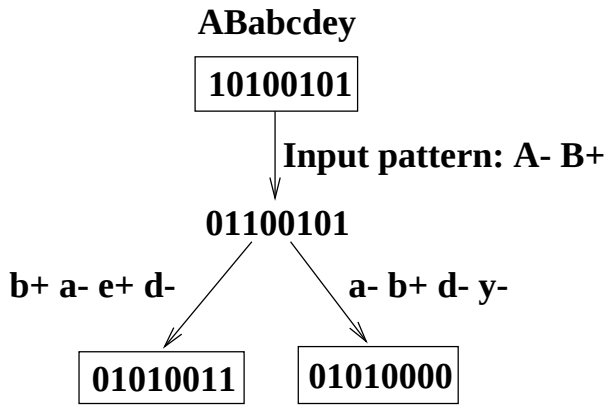
Bad news:

- Not all input patterns can be safely used
- Computationally expensive

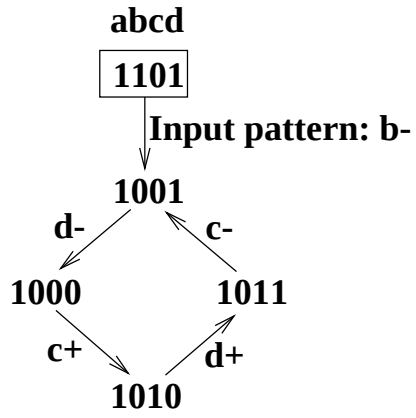
Problems with synchronous test patterns





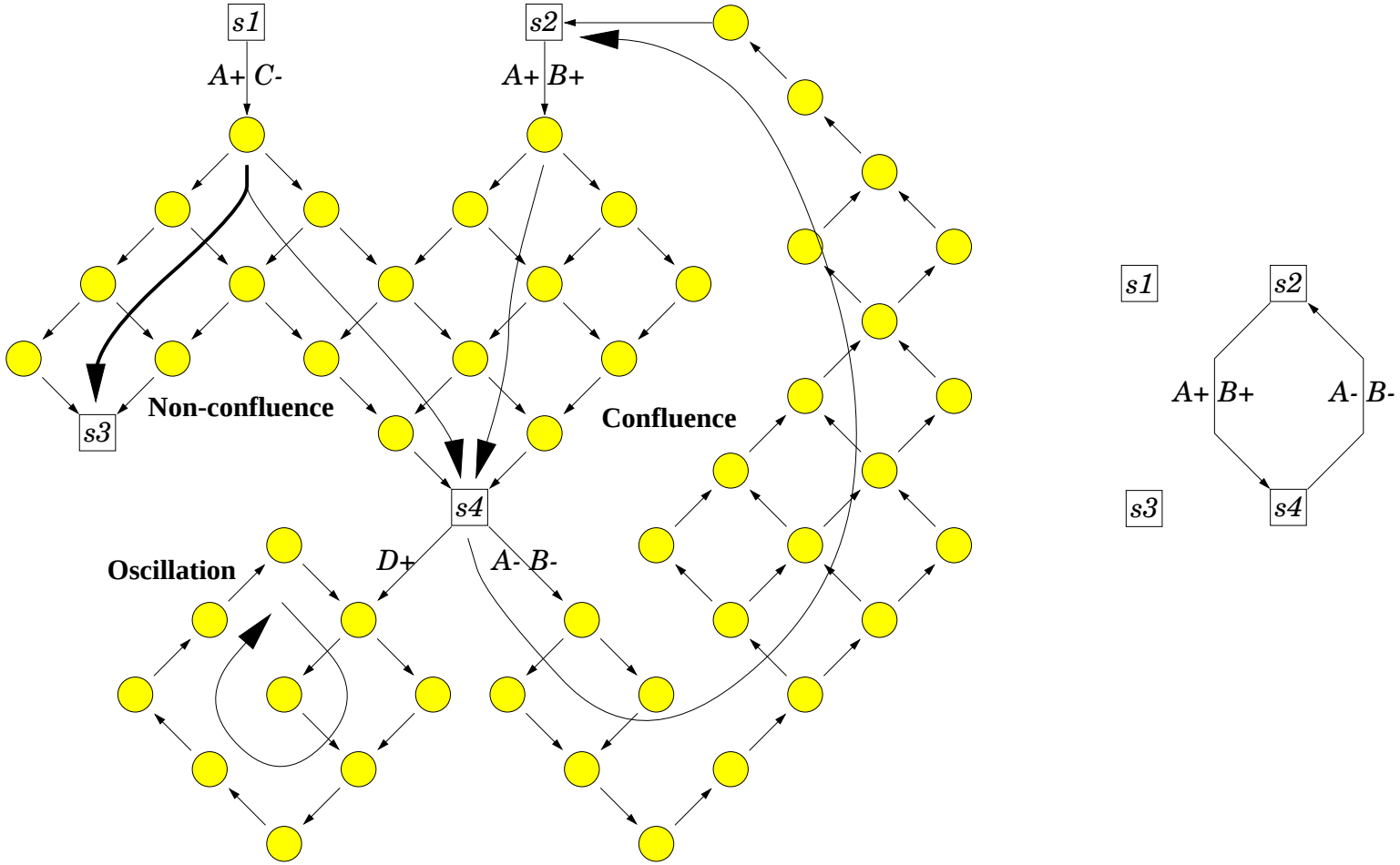


Non-confluence



Oscillation

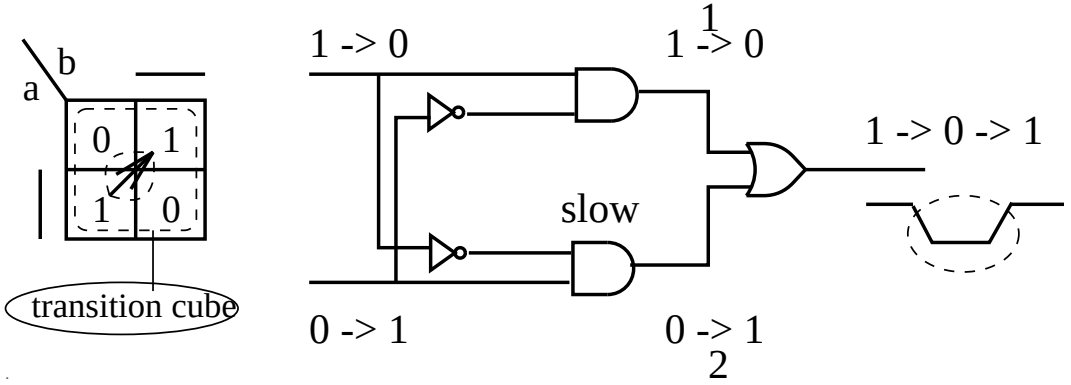
Finding synchronous test patterns



Appendix 1: Hazards and races

- Types of hazards
- Combinational hazards
- Races and sequential hazards
- Hazard elimination
- Modern view on hazards and races

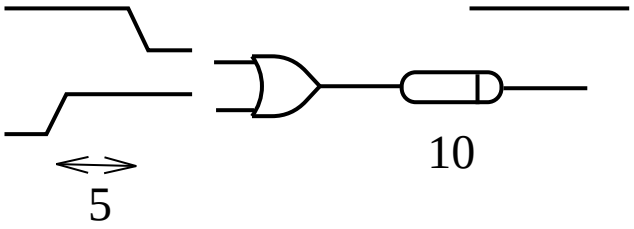
Hazards



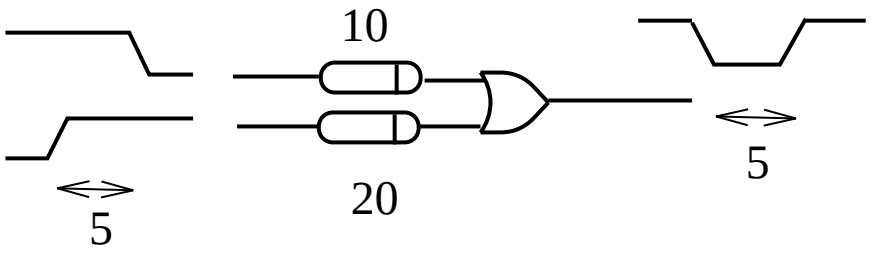
Hazard example:
for $c = a\ xor\ b$

- Hazard: signal transition not specified by the designer
- Hazards make asynchronous design difficult
- Eliminating hazards reduces power dissipation in **synchronous** design [Pedram]
- Theory of hazards: [Unger, Kung, Nowick]

Hazards and delay model



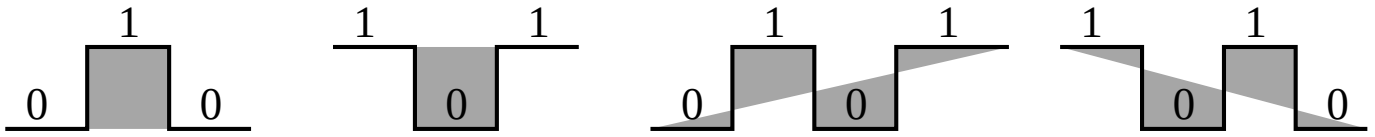
- Inertial gate delay model
  $\Rightarrow$ no hazards



- Wire delay model
  $\Rightarrow$ hazards

Hazard analysis depends on the delay model

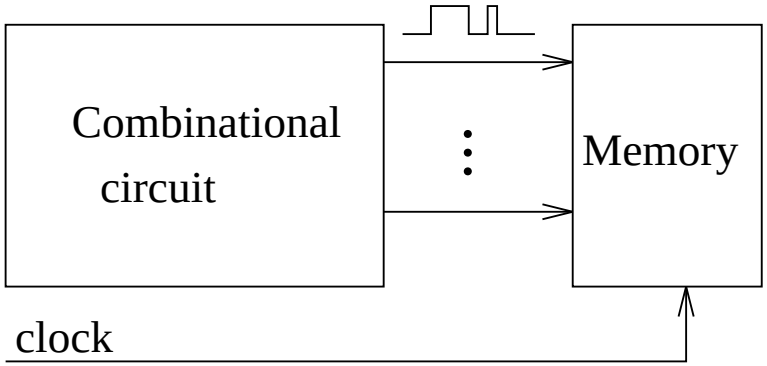
Taxonomy of hazards



Static hazards Dynamic hazards

- **Signal behavior**:
  static (no transition is required)
  or dynamic (monotonous transition is required)
- **Circuit type**:
  combinational (circuits without feedbacks) or
  sequential (circuits with feedbacks)
- **Due to specification or due to implementation**:
  function or logic; essential or not essential
- **Due to the environment behavior**:
  next input transition is applied before the circuit settles

Combinational Hazards. Motivation



Clock arrives **after** combinational outputs settle

Clock period calculation: *propagation + hold + set*

No clock $\Rightarrow$ wrong value can be written in a memory

Combinational hazards

- Function hazards: inherent in the specification of the logic function.

  Condition for 1-hazards: a transition cube contains 0

  Cannot be eliminated by changing the logic

  Each Boolean function of more than one variable has static hazards **for some input transitions** $\Rightarrow$ restrict input changes

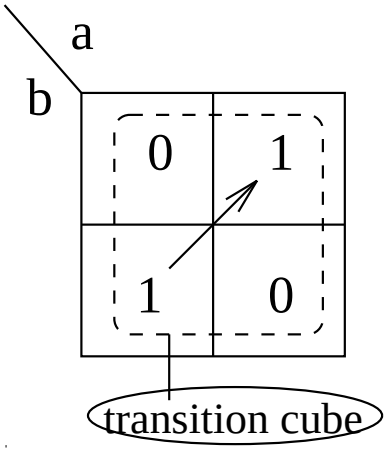
- Logic hazards:
  depend on the particular implementation of the logic function

  Can be eliminated by changing the logic (or sometimes the delays)

Function hazards

- Condition for 1-hazards:
  a transition cube contains 0

- Cannot be avoided by changing the logic

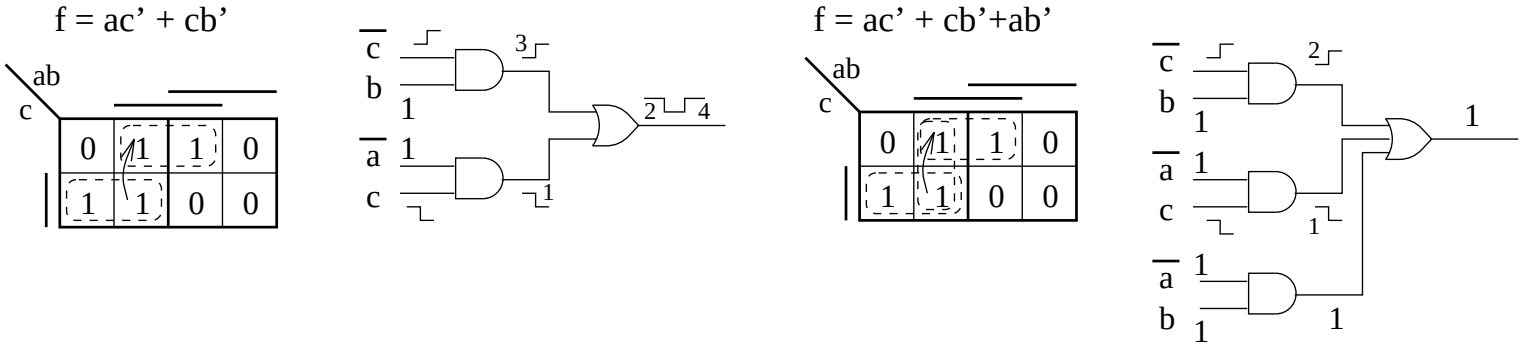


If input changes are not restricted, then
any boolean function of more than one variable has static hazards

Restrict input changes ⇒ – single (SIC)

– multiple (MIC)

Static logic hazard elimination



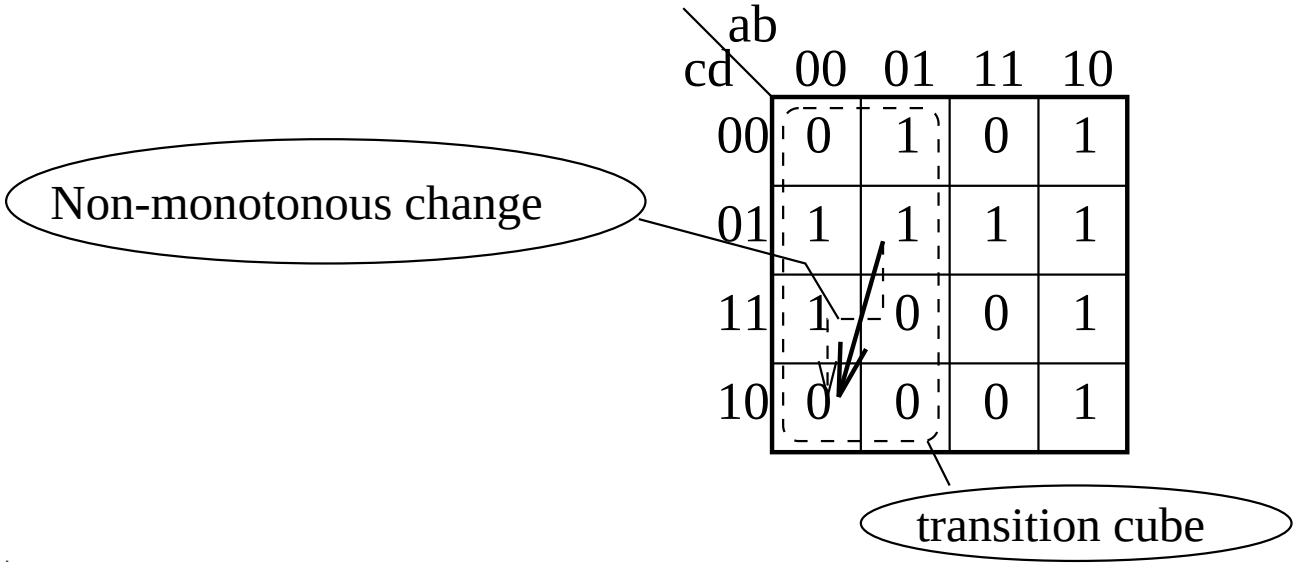
Static hazard: a signal which should remain constant changes

Static logic 1-hazard elimination condition:
each transition cube is contained inside a cube of the cover

A sum of **all** prime implicants is free from static hazards
(for those transitions which are free from function hazards)

Static logic 0-hazards never occur in a two-level Sum-of-products

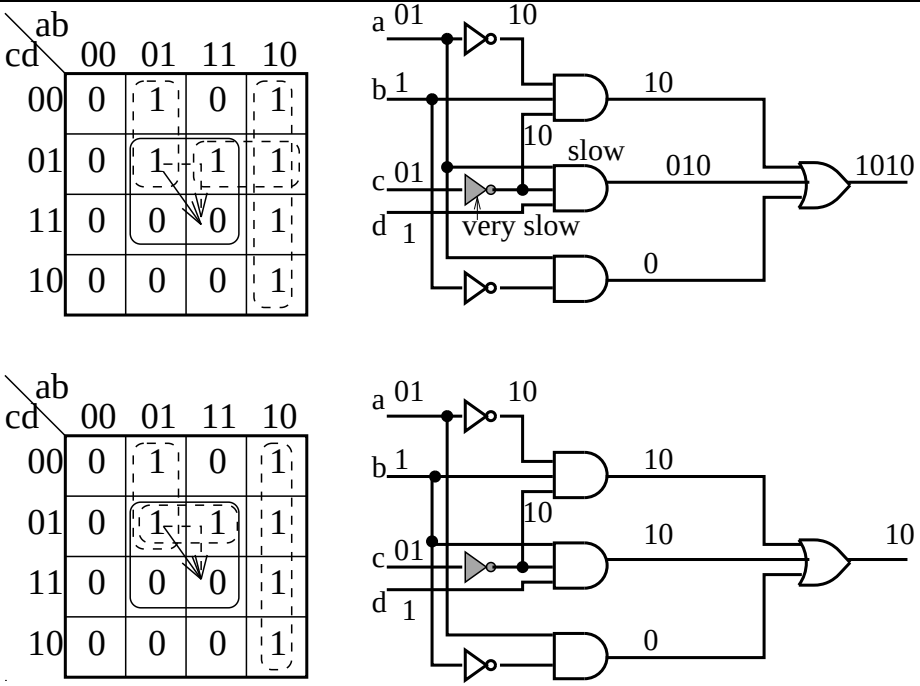
Dynamic function hazards



Dynamic hazard: a signal changes multiple times instead of once

Dynamic function hazard:
non-monotonous change of the function inside the transition cube

Dynamic logic hazard elimination



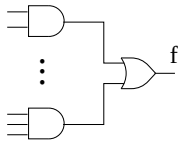
Dynamic logic 1to0-hazard elimination condition:
if transition cube intersects cube c of the cover,
then c contains the *start point* of the transition cube

SOP of **all** prime implicants has no dynamic hazards under **SIC**

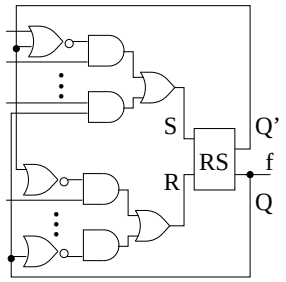
0to1-hazards are symmetrical (the same for the end point)

Hazard-free combinational implementations

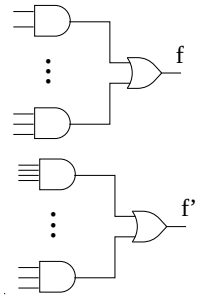
- Eichelberger
  (SOP of primes + SIC)



- Bredeson and Hulina
  (RS-flip-flop + factorization)

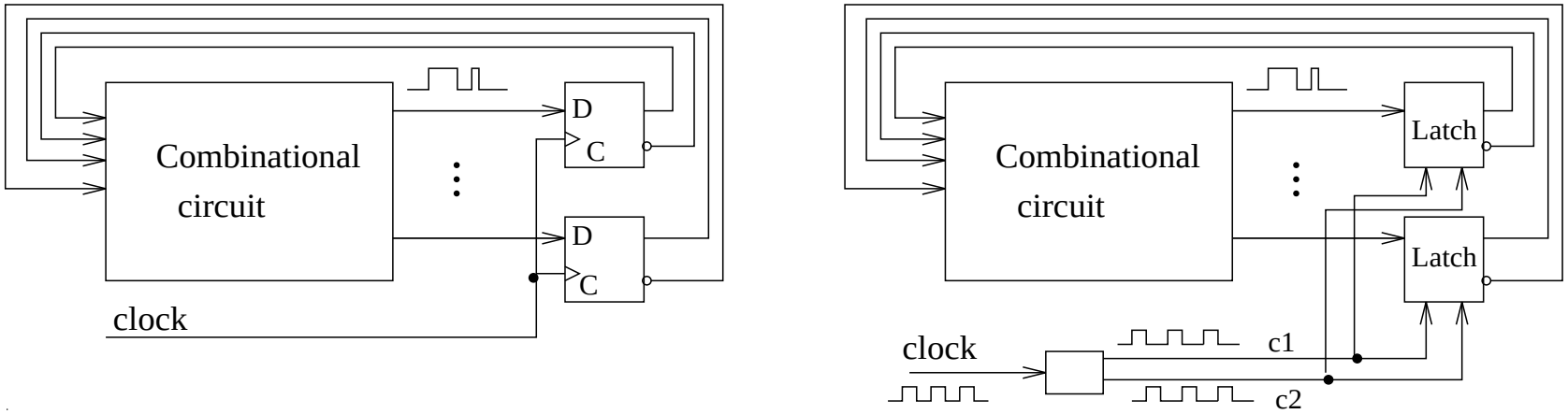


- Two-phase operation
  (f and $\overline{f}$ + spacer)



Sequential circuits

Sequential circuits $\approx$ circuits with feedbacks



In synchronous circuits feedbacks are broken by:

- Edge-triggered flip-flops
- Two-phase nonoverlapping clocks

Sequential hazards

Sequential circuits $\approx$ circuits with feedbacks

Sequential hazards occur because feedbacks propagate new values before the input net completes signal propagation to all inputs of the next state logic

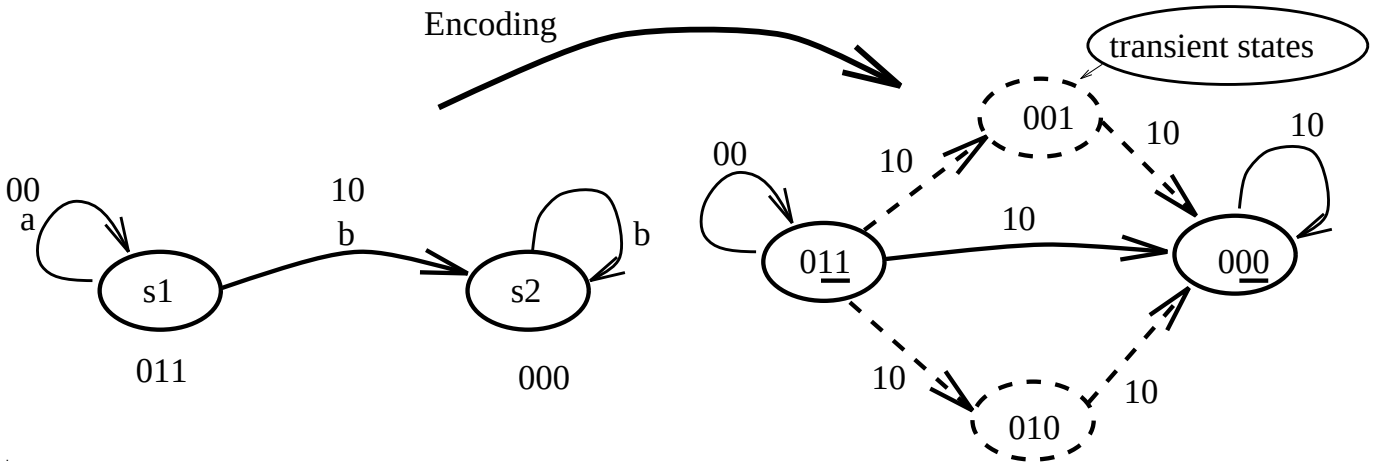
- **Essential hazard**: inherent in the FSM specification.

  cannot be eliminated by another state encoding $\Rightarrow$
  cannot be eliminated for unbounded delays

  can be masked out by controlling the delays

- Non-essential hazards (**races**):
  can be eliminated by a proper state encoding

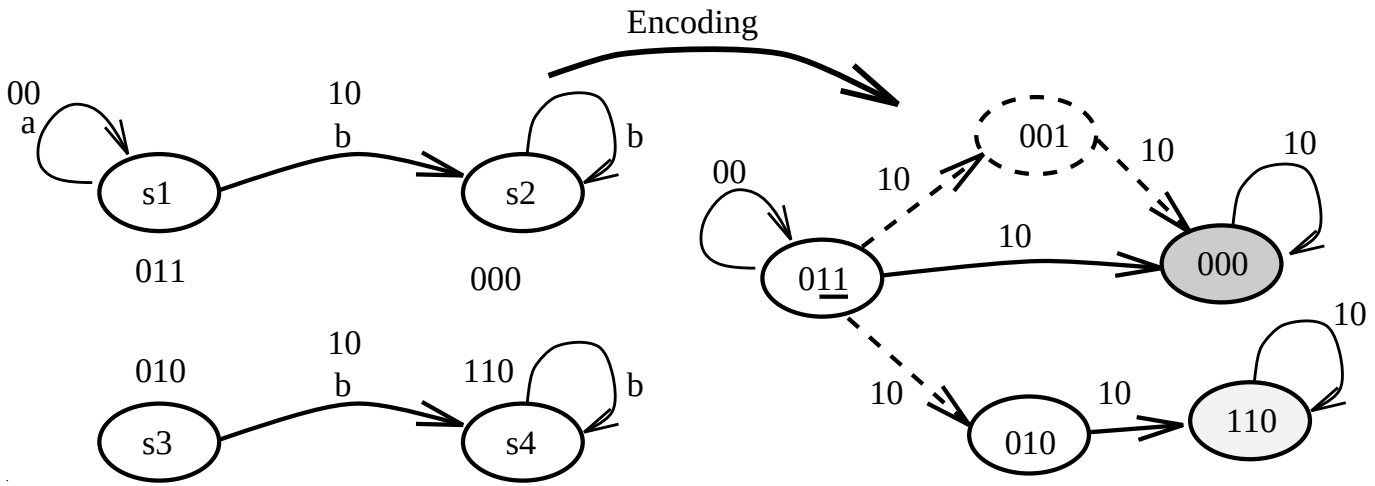
Non-critical races



Race: more than one state signal changes

Non-critical race:
all transient states drive the FSM into the same final state

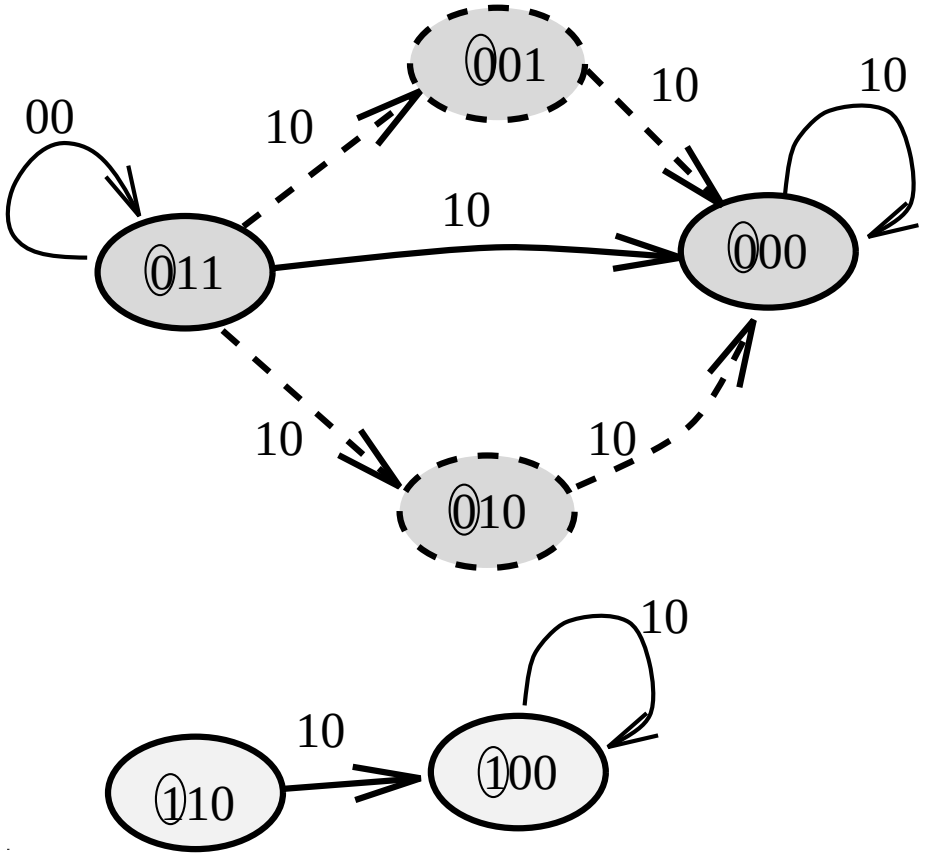
Critical races



Critical race:
different transient states drive the FSM into different final states.

Final state depends on the race winner

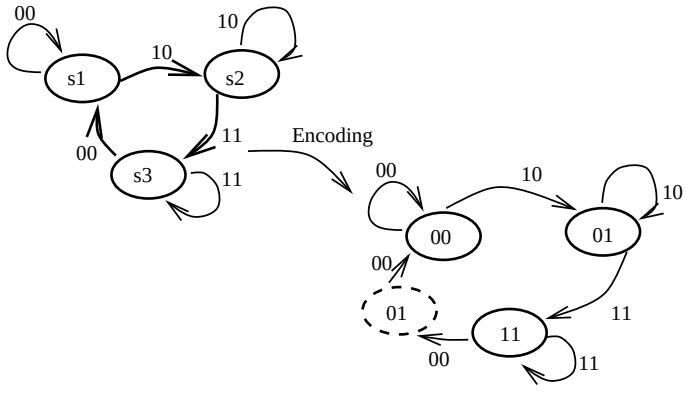
Race-free encoding



Tracey encoding:

Two state transitions under the same input
$s1 \stackrel{b}{\rightarrow} s2$ and $s3 \stackrel{b}{\rightarrow} s4$
must be distinguished by a stable state signal:
$\mathbf{0}11 \stackrel{10}{\rightarrow} \mathbf{0}00$ and $\mathbf{1}10 \stackrel{10}{\rightarrow} \mathbf{1}00$

Types of race-free encoding



- **Single bit change:** simple, bad throughput

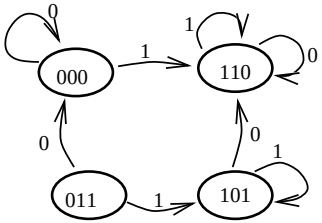
adjacent states differ by exactly one bit
requires few FSM cycles to reach a stable state

Example: one-hot encoding

Single transition:
better throughput, more complex

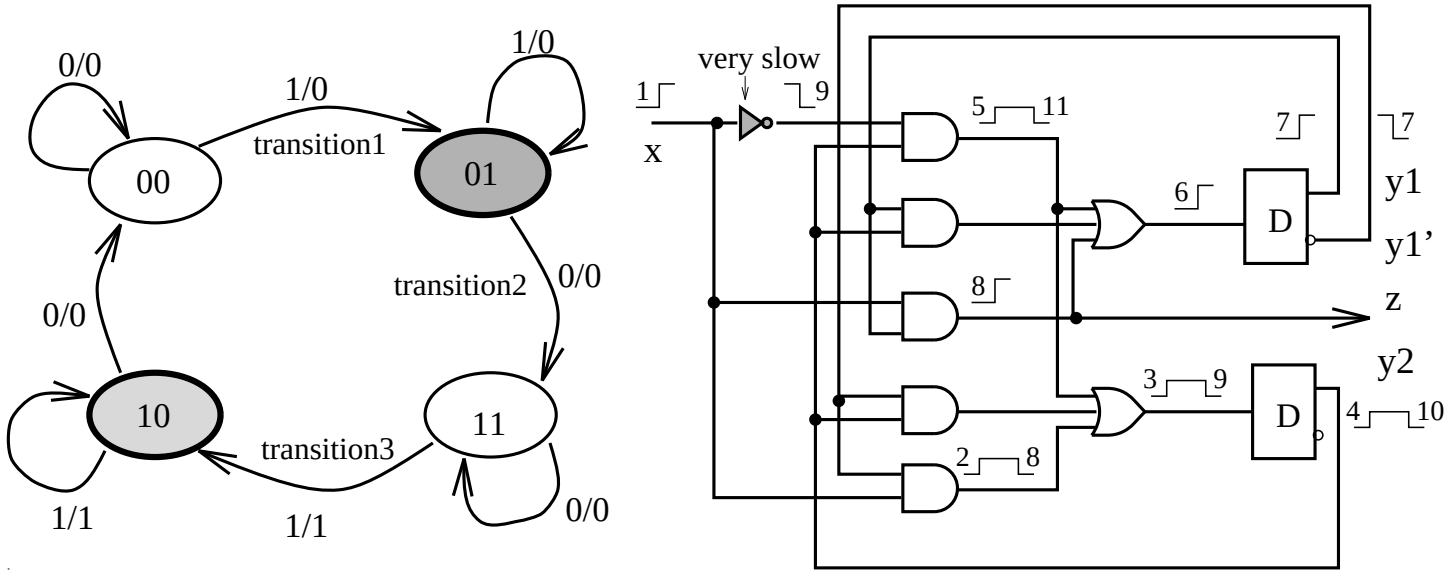
adjacent states may differ by multiple bits
requires one FSM cycle to reach a stable state

Examples: equal distance encoding;
Tracey encoding



Race-free FSMs may still have **essential hazards**

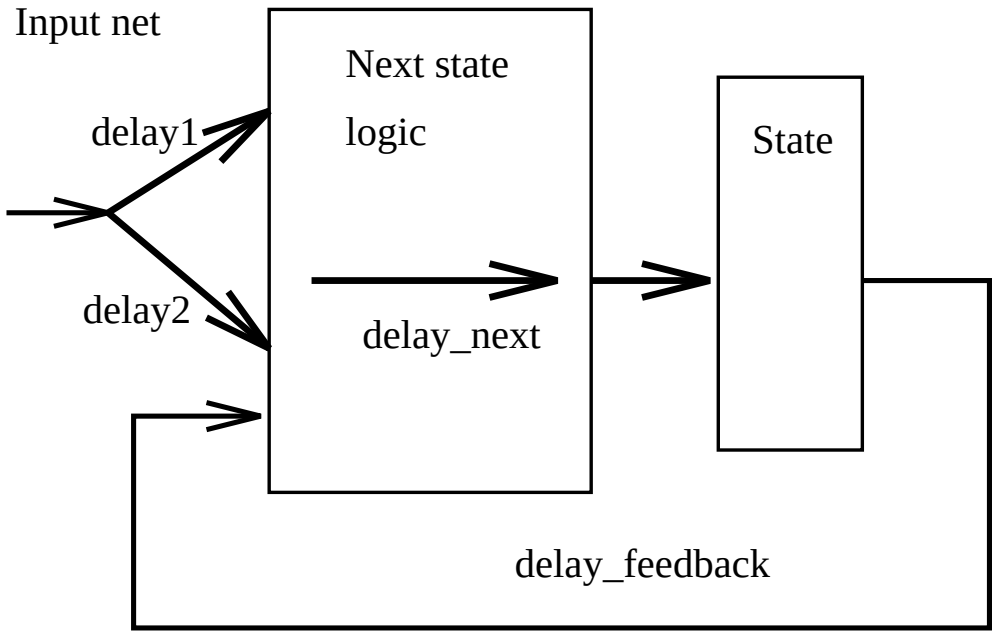
Mod-2 counter: essential hazards



Unger's condition for essential hazards:

state after **three** transitions of an input signal ≠
state after **one** transition of the same input signal

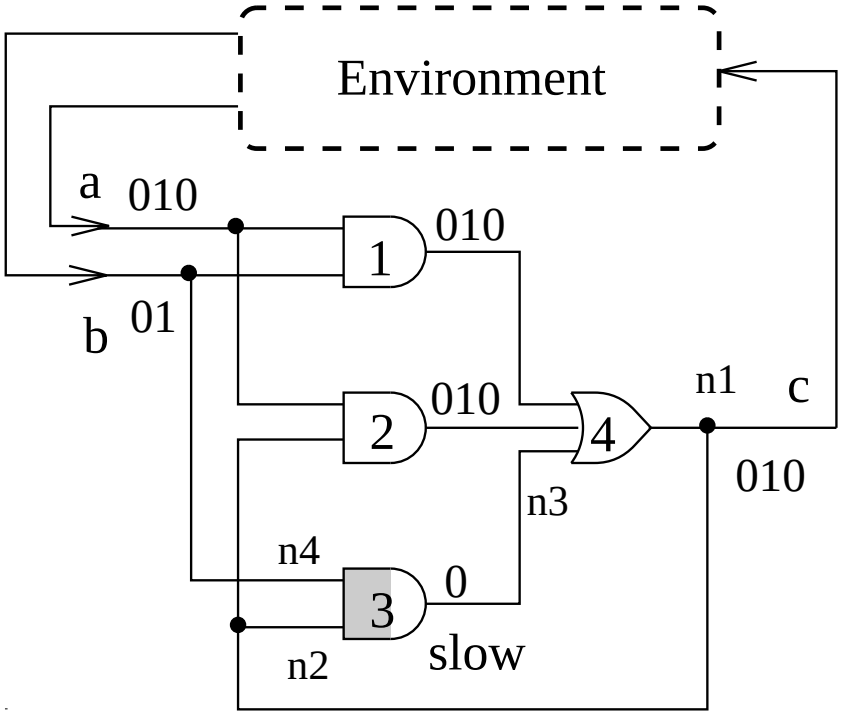
Why essential hazards occur



No essential hazards if and only if
$|delay1 - delay2| < mindelay_{next} + mindelay_{feedback}$

Essential hazards can be removed by controlling the delays

Delay hazards



- I/O-mode:
  input b changes
  after output c, but
  before gate 3 settles
- This is a **delay hazard**

Delay hazards occur in I/O-mode even in designs free from essential hazards

Hazard elimination methods

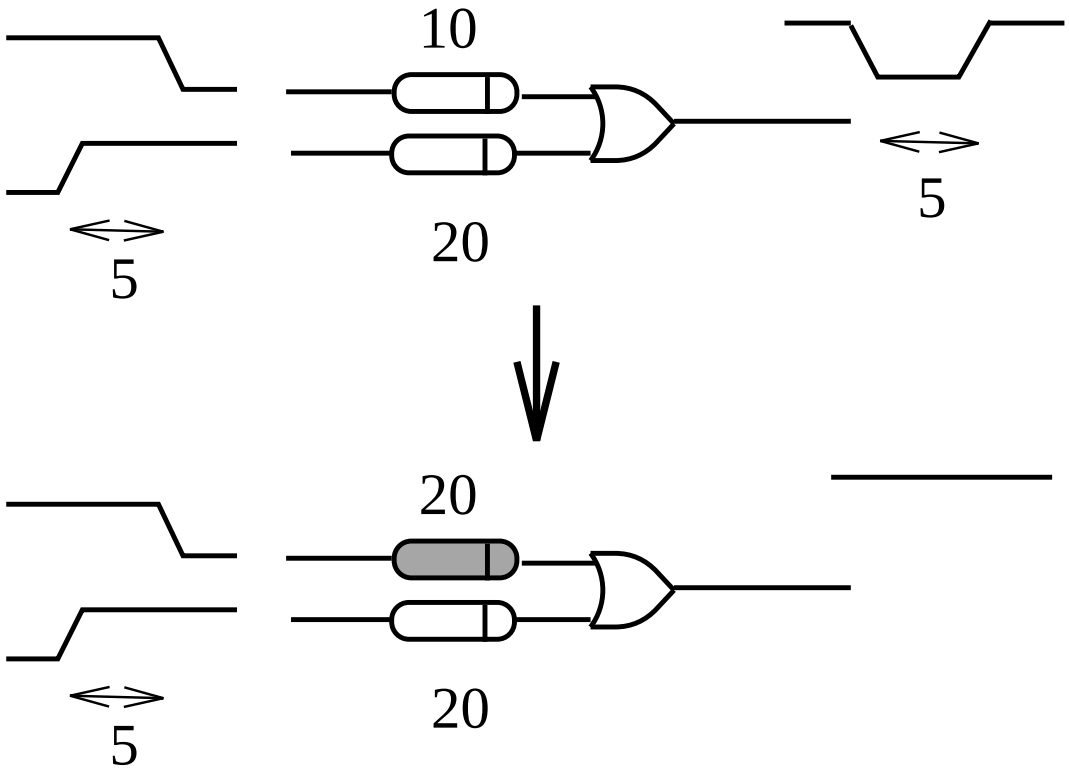
- Changing delays (delay padding).
  Works only for bounded delay model

- Logic transformations (circuit redundancy).
  Works both for bounded and unbounded delay models

- Encoding of inputs and outputs (code redundancy)
  and/or changing allowed input transitions.
  Works both for bounded and unbounded delay models

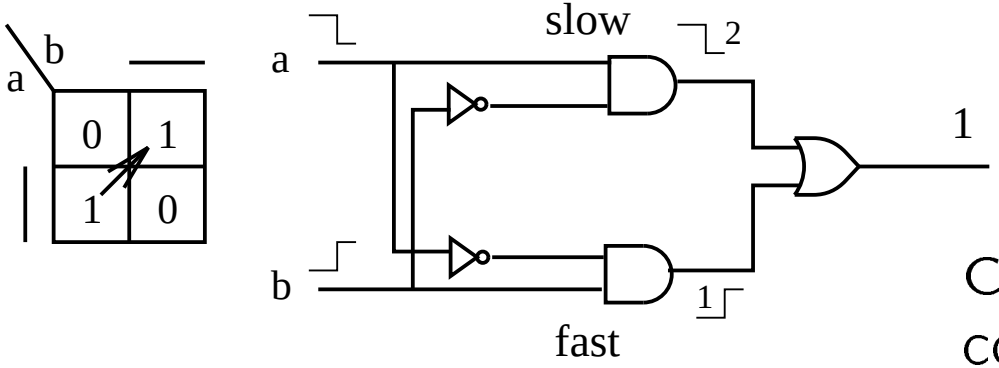
Fighting with hazards always requires some area and time overhead

Masking hazards by delay padding (1)

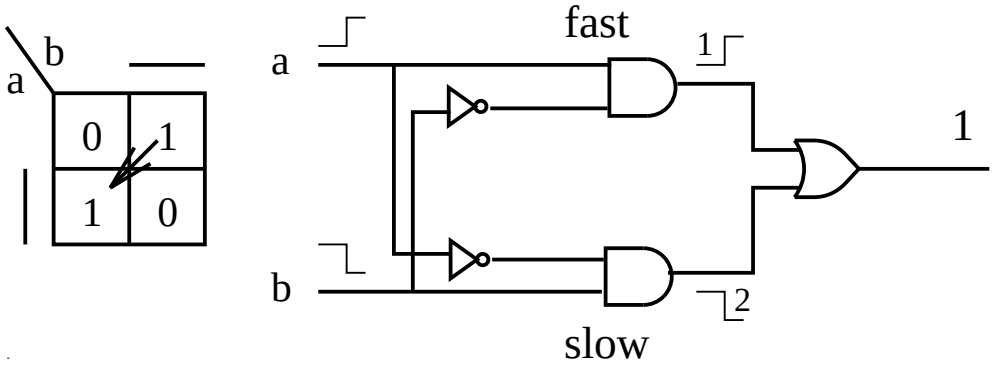


Controlling delays can eliminate hazards

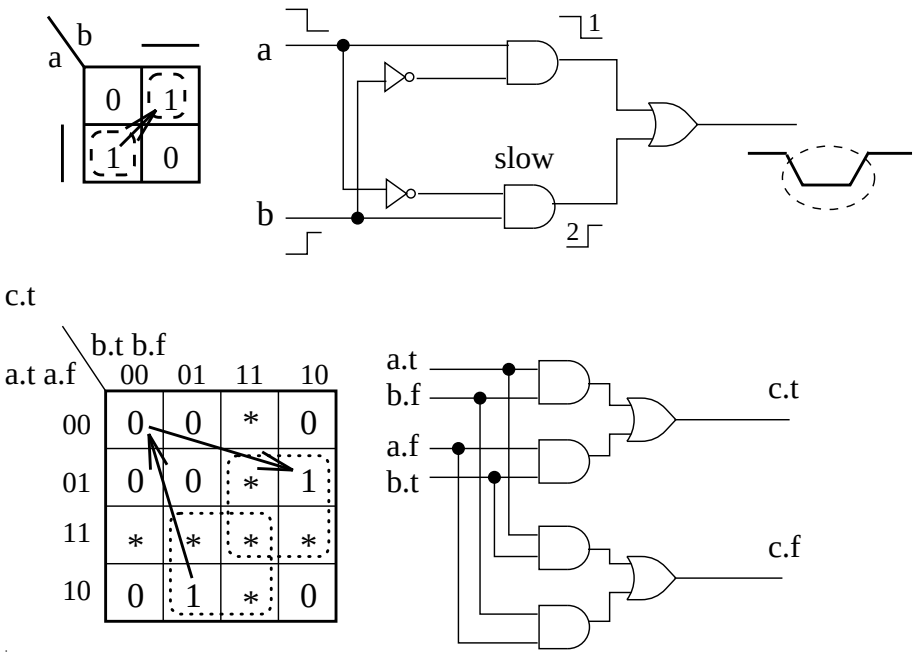
Masking hazards by delay padding (2)



Contradictory constraints $\Rightarrow$
controlling delays cannot
eliminate hazards in general



Hazard elimination by redundant encoding



Dual-rail four-phase XOR-gate

- Function hazards cannot be eliminated by changing the logic $\Rightarrow$ change the *specification*
- Hazards depend on the allowed input transitions: XOR-gate is hazard-free for single input changes
- Redundant encoding of input and output signals and four phase signalling protocol allows to eliminate even **functional** hazards: XOR-gate is hazard-free
  $Valid \rightarrow Empty \rightarrow Valid$

Modern view on hazards and races

Classical hazard/race taxonomy is complex for sequential circuits even in Fundamental Mode.

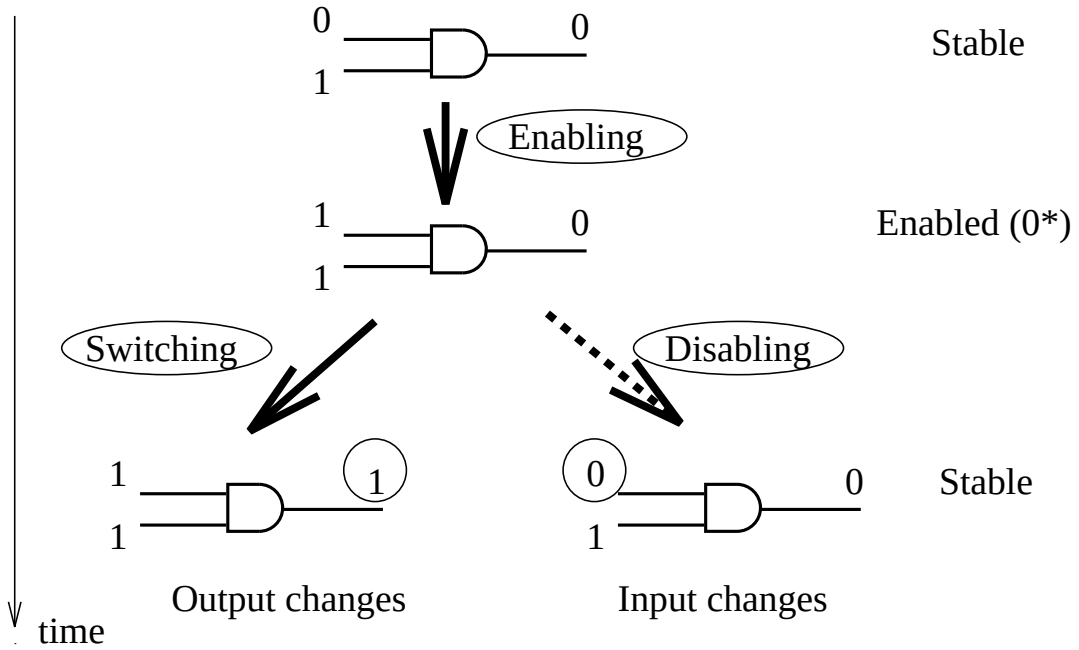
It is much more complex for the I/O-mode:

- Hazards may be viewed as signal transition *disabling*
- Critical races may be viewed as *incomplete* (ambiguous) specifications

Hazard avoidance:
design a circuit in which transition disabling cannot occur

Critical race avoidance:
make the specification complete and unambiguous

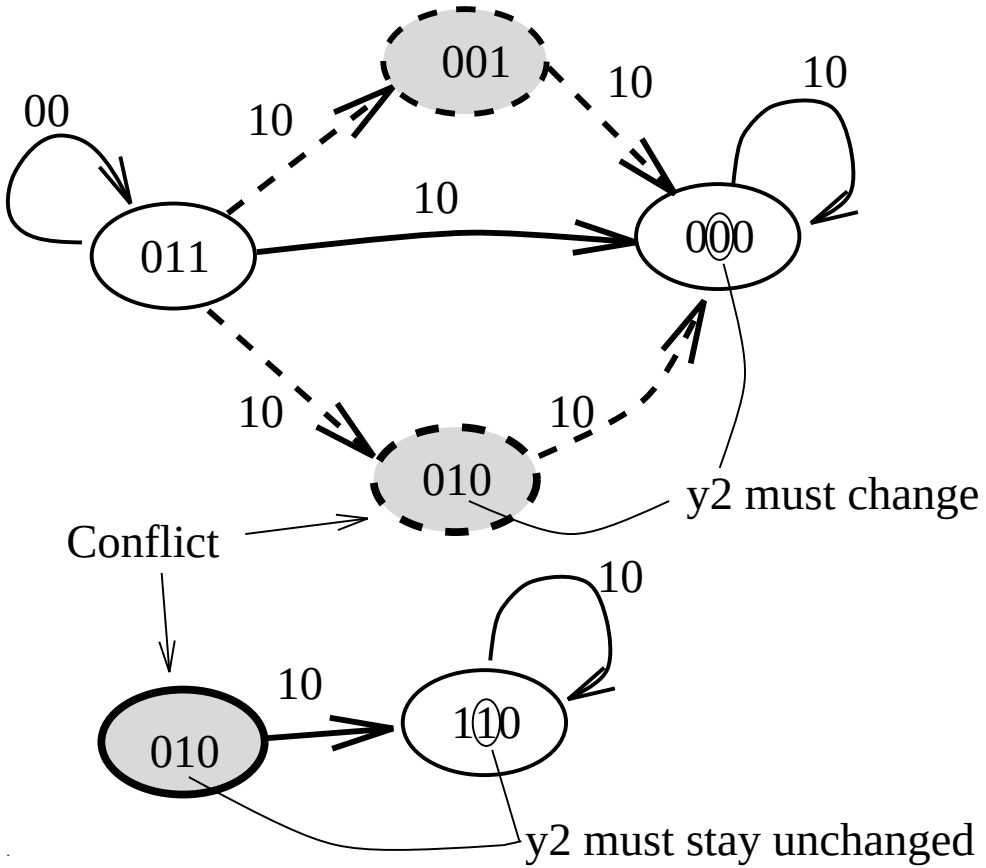
Speed-independent design



For unbounded gate delay model:
Disabling cannot occur $\Rightarrow$ no hazards

No need for a complex theory of hazards for this delay model

Critical races as incomplete state coding

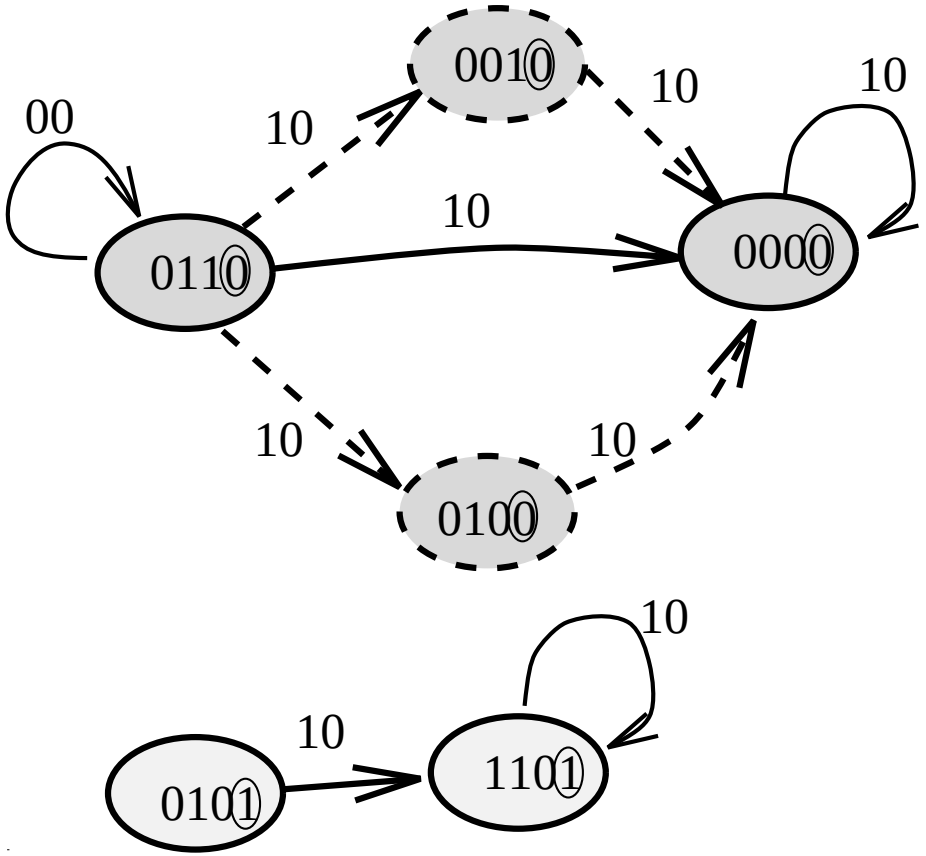


FSM spec is ambiguous, i.e. **incomplete**

State assignment conflict:

$< y1, y2, y3 >$	next state $y2'$
010	0
010	1
...	...

Complete state coding



Solving state assignment **conflicts:**

Add new state signals or

Remove one of the states (by re-encoding, reducing concurrency)

Appendix 2: Review of other methods of synthesis

- CSP-based approach [Martin,Burns,et al]
- Burst Mode finite state machines [Davis et al,Nowick,Yun,Dill]

Other specification models. CSP

- CSP = communicating sequential processes.
- Concurrent processes communicating by input and output commands on channels.
- Semantics are based on trace theory. [Udding, van de Snepscheut, Rem]
- In general, techniques try to come up with quasi-delay-insensitive implementations
- Two main approaches: Production rule based [Martin, ...] and Syntax-directed decomposition [Ebergen, Berkel]

CSP PROGRAM

$$*[[l_i]; r_o\uparrow; [r_i]; r_o\downarrow; [\neg r_i]; l_o\uparrow; [\neg l_i]; l_o\downarrow]$$

- ";" = sequencing.
- $r_0\uparrow$ = r_0 goes high, $r_0\downarrow$ r_0 goes low.
- $[l_i]$ = wait until l_i is high, $[\neg l_i]$ wait until l_i is low.
- Program meaning: l_i has to be high before r_0 goes high. The circuit will wait until r_i goes high, before r_0 will go low again and so on ....

Production rules and CSP programs

CSP program

$$[[l_i]; r_o\uparrow; [r_i]; r_o\downarrow; [\neg r_i]; l_o\uparrow; [\neg l_i]; l_o\downarrow]$$

Production rules

$$\begin{aligned} l_i &\mapsto r_o\uparrow \\ r_i &\mapsto r_o\downarrow \\ \neg r_i &\mapsto l_o\uparrow \\ \neg l_i &\mapsto l_o\downarrow \end{aligned}$$

- ";" = sequencing.
- $[l_i]$ = wait
- production rule = boolean condition $\mapsto$ transition.
- $l_i \mapsto r_o\uparrow$: when l_i is high, r_o will go high.
- $\neg r_i \mapsto l_o\uparrow$: when r_i is low, l_o will go high.
- conflict: $r_o\uparrow$ and $r_o\downarrow$ are not mutually exclusive.

Elimination of conflict

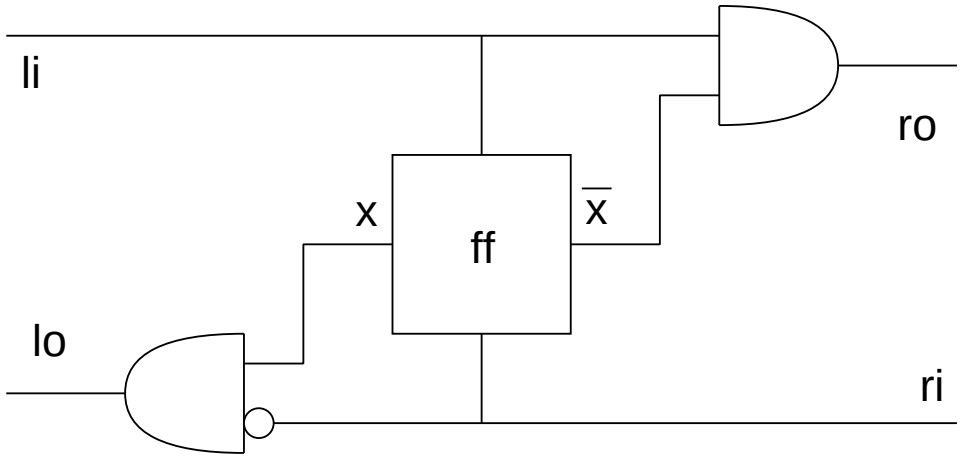
- Add a state signal to solve conflict:

$$*[[l_i]; r_o\uparrow; [r_i]; x\uparrow; [x]; r_o\downarrow; [\neg r_i]; l_o\uparrow; [\neg l_i]; x\downarrow; [\neg x]; l_o\downarrow]$$

- The new production rules:

$$\begin{aligned} \neg x \ \wedge \ l_i &\mapsto r_o\uparrow \\ r_i &\mapsto x\uparrow \\ x &\mapsto r_o\downarrow \\ x \ \wedge \ \neg r_i &\mapsto l_o\uparrow \\ \neg l_i &\mapsto x\downarrow \\ \neg x &\mapsto l_o\downarrow \end{aligned}$$

IMPLEMENTATION

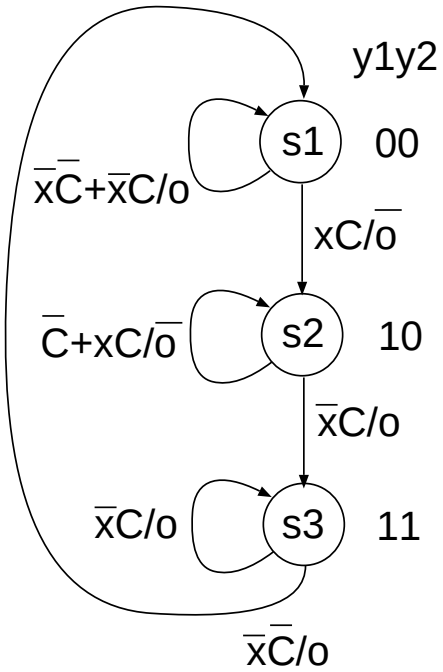


- The production rules can now be identified with operations.

- r_0 maps to an and-gate ($r_0 = \overline{x} l_i$).

$$\neg x \ \wedge \ l_i \mapsto r_o \uparrow$$
$$x \mapsto r_o \downarrow$$

FSM

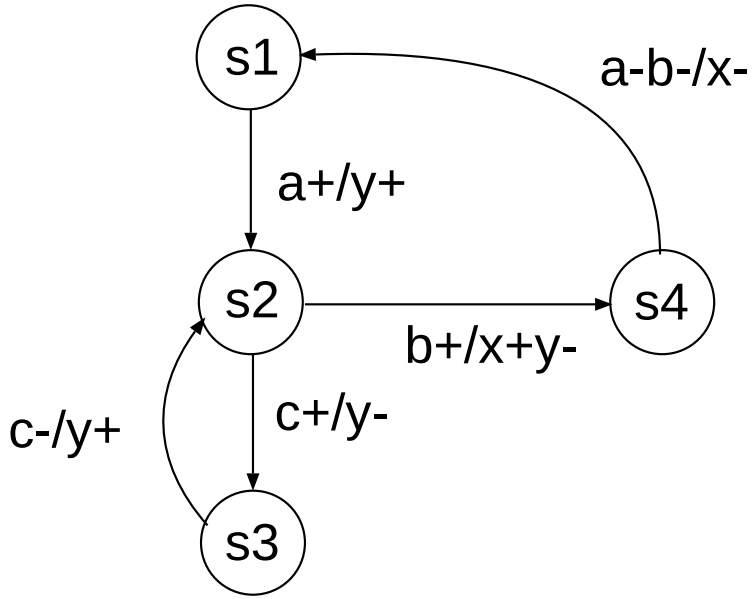

y1y2
s1
00
$\bar{x}\bar{C}+\bar{x}C/o$
$xC/\bar{o}$
s2
10
$\bar{C}+xC/\bar{o}$
$\bar{x}C/o$
s3
11
$\bar{x}C/o$
$\bar{x}\bar{C}/o$

FSM(2)

- Nodes = states, arcs = state transition
- Each arc is labeled with a pair of $input/output$ symbols.
- $input$ = condition for state transition to take place.
- $output$ = values for output signals after the state transition.
- Mostly limited to fundamental mode [Unger].

BURST MODE FSM

- Input transitions fire.
- Output transitions fire.
- State signals change.



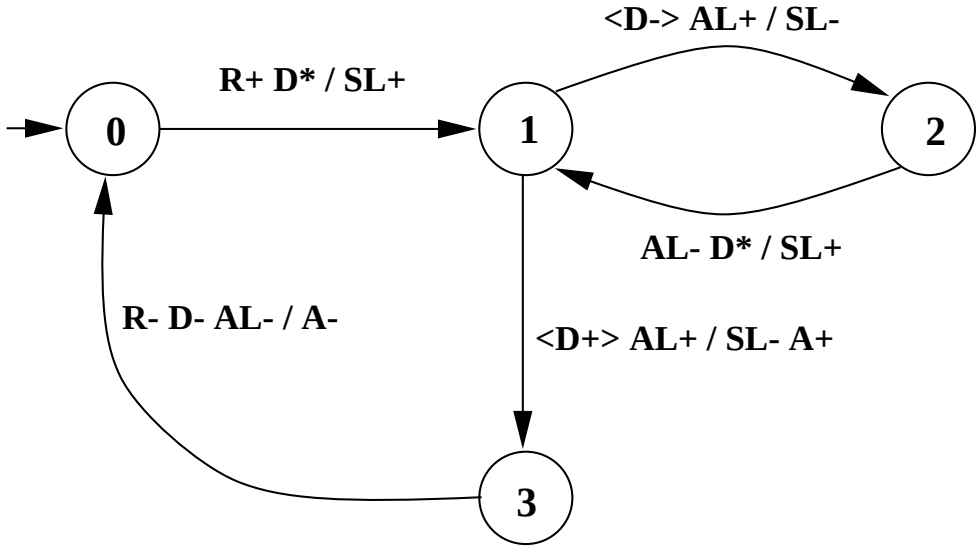
Main features of burst mode FSM

- Mostly limited to fundamental mode [Unger]
- Constrained state minimization [Nowick, Yun]
- Exact minimization for hazard-free logic [Nowick]
- Standard tools can be used under the new constraints

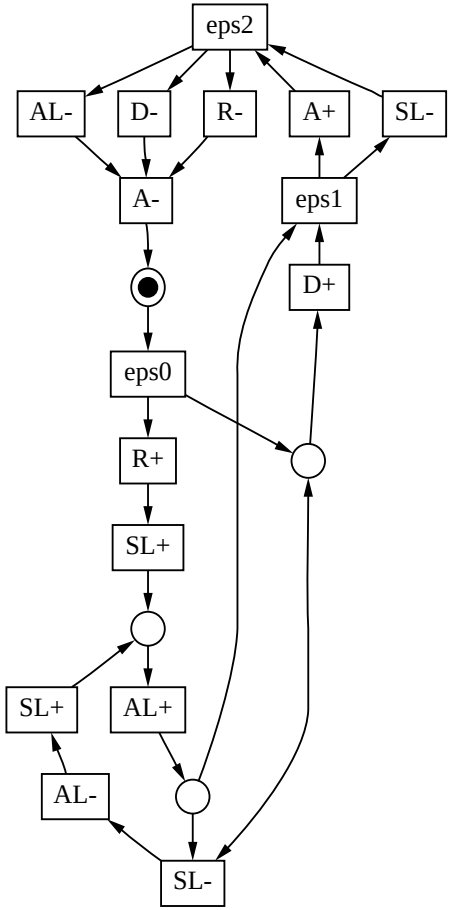
Extended Burst Mode FSM

- Directed don't cares ($a*$): some concurrency between inputs and outputs is allowed for input transitions which do not influence an output burst
- Conditionals: control flow depends on the levels (not the edges) of conditional signals
- Every XBM can be represented by an equivalent STG
- See [Yun94] for details

XBM and STG. Example



$D*$ is a directed don't care
(only monotonous changes are allowed)
$< D- >$ is a conditional guard = "if D=0 then ...."



Restrictions on XBM specification

1. Conditional signals cannot serve as edge signals

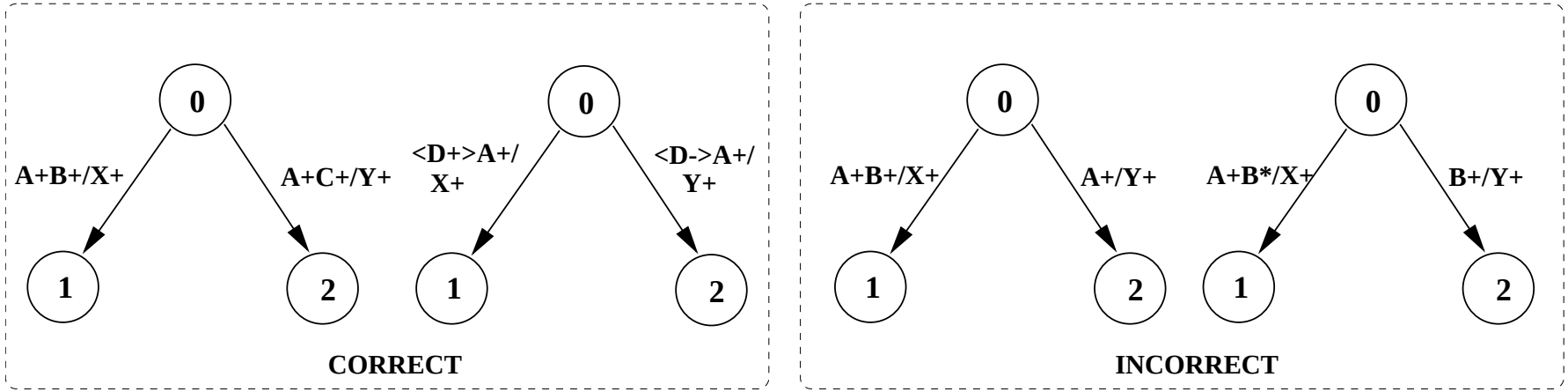
2. Compulsory edge transition must be present at every input burst
   Compulsory = must appear during the state transition it labels, not before.

3. Setup/hold constraints for changes of conditional signals:
   stay stable during $[First\_edge - setup, Last\_edge + hold]$

4. Input bursts must be distinguishable

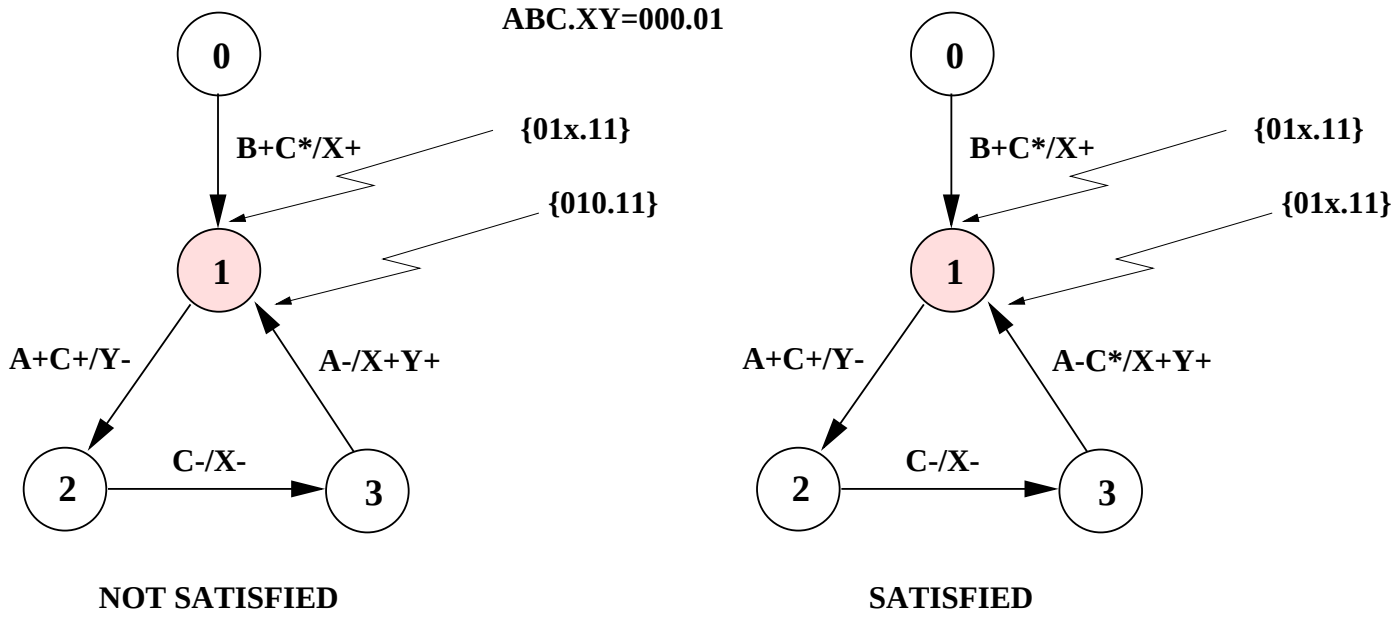
5. Each state satisfies unique entry point condition

Distinguishability of input bursts



Distinguishability = one burst is not a subset of another (including conditionals)

Unique entry condition



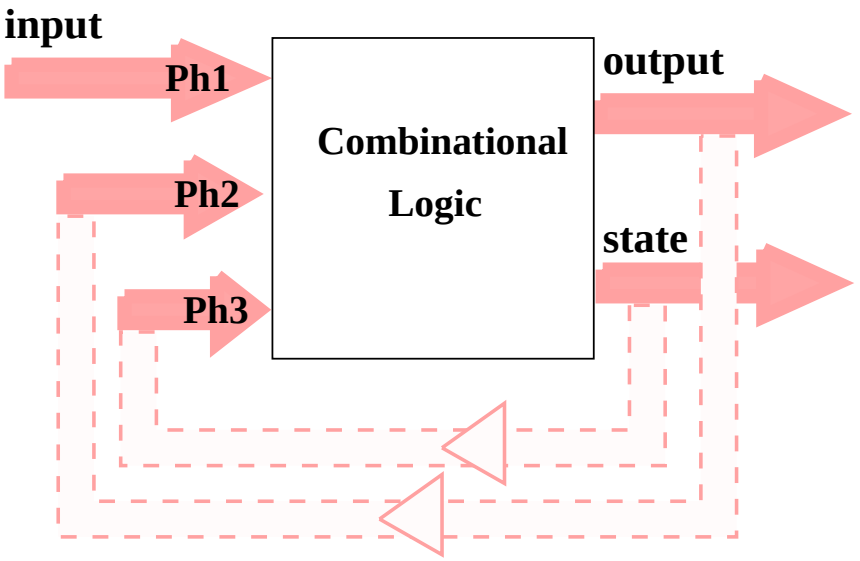
The set of input and output values is the same for any input arc of a state

This condition can always be satisfied by splitting states

Structure of the 3D XBM implementation

Three types of cycles:

- input burst $\Rightarrow$
  output burst $||$ state burst
- input burst $\Rightarrow$
  output burst $\Rightarrow$ state burst
- input burst $\Rightarrow$
  state burst $\Rightarrow$ output burst
- choice depends on type of combinational logic used (to avoid hazards) and on the required level of concurrency



Reduction of XBM to combinational logic

- Specify logic functions free of *function* hazards
- Implement logic functions free of *logic* hazards
- Ensure that sequential feedbacks do not introduce new hazards

Sequential hazards in XBM

- Constraints on the environment:
  - Fundamental mode constraints: no compulsory transitions of the next input burst may arrive before the machine is stabilized
  - Halt/setup constraints for conditional signals
- Constraints on feedbacks = Fundamental mode for feedbacks:
  - To avoid essential hazards (recall the Mod2-counter example) check that feedbacks are slow enough. If not, insert delays.
  - If the structure of the combinational logic is fixed (2-level SOP), then use sufficient constraints like, e.g.,:

    $t^{min}_{comb.logic} + t^{min}_{feedback} > T^{max}_{inverter+input\,wire}$
- Constraints on state encoding: use race-free encoding for state signals

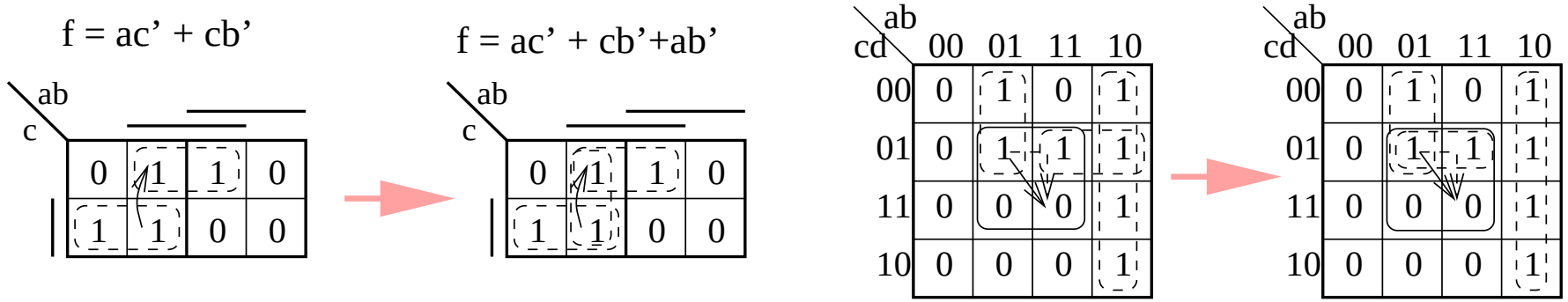
Function hazards in XBM

- Any single burst of transitions at the input of combinational logic is function hazard-free by construction of the next state table

- Assigning the next state values for different bursts of transitions can produce conflicts in the next state table = CSC problem for XBM

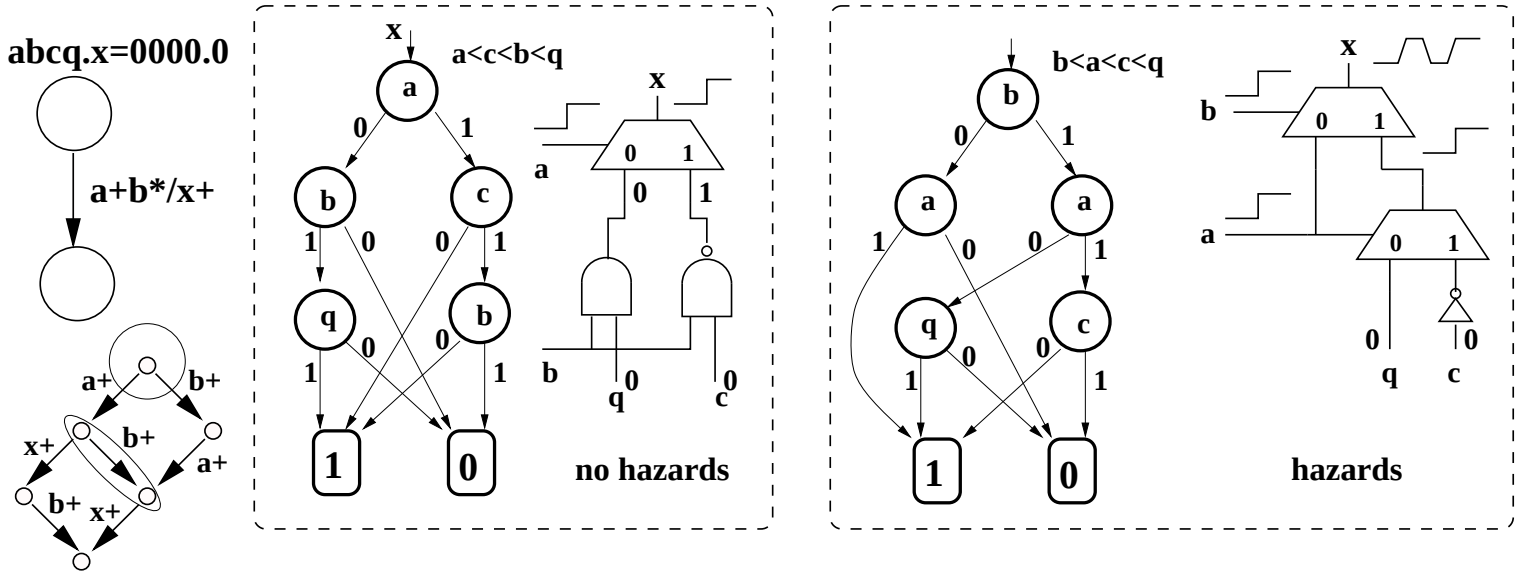
- To solve the conflicts use additional state signals and the race-free encoding.

Logic hazards in XBM. Sum-of-products logic



- Static hazards elimination condition:
  each transition cube is contained inside a cube of the cover
- Dynamic 1to0-hazard (0to1) elimination condition:
  if transition cube intersects cube c of the cover,
  then c contains the *start (end) cube* of the transition cube
- Conflicting requirements can be resolved by adding more state signals

Logic hazards in XBM. BDD-based logic



- $x = \overline{a}bq + a\overline{c} + a\overline{b}$. Signal a is a trigger for x, signal b - is not
- Trigger signals must precede non-trigger signals in variable ordering for BDD: $a < b$ is valid, $b < a$ – is not.
- Conflicting requirements can be resolved by adding more state signals

3D synthesis procedure

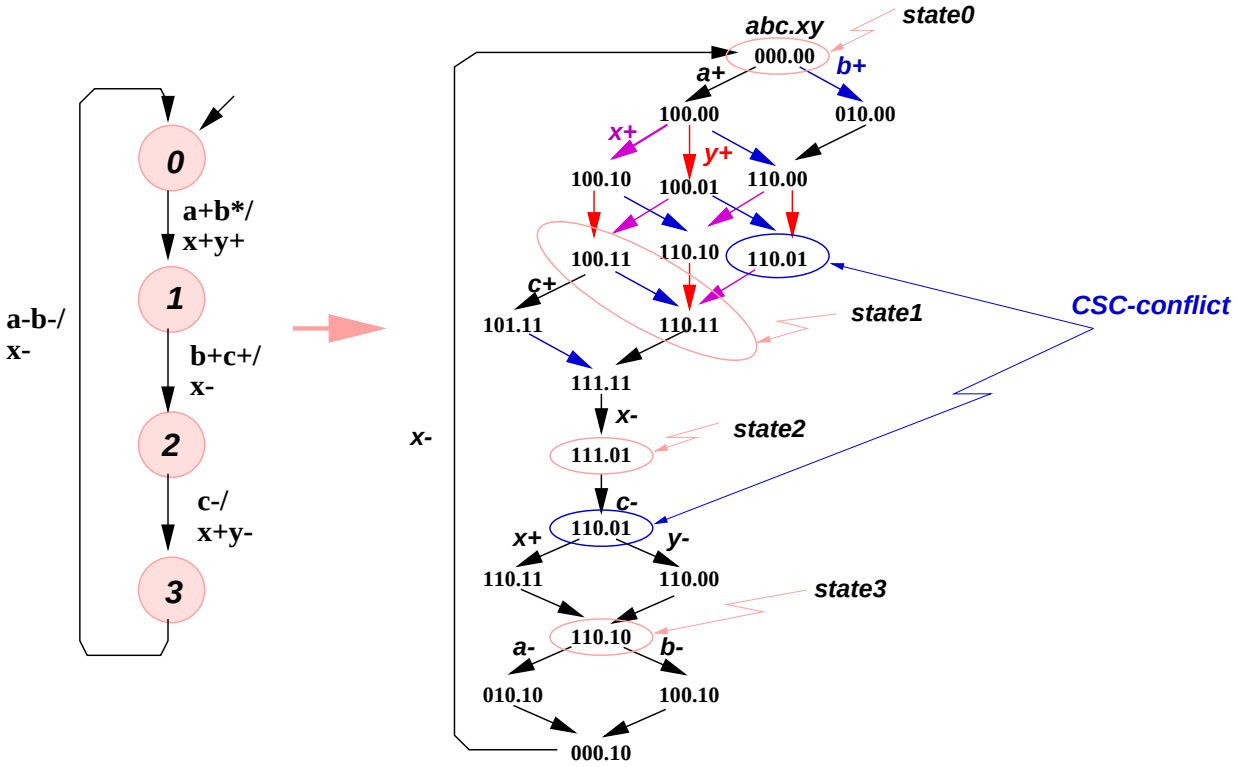
1. Next state assignment: one state of the specification to one layer of the Karnaugh map

2. Layer minimization: compatible layers are merged

3. Layer encoding: use adjustments of standard race-free encoding (Tracey)

4. Synthesis of hazard-free combinational logic (as described above)

State assignment in XBM and CSC



State assignment resolves conflicts in definition of the next state function similar to CSC-conflicts in STG synthesis

Layer minimization

- Standard state minimization for *incompletely* specified FSMs
- Compatibility of states (layers) defined differently
- State i and j are not compatible = cannot be merged in one layer without state conflicts (CSC) or violating requirements for hazard-freedom of logic
- Compatibility relation depends on the implementation of the combinational logic (SOP,BDD-based)

State compatibility